



## Full Length Article

# Microscopic control of SiGe/high- $\kappa$ oxide gate stack for p-MOSFET hole qubits

Ibrahim B. Adetunji<sup>a,b</sup>, Francesco Tavanti<sup>a,c,\*</sup>, Alessandra Catellani<sup>a</sup>, Arrigo Calzolari<sup>a</sup>

<sup>a</sup> CNR-NANO Istituto Nanoscienze, Centro S3, Modena I-41125, Italy

<sup>b</sup> Bells University of Technology, Physical Sciences Department, Ota, Ogun State, Nigeria

<sup>c</sup> Department of Chemical Sciences, University of Padova, via Marzolo 1, Padova 35100, Italy

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## ABSTRACT

The formation of  $\text{GeO}_x$  and  $\text{HfGeO}_x$  by-products, and the Ge diffusion at the interface between SiGe active layer and high- $\kappa$  amorphous gate oxide (a- $\text{HfO}_2$ ) are major issues that affect the mobility of SiGe channels in p-type metal-oxide-semiconductor field-effect transistors (MOSFETs). Experimental evidence suggests that the inclusion of multiple interlayers and Nitrogen incorporation may reduce these interface defects and prevent the formation of detrimental traps at the SiGe/oxide contacts. In this work, we address the problem by combining density functional theory and classical molecular dynamics simulations. Our results reveal that the introduction of an ultrathin a- $\text{SiO}_2$ /a-SiON bilayer between SiGe and a- $\text{HfO}_2$  is an efficient solution to eliminate the mixed oxides formation, preventing the diffusion of germanium into the gate oxide and improving the p-MOSFET efficiency.

## 1. Introduction

The potential of silicon-based charge-spin quantum-dot qubits as material for commercial complementary metal oxide semiconductor (CMOS) technology has generated a lot of interest due to their record coherence times and fidelity [1–4]. Despite of these characteristics, their operation has been limited to temperatures below 100 mK because of the low confinement and coupling energies [5,6]. Yet, getting qubit with higher confinement, higher coupling energies, and with spin resonance in the upper mm-wave region will give room for higher temperature operation. On the technological side, MOSFETs are the building blocks of modern electronic devices [7–9]. Thus, being able to realize stable qubits by exploiting the MOSFET technology would take advantage of the huge know-how in the field with an evident technological gain. Many materials such as Si-channel n-MOSFETs (electron-spin qubit) and SiGe-channel p-MOSFETs (hole-spin qubit) [10] are now being investigated for the realization of quantum-dot qubits with higher temperature and fidelity for quantum computing. In this case, the control and the stability of the resulting qubits rely on the control and the stability of the underlying MOSFETs device.

The size reduction and scaling of MOSFETs have contributed to the increased transistor density, improved performance and decreased power consumption in electronic devices [11–14]. However, these

remarkable gains are faced with problems such as low mobility of substrates, or metal gate and high- $\kappa$  dielectric integration [15–17]. Many efforts have been directed towards searching for: i. semiconductor channels with mobility higher than crystalline Si [18–24], for example strained silicon (sSi),  $\text{Si}_{1-x}\text{Ge}_x$  (SiGe), Ge and group III-V semiconductors [22,25–27]; ii. new gate materials with high- $\kappa$  dielectric alternative to the traditional amorphous a- $\text{SiO}_2$  in order to reduce gate leakage, such as a- $\text{HfO}_2$ , a- $\text{ZrO}_2$ ,  $\text{Al}_2\text{O}_3$ ,  $\text{Y}_2\text{O}_3$  and  $\text{La}_2\text{O}_3$  [15,28].

Among these materials, SiGe and amorphous  $\text{HfO}_2$  (a- $\text{HfO}_2$ ) are considered the materials of choice for the fabrication of p-MOSFETs (Fig. 1a) [29–34]. SiGe shows a high carrier mobility that can be fine-tuned by controlling the Ge content; while a- $\text{HfO}_2$  reduces the gate leakage with respect to fixed equivalent oxide thickness. Furthermore, a- $\text{HfO}_2$  has good thermodynamic and chemical stability, reasonable band offset and lack of dislocations and grain boundaries, which are prominent in the crystalline oxide gates [35–37]. The major concern in the implementation of these two materials into MOSFETs is the nature and quality of their inherent interface. The presence of interface defects is responsible for degradation which eventually affects the device performances.

Two main aspects are particularly critical: i. the formation of Si-O dangling bonds at the interface, which are responsible for trapping electronic states in the channel band-gap region [38–44]; ii. the

\* Corresponding author at: Department of Chemical Sciences, University of Padova, via Marzolo 1, Padova 35100, Italy.

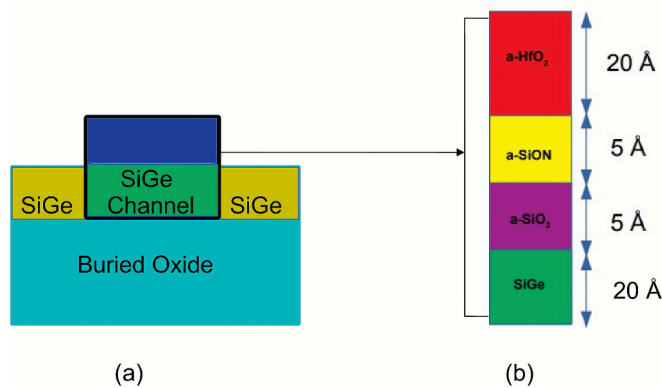


Fig. 1. Simplified cross-sectional scheme of SiGe p-MOSFET quantum dot.

diffusion of Ge atoms into the oxide layer and the formation of under-coordinated  $\text{GeO}_x$  complexes that nucleate the growth of  $\text{GeO}_2$  impurities [45–49].

The formation of  $\text{SiO}_x$  dangling bonds can be reduced by including a subnanometer layer of oxides such as  $\text{SiO}_2$  [37,50] or  $\text{Al}_2\text{O}_3$  [51], while selective oxygen scavenging [40,52] and passivation with nitrides and sulfur [53–58] are useful to decrease the amount of Ge concentration [43]. However, these solutions are not sufficient to prevent Ge to diffuse through the oxide surface, resulting into degrading defect states. This drawback can be mitigated using multiple interlayer (IL) insertion within the SiGe/a- $\text{HfO}_2$  interface.

In this study, we investigated the SiGe/a- $\text{SiO}_2$ /a-SiON/a- $\text{HfO}_2$  gate stack, following the experimental prescriptions proposed by S. Krishnan and coworkers [59,60]. The inclusion of the two ILs improves the stability of the overall system, by reducing the formation of both  $\text{SiO}_x$  and  $\text{GeO}_x$  dangling bonds. Albeit this model structure has been adopted *de facto* by several fabrication factories, the origin of this behavior is still unclear. Here, by using a multi-scale/multi-physics approach based on classical molecular dynamics and density functional theory (DFT), we provide a microscopic understanding of this multilayer channel-gate stack. This opens the way to the realization of stable and controllable SiGe-channel p-MOSFETs that could be used for the production of quantum-dot qubits with high temperature and fidelity.

## 2. Methods

Structural and electronic ground-state simulations have been carried out through first principles approaches based on density functional theory, as implemented in the Quantum Espresso(QE) package [61–63]. In the treatment of the exchange–correlation potential, we used PBE generalized gradient approximation (GGA) [64]. Atomic potentials were described by ultrasoft pseudopotentials of the Vanderbilt’s type [65]. Single particle wavefunctions and charge were expanded on a plane wave basis with kinetic energy cutoff of 25 Ry and 250 Ry respectively that give a good compromise between accuracy and computational cost for both layer and interface systems. In the case of bulk  $\text{HfO}_2$  only, the cutoff was chosen to be 50 Ry to take have a higher resolution in the possible localized states. Brillouin-zone integration was performed using  $\Gamma$ -point during the atomic relaxation, and with a uniform  $(2 \times 2 \times 1)$  Monkhorst-Pack k-points mesh for the evaluation of the electronic structure.

Underestimation of the band gap, typical of standard DFT-GGA functionals, has been corrected by including a Hubbard-like potential, within the DFT + U frameworks along the lines described, e.g., in Ref. [66]. The optimized values for chemical species have been obtained for each isolated compound (i.e. SiGe,  $\text{SiO}_2$ , SiON, and  $\text{HfO}_2$ ) by using the pseudohybrid Hubbard Density Functional approach (namely ACBN0) [67], implemented in the AFLOW $\pi$  infrastructure code [68]. The effects of the ACBN0 approach on the structural, electronic and

vibrational properties of inorganic semiconductors have been largely tested in previous reports (see e.g. Refs. [69,70]).

The semiconductor channel is modeled through a periodic supercell including a  $\text{Si}_{0.75}\text{Ge}_{0.25}(001)$  surface, accordingly to experimental works and commonly fabricated devices and previous works [37,71], with a  $(2 \times 2)$  lateral periodicity of dimension  $(11.15 \times 11.15) \text{ \AA}^2$  and  $11.15 \text{ \AA}$  of thickness, obtained through geometry optimization of the  $(2 \times 2 \times 2)$  cubic supercell. A  $15 \text{ \AA}$ -thick layer of vacuum was added to prevent interactions between periodically repeated slab replicas. The bottom layer was passivated with Hydrogen atoms. Hereafter, if not explicitly stated, we will refer  $\text{Si}_{0.75}\text{Ge}_{0.25}$  simply as SiGe.

In order to simulate the SiGe/oxide stacks, we considered the direct SiGe/a- $\text{HfO}_2$  interface and three multilayers with increasing complexity, as presented in Fig. 1(b): (i) SiGe/a- $\text{SiO}_2$ , (ii) SiGe/a- $\text{SiO}_2$ /a-SiON, and (iii) SiGe/a- $\text{SiO}_2$ /a-SiON/a- $\text{HfO}_2$ .

The initial structure of the single amorphous oxides  $\text{SiO}_2$ , SiON and  $\text{HfO}_2$ , have been obtained from classical molecular dynamics simulations. The three amorphous materials have been modeled in bulk-like configurations having the same lateral periodicity of the SiGe substrate (i.e.  $11.154 \text{ \AA}$ ), and different thicknesses, as proposed in the experimental systems [59]:  $5.0 \text{ \AA}$  for both  $\text{SiO}_2$  and SiON,  $20.0 \text{ \AA}$  for  $\text{HfO}_2$ . The respective crystal structures have been melted to a temperature of  $3000 \text{ K}$  for  $10 \text{ ns}$  in order to have a complete liquid phase ensuring the loss of the initial memory of the crystalline system. Then, each system has been cooled down to the temperature of  $300 \text{ K}$  with a cooling rate of  $10 \text{ K/ps}$ , which ensures the correct formation of the amorphous/glass phase while maintaining a quite low computational effort [72]. After the system reached the  $300 \text{ K}$  temperature, a production run of  $20 \text{ ns}$  in the NVT ensemble has been performed at constant temperature of  $300 \text{ K}$  using the Nose-Hoover thermostat with a coupling time of  $1 \text{ ps}$  and with a timestep of  $2 \text{ fs}$ . All classical MD simulations have been performed using the GULP package [73]. For each system, we employed different force fields that were able to reproduce the main structural features of the single materials: for  $\text{SiO}_2$  the parameters were obtained from the work of Pedone et al. [74], explicitly developed for glassy dioxides; for SiON the Reax force field from Van Duin et al. [75] has been used; and for the  $\text{HfO}_2$  parameters were obtained from the work of Broglia et al. [76] that accurately describe lattice parameters and bond lengths. The radial distribution function,  $g(r)$ , (see Supplementary Materials Fig. S1) has been computed on the last  $5 \text{ ns}$  of the production run using the VMD package [77]. A representative snapshot of each oxide bulk has been assumed as initial structure for the DFT total-energy-and-forces optimization of the corresponding 2D layer, obtained by including in the simulation cell a vacuum space in the direction perpendicular to the surface. The final DFT configuration for each layer ( $\text{SiO}_2$ , SiON and  $\text{HfO}_2$ ) was used to compose the stacks. By construction, all amorphous layers were generated in a simulation cell having the same lateral periodicity of SiGe(001) and then relaxed at the DFT layers. For the preparation of the interface structures, we sequentially stacked the relaxed oxide layers on top of the SiGe slab. Thus, the SiGe/a- $\text{SiO}_2$  interface is obtained by setting the a- $\text{SiO}_2$  layer on the SiGe (001) surface and then relaxed with DFT. Then, the SiON layer was added on the previous relaxed SiGe/a- $\text{SiO}_2$  interface; the ternary system has been further relaxed at the DFT level. Lastly, the  $\text{HfO}_2$  was stacked on the ternary system obtaining the SiGe/a- $\text{SiO}_2$ /a-SiON/a- $\text{HfO}_2$  multilayer that has been also optimized at the DFT level. Each IL has been manually placed over the previous structure avoiding superimposition of atoms by maintaining an initial average distance between interface atoms of  $\sim 2 \text{ \AA}$ , which is of the order of the average distance between pairs involved in the interfaces (e.g. Si-O, Si-Ge, etc). Atomic bonds at the interface are optimized during the relaxation processes. Notably, since oxides are amorphous, they can easily accommodate small deviations in atomic positions without introducing long-range elastic strain. In a similar way, the binary SiGe/ $\text{HfO}_2$  interface, i.e. without ILs, has been also simulated for comparison, by combining the two composing slabs.

All the structural DFT relaxations were performed using QE. All unrelaxed and relaxed atomic structures are collected in the *Supplementary Materials Figs. S2(a–d)*. This procedure to build multi-layer stacks has been already employed in previous work, where crystalline surfaces have been capped with amorphous materials for electronic applications and showing very good agreement with experimental results on devices [78].

### 3. Results and discussion

#### 3.1. Composing layers

We first considered the SiGe surface and the single oxide layers, separately. Structural relaxation plays a key role in the realization of stable amorphous oxides, because of the presence of local-order structures and non-stoichiometric defects (e.g. over- and under-coordinated atoms). Bond lengths of each material are reported in *Table 1* and compared with previous results obtained by Neutron diffraction, EXAFS, and ab initio molecular dynamics simulations. All values from both MD and DFT are close to each other and in good agreement with previously published results. In the case of SiON, the N-N first peak of  $g(r)$  at 1.11 Å is very narrow and followed by a broader peak at 2.90 Å, in agreement with experimental work [79]. Major structural rearrangements occur at SiGe surface where Si and Ge atoms from rows of buckled dimers along the [1 1 0] direction, see *Supplementary Materials Fig. S2(a)*. The resulting Si-Si, Ge-Ge and Si-Ge bond lengths from  $g(r)$  (2.42 Å, 2.49 Å, 2.44 Å, respectively) are in agreement with the reported data [80–82]. Similarly, a-HfO<sub>2</sub> and a-SiO<sub>2</sub> structures undergo strong atomic rearrangement at surface, as presented in *Supplementary Materials Figs. S2(b and d)*. The Si-O and Hf-O bond lengths before and after relaxations in both structures are 1.65(1.63) and 2.19(2.07) Å respectively, in agreement with available data [83–85]. In the case of a-SiON, a very pronounced redistribution of Si, O and N atoms occurred after DFT relaxation (*Supplementary Materials Fig. S2(c)*). This is most probably due to the Force Field employed in MD simulation that is not specific for SiON alloys. In particular, we observed the formation of 2N-N dimers and the clustering of Si and O atoms. The Si-O, Si-N and N-N bond lengths before and after relaxation are: 1.55(1.65), 1.95(1.71) and 1.25(1.25) Å respectively. The optimized DFT values are in agreement with available data [86].

The density of states (DOS) plots of SiGe and of the three considered oxides are shown in *Fig. 2(a–d)*, the zero energy reference is set to the Fermi level ( $E_F$ ) of each system. Electronic structures were calculated

**Table 1**

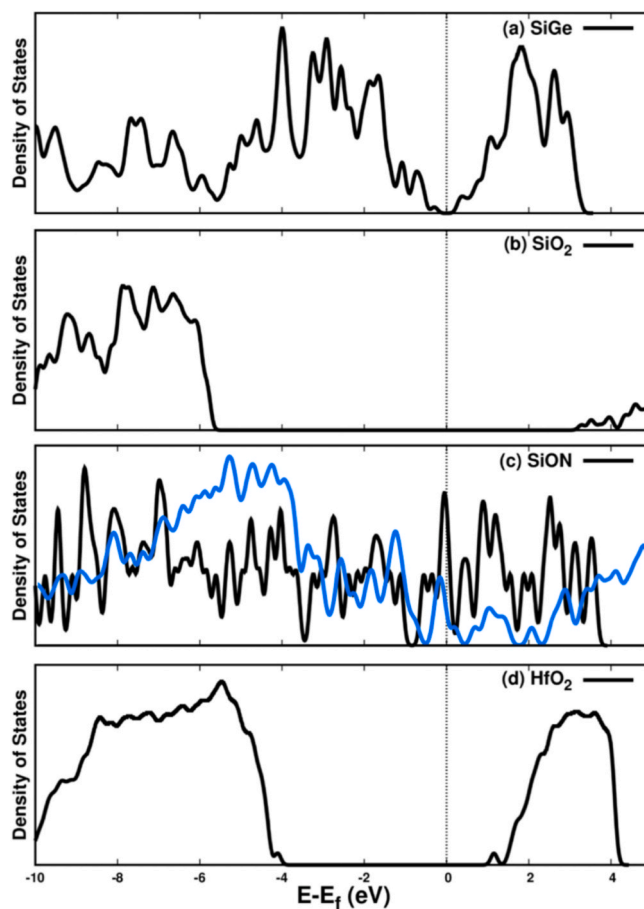
The bond lengths expressed in Å for each pair for the three amorphous systems obtained by classical Molecular Dynamics (MD) and by DFT calculations (DFT).

System	Bond (Å)	This work (MD)	This work (DFZ)	Exptl. And Comp. results
SiO <sub>2</sub>	Si–O	1.65	1.63	1.61 <sup>a</sup>
	Si–Si	3.07	3.05	3.07 <sup>a</sup>
SiON	O–O	2.63	2.65	2.63 <sup>a</sup>
	Si–O	1.55	1.65	1.61 <sup>a</sup>
	Si–Si	3.07	3.00	3.06 <sup>b</sup>
	O–O	2.50	2.65	2.60 <sup>b</sup>
	Si–N	1.95	1.71	1.73 <sup>b</sup>
	O–N	2.90	2.75	
	N–N	1.25/2.90	1.25	2.97 <sup>b</sup>
HfO <sub>2</sub>	Hf–O	2.08	2.07	2.08/2.11 <sup>c</sup>
	Hf–Hf	3.53	3.32/3.80	3.32/3.39 <sup>c</sup>
	O–O	2.70	2.65	2.55/2.69 <sup>c</sup>

<sup>a</sup> Ref. [87] and [88].

<sup>b</sup> Ref. [79].

<sup>c</sup> Ref. [76] and [89].



**Fig. 2.** Density of states (DOS) plots for (a) SiGe(001), (b) a-SiO<sub>2</sub>, (c) a-SiON<sub>2</sub>, and (d) a-HfO<sub>2</sub> isolated surfaces. Vertical dashed lines mark the Fermi energy ( $E_F$ ) of each system. In panel c) the black line represents the 42 atoms system and the blue line the 126 atoms system.

within the DFT + U framework (see Method). SiGe, a-SiO<sub>2</sub> and a-HfO<sub>2</sub> exhibit the expected semiconductor character, with a calculated energy bandgap of 0.58 eV, 9.05 eV and 5.24 eV respectively, in excellent agreement with previously reported data [35,90]. No defect states are observed in the gap, except for a small shallow state appearing close to the conduction region for a-HfO<sub>2</sub>. On the contrary, a-SiON displays a conductor-like behavior, with no-recognizable band gap (*Fig. 2(c)*) in contrast with the 2–5.5 eV gaps reported for crystalline and stoichiometric amorphous Si<sub>2</sub>N<sub>2</sub>O [91]. This is due to the non-stoichiometric composition and high defect density of the simulated layer, arising from the melt-quench procedure, and due to the small thickness of the film that favors the formation of trap states in the gap [92]. In particular, the model layer contains undercoordinated Si and N atoms, Si–Si bonds, and oxygen vacancies, each of them generates localized states which fill and reduce the nominal mobility gap. This result is consistent with previous reports of effective band gap narrowing in SiON for O/N-deficient compositions or high concentrations of coordination defects [91,92]. The high number of dangling bonds in SiON thin film is mainly given by O and N atoms that are not fully coordinated, especially those on the surface. However, the number of O-dangling bonds drastically reduces when the SiON stack is deposited on the SiGe-SiO<sub>2</sub> interface with fewer N-dangling bonds that still persist due to the presence of surface atoms exposed to vacuum. Yes, this is an intermediate configuration during the growth process. Indeed, when HfO<sub>2</sub> also cover the top of the stack, these defect states fully disappear, as reported in *Fig. S3*. This confirms that the presence of frustrate bonds (and corresponding defect states in the DOS) in the isolated films of in the intermediate

structures is not an issue for the final multilayer. Therefore, the absence of a net gap in our model is a feature of the specific ultra-thin, disordered, defect-rich SiON layer structure generated here, while it is not representative of ideal stoichiometric  $\text{Si}_2\text{N}_2\text{O}$  bulk, which has a well-established semiconducting behavior. To confirm this trend, we built for comparison a thicker SiON layer (12.311 Å) composed of 126 atoms in its amorphous state phase and performed electronic states calculation using the same set of parameters of the other runs. By computing the DOS (blue line in Fig. 2c), we observe a band gap of approximately 6 eV with several trap states within the gap, confirming that lowering the SiON thickness results in an increase in the defect states that close the real band gap.

The electronic states across the Fermi level stem mostly from the 2p lone pairs of nitrogen, as previously reported in Ref. [92]. However, the comparison between the single-particle orbitals of a-SiO<sub>2</sub> and a-SiON indicates that an evenly amount of O atoms also contributes to the metal-like feature of a-SiON.

### 3.2. Multilayer stacks

Fig. 3 collects the relaxed multilayer structures obtained stacking SiGe and the amorphous oxides with (SiGe/a-SiO<sub>2</sub>, SiGe/a-SiO<sub>2</sub>/a-SiON, and SiGe/a-SiO<sub>2</sub>/a-SiON/a-HfO<sub>2</sub>) and without (SiGe/a-HfO<sub>2</sub>) the oxide interlayers. The direct contact between SiGe and a-HfO<sub>2</sub> (panel b) favors the formation of under-coordinated GeO<sub>x</sub> and SiO<sub>x</sub> pairs due to the presence of oxygen atoms at the interface. HfO<sub>2</sub> does not block the Ge diffusion of Ge across the surface favoring the formation of HfGeO<sub>x</sub> composites that are known to degrade the electrical quality of the interface by increasing the leakage current [45,93]. The comparison between the DOS spectra of SiGe surface and SiGe/a-HfO<sub>2</sub> interface (Fig 4a) confirms the experimental expectation [45]. The DOS plot shows the appearance of HfGeO<sub>x</sub>-derived states that completely fill the pristine SiGe band gap and impart a conducting-like character to the interface. The presence of these states at the Fermi level (vertical dashed line in Fig 4) is responsible for the increase of the leakage current observed in the experiments.

Covering SiGe with the a-SiO<sub>2</sub> layer (panel c) allows for a better saturation of the surface Si atoms of SiGe and the reduction of the Si-O

dangling bonds, as reported in Fig. S3. Although the amorphous oxide was generated by a melt-quench procedure rather than by explicitly modeling O<sub>2</sub> incorporation as in real devices [94], including the a-SiO<sub>2</sub> layer partially mimics the effect of the oxidation process by providing a stoichiometric SiO<sub>2</sub> environment that passivates Si bonds and reproduces the structural role of an interfacial oxide in real devices. Yet, a-SiO<sub>2</sub> is permeable to Ge that easily penetrates into the oxide layer forming undercoordinated SiGeO<sub>x</sub> mixed oxides. Structural analysis shows that Ge atoms migrate through the amorphous SiO<sub>2</sub> via interstitial-like hopping between transient free-volume pockets. These hops are enabled by bond-switching events in the Si-O network, in which Ge coordinates to non-bridging oxygens or replaces Si in a local Si-O unit, forming Ge-O bonds before moving onward. This is facilitated by the intrinsic disorder and variable ring sizes in amorphous silica, which provide low-coordination sites and diffusion channels absent in crystalline silica. Moreover, the analysis of Ge displacement along the Z-direction reported in Fig. 2 shows two main features: 1) the SiGe-SiO<sub>2</sub> interface modifies the vertical Ge distribution, with the formation of a Ge-rich region followed by a Ge-poor layer; 2) the formation of a Ge-rich region at the top of SiO<sub>2</sub> IL, given by the Ge diffused atoms across the oxide. The Ge condensation at interface, that we observed through a total-energy-and-force structure relaxation, well agrees with the results of previous MD simulations [95], which show how Ge atoms aggregate at the oxide interface during the oxidation process characteristic of the SiGe fabrication.

To confirm the diffusion process and the stability of the obtained structure SiGe-SiO<sub>2</sub> interface, we performed two sets of Car-Parrinello ab initio dynamics (AIMD) at T = 300 K and T = 500 K for 10 ps each, to mimic working conditions and to accelerate dynamics. At both temperatures, the system remains stable (small values of Root Mean Square Fluctuations, RMSF, in Fig. 5a) with the same interatomic connectivity. The minor structural changes are only due to thermal fluctuations of atoms up to 0.5 Å, especially in the oxide region, having restrained the H-atoms at the bottom layer, as reported in Fig. 3a. In a similar way, also the small differences in the peak height of partial g(r) plots (Fig. 5b) from the relaxed (i.e. static) and AIMD simulations, are directly ascribable to the thermal fluctuations of atoms at finite temperatures.

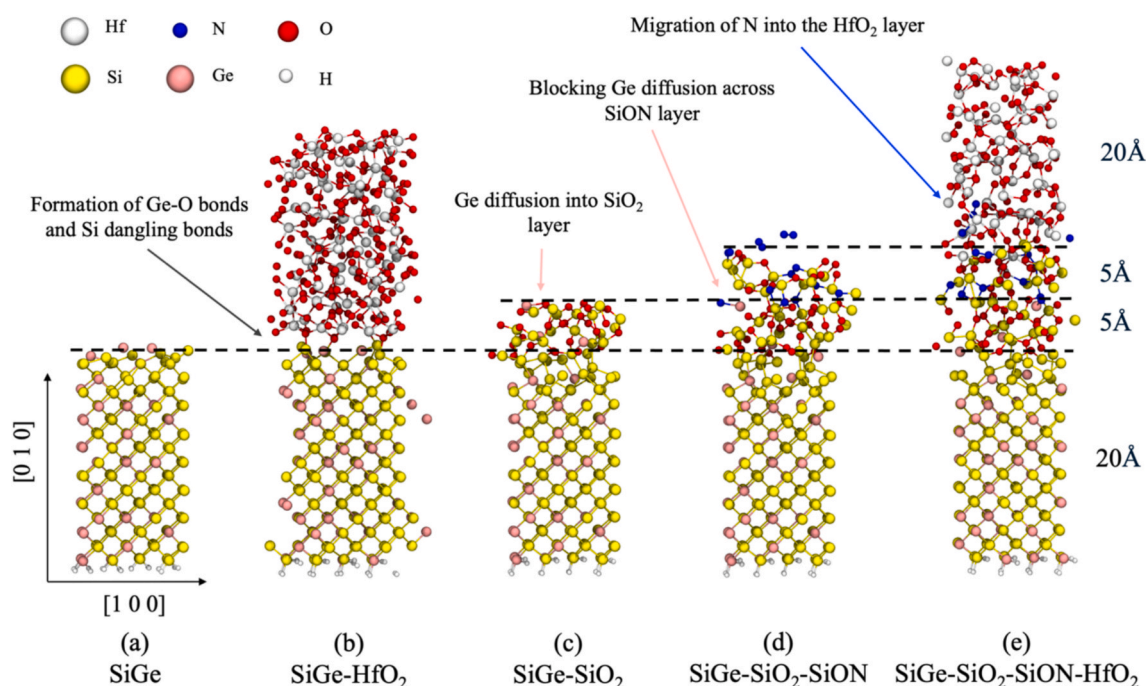


Fig. 3. Optimized atomic structure of SiGe surface and multiple SiGe/amorphous-oxide stacks.

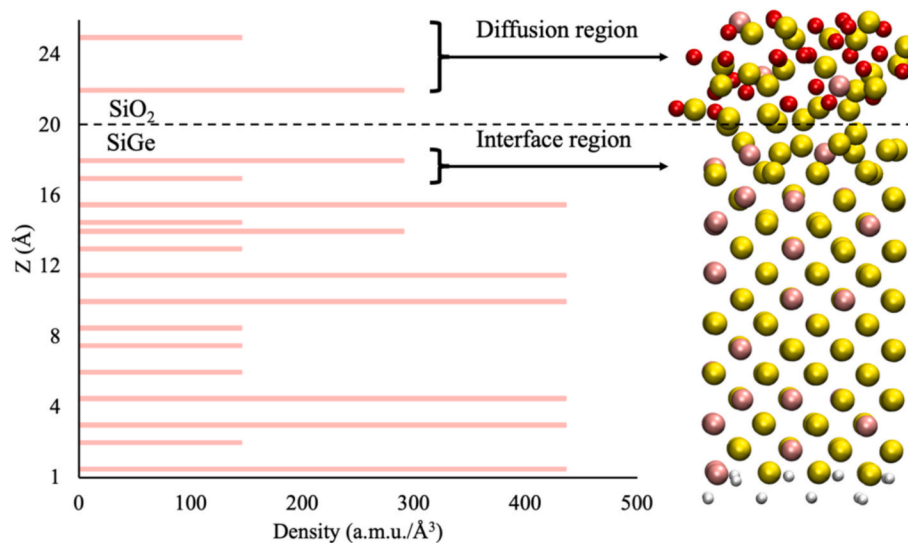


Fig. 4. Density of Ge atoms along the Z-direction where there are highlighted the Ge condensation at the interface region and the Ge atoms that diffuse into SiO<sub>2</sub> IL.

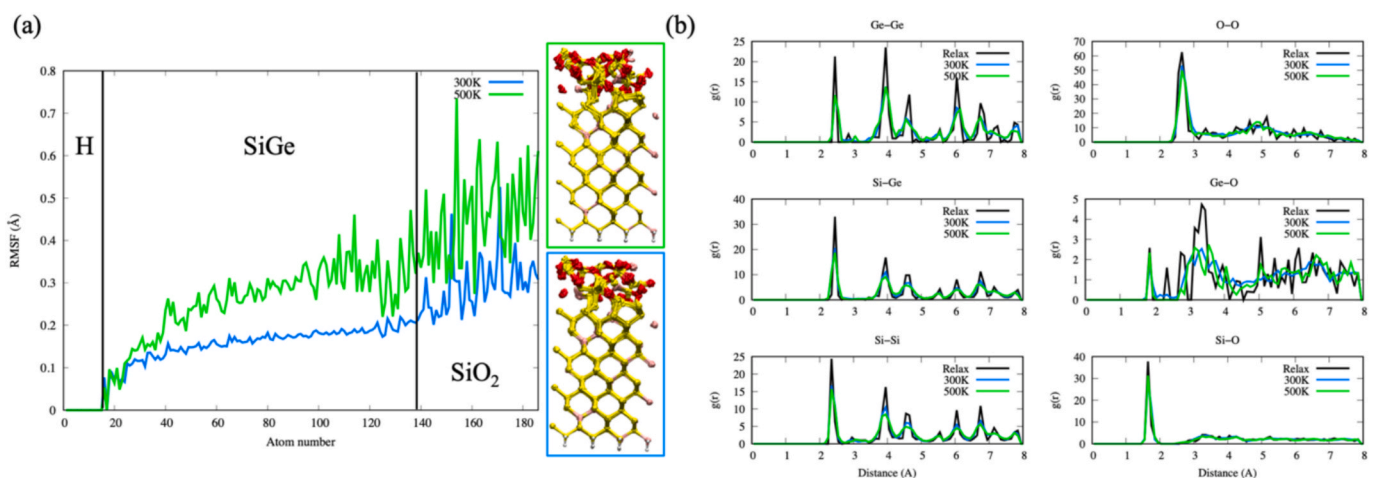


Fig. 5. (a) The RMSF and the superimposition of atomic structures at 300 K and 500 K AIMD. (b) The comparison of the partial  $g(r)$  at both temperatures and for the relaxed structure.

The mixture of GeO<sub>x</sub> (parasitically unstable) and residual SiO<sub>x</sub> could create interface-trapped charge density defects [37]. However, the electronic structure results (Fig. 6) indicate: i. the formation of a type-I band-alignment with the SiGe bandgap completely included in the a-SiO<sub>2</sub> one, ii. the absence of both Si- and Ge-derived defect states in the bandgap of the SiGe/a-SiO<sub>2</sub> interface, which preserves the energy gap (0.36 eV) of pristine SiGe. The analysis of the optimized structure indicates also the spontaneous diffusion of Ge atoms (pink balls) across the a-SiO<sub>2</sub> layer, with the Ge atoms that reach the upper surface of the oxide layer (Fig. 3c). This implies that – without further spacers – Ge could again be in touch with the a-HfO<sub>2</sub> surface, as in the binary interface. Thus, inclusion of a-SiO<sub>2</sub> is an efficient strategy to optimize the SiGe surface, but not to curate the Ge mobility. We obtained the spontaneous diffusion of Ge atoms with DFT relaxations without temperature effects, suggesting that our simulations take into account the kinetic effects.

The incorporation of a nitridation interfacial layer has been experimentally proved to prevent Ge diffusion into a-HfO<sub>2</sub> [45] and further improve the interface quality. Therefore, we added an amorphous oxynitride (a-SiON) interlayer on the top of SiGe/a-SiO<sub>2</sub> stack. The relaxed atomic configuration of the ternary multilayer is shown in Fig. 3(d). Upon structural relaxation, the a-SiON layer effectively inhibits the diffusion of Ge atoms across the interface due to its denser atomic

structure, strong Si-N (1.71 Å) and Si-O (1.65 Å) bonding and low oxygen diffusivity [96]. Additionally, nitrogen partially diffuses into the lower SiO<sub>2</sub> layer as well as it segregates on the outermost layer, by forming N-N dimers weakly bonded to the top surface of the stack. The suppression of Ge diffusion by the oxynitride layer eventually prevents the undesirable formation of HfGeO<sub>x</sub> phases during subsequent stacking a-HfO<sub>2</sub>, while the generation of N-N bonds may cause the establishment of further localized gap states near the Fermi level, which may impact the electronic properties of the interface. In fact, the DOS of the SiGe/a-SiO<sub>2</sub>/a-SiON stack (Fig. 6c) displays a non insulating features, with a N-derived sharp peak laying at the Fermi level.

We finally re-introduced the a-HfO<sub>2</sub> on top of the previous stack to form SiGe/a-SiO<sub>2</sub>/a-SiON/a-HfO<sub>2</sub> multilayer. The optimized structure is shown in Fig. 3(e). After relaxation, we observe significant intermixing between a-SiON and a-HfO<sub>2</sub>, while Ge atoms remain segregated within the a-SiO<sub>2</sub> slab, as discussed above, obtaining an oxide layer (SiO<sub>2</sub>-SiON) with thickness between 10Å and 11Å due to diffusivity phenomena. This minimizes the possibility to form the detrimental HfGeO<sub>x</sub> composites at the interface. Furthermore, the previous N-N dimers moved inside a-HfO<sub>2</sub> and formed 3-fold coordination with Hf atom. The N-N-Si-O bridge formed in lower SiGe/a-SiO<sub>2</sub>/a-SiON interface migrated upwards, towards the a-HfO<sub>2</sub> layer, which gives rise to the

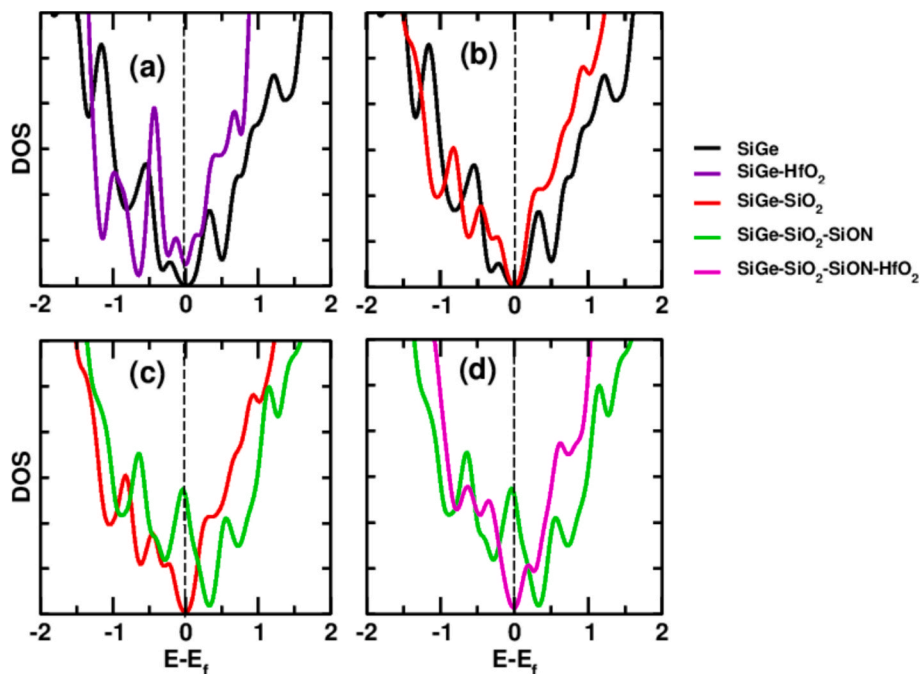


Fig. 6. Density of states for (a) SiGe/HfO<sub>2</sub> (b) SiGe/a-SiO<sub>2</sub> (c) SiGe/a-SiO<sub>2</sub>/a-SiON, and (d) SiGe/a-SiO<sub>2</sub>/a-SiON/a-HfO<sub>2</sub> multiple interfaces. Vertical dashed lines mark the Fermi energy ( $E_f$ ) of each interface.

formation of two octahedral coordinated Hf atoms.

In order to gain further insights into the structural effects of the IL inclusion, we compared the SiGe/HfO<sub>2</sub> and the SiGe/a-SiO<sub>2</sub>/a-SiON/a-HfO<sub>2</sub> interfaces. We computed the atomic density of each chemical along the z-axis (i.e. perpendicular to the multilayer), as reported in Fig. 7. In SiGe/HfO<sub>2</sub>, the different chemical composition prevents any bond

continuity across the interface and the formation of under-coordinated sub-composites. In the complete system, we observe a smoother interface region that maximizes the suppression of under-coordinated sites and dangling bonds. In particular, the first SiO<sub>2</sub> maintains the continuity of Si-bonds and introduces oxygen that is the common element also of the remaining layers. Ge partially diffuses in the SiO<sub>2</sub> layer, remaining

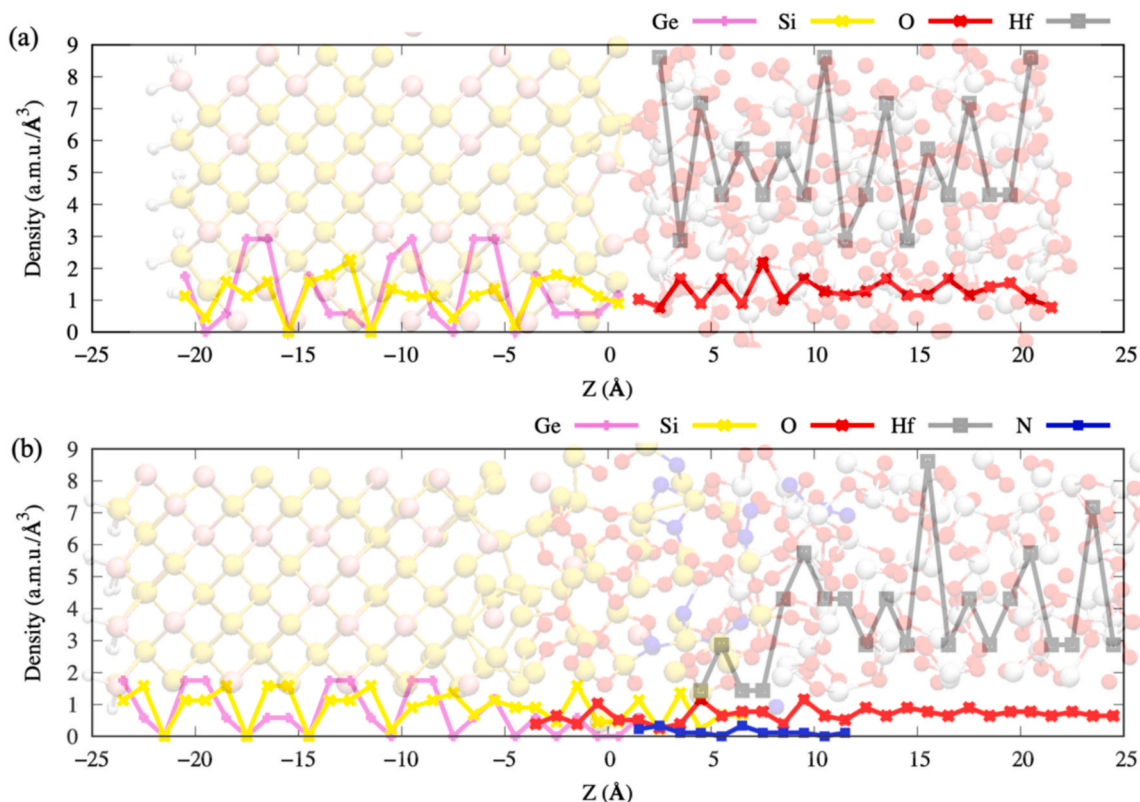


Fig. 7. Atomic density distribution of each chemical species along the z-direction for (a) SiGe/HfO<sub>2</sub> and (b) the SiGe/SiO<sub>2</sub>/SiON/HfO<sub>2</sub> interfaces.

blocked within a-SiON. Hf slightly diffuses into the a-SiON layer, but without reaching the Ge-diffusion region, while N spatially spreads over 10 Å between SiO<sub>2</sub> and HfO<sub>2</sub>, i.e. doubling the 5 Å thickness of the initial structure.

The different bonding path and the local order redistribution can be quantified by computing the q-value parameter, which is a measure of the local disorder around each atom based on the first shell of neighbors, by using the BELLO code [97,98]. The q-value is defined as:

$$q = 1 - \frac{3}{8} \sum_{k>i} \left( \frac{1}{3} + \cos\theta_{ijk} \right)^2 \quad (1)$$

where  $\theta_{ijk}$  is the angle formed by atoms  $i$  and  $k$  with the central atom  $j$ . The local order parameter can assume values from 1, (perfect tetrahedral network) to 0 (six-fold octahedral network) and to  $-2$  (six-fold non-octahedral network). The q-value for the SiGe/HfO<sub>2</sub> systems has a large jump from 1 in the crystalline SiGe to the disordered HfO<sub>2</sub>, where the q-values have a large distribution, see Fig. 8. In the case of SiGe/SiO<sub>2</sub>/SiON/HfO<sub>2</sub>, the q-value is 1 in the SiGe region and decreases much more smoothly in the SiO<sub>2</sub> layer.

This multiple atom rearrangement has a positive effect on the electronic properties of the overall multilayer, as indicated by the DOS spectra in Fig. 6(d). The complete stack recovers the expected insulating character, with an energy gap of 0.31 eV associated to the SiGe channel. Neither SiO<sub>x</sub> nor HfGeO<sub>x</sub> derived states appear in the SiGe bandgap: the inclusion of the a-HfO<sub>2</sub> saturates the N-N dangling bonds emptying the bandgap. O-derived localized states, associated to outermost a-HfO<sub>2</sub> are detected far from the Fermi energy, well inside the valence band.

Fig. 9(a) shows the charge density difference  $\Delta\rho(z)$  along the z-direction, defined as the difference between the charge density of the complete stack and of those of the single layers:

$$\Delta\rho = \rho(\text{SiGe/SiO}_2/\text{SiON/HfO}_2) - \rho(\text{SiGe}) - \rho(\text{SiO}_2) - \rho(\text{SiON}) - \rho(\text{HfO}_2) \quad (2)$$

At the SiGe/a-SiO<sub>2</sub> interface  $\Delta\rho(z)$  has a large negative value, which indicates a net charge transfer from SiGe to a-SiO<sub>2</sub> and the formation of an interfacial dipole. The remaining part of the multistack exhibits a charge accumulation at the single oxide/oxide interfaces. The PDOS of Fig. 9(b) shows that the SiGe band gap (in green) is fully enclosed within the HfO<sub>2</sub> band gap, evidencing a type-I band alignment and no interface-induced mid-gap states are observed within the SiGe band gap.

#### 4. Conclusion

We have examined the effects of multiple interlayers insertion between Si<sub>0.75</sub>Ge<sub>0.25</sub> and a-HfO<sub>2</sub> oxide with the aim of reducing the formation of GeO<sub>x</sub> and HfGeO<sub>x</sub> composites, eliminating Ge out-diffusion, and subsequently creating a defect-free interface. Our results revealed that combining SiGe and a-SiO<sub>2</sub> oxide as the first interlayer, Ge atoms are able to migrate into the aSiO<sub>2</sub> which resulted into the formation of SiGeO<sub>x</sub> mixed oxides. The introduction of a second interlayer (a-SiON oxide) is able to block the Ge diffusion but it caused the appearance of defect trap states that could negatively increase the leakage current. The complete stacking arrangement SiGe/a-SiO<sub>2</sub>/a-SiON/a-HfO<sub>2</sub> shows a type-I band alignment, restores the necessary semiconducting character of the interface whilst protecting the HfO<sub>2</sub> layer from Ge and the generation of HfGeO<sub>x</sub> micro-composites. We can thus conclude that, despite a greater structural complexity, the insertion of multiple interlayers between SiGe and a-HfO<sub>2</sub> oxide is an efficient solution to obtain high quality high- $\kappa$  oxide gate stacks for p-MOSFET applications. Our results allow to optimize strategies to reduce leakage currents and device instabilities induced by Ge migration at the high-k oxide in p-MOSFETs, without altering much the device engineering cost due to the increased structural complexity. This is a necessary step towards the realization of efficient p-MOSFET hole qubits.

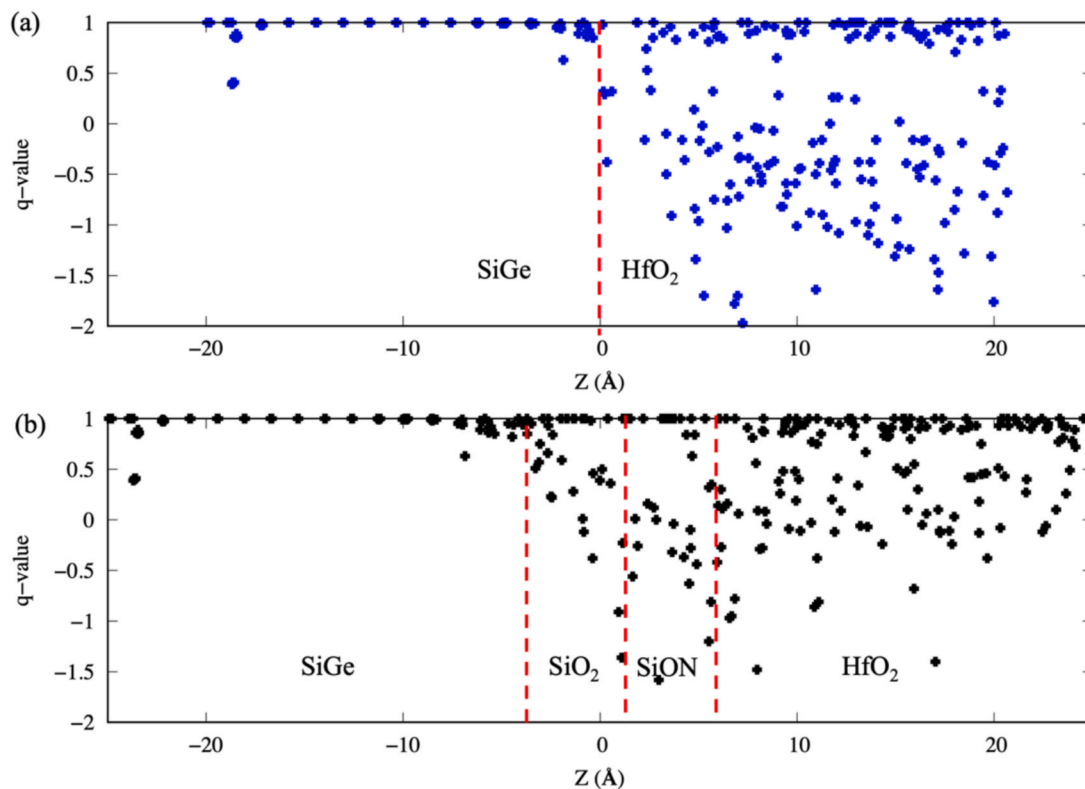
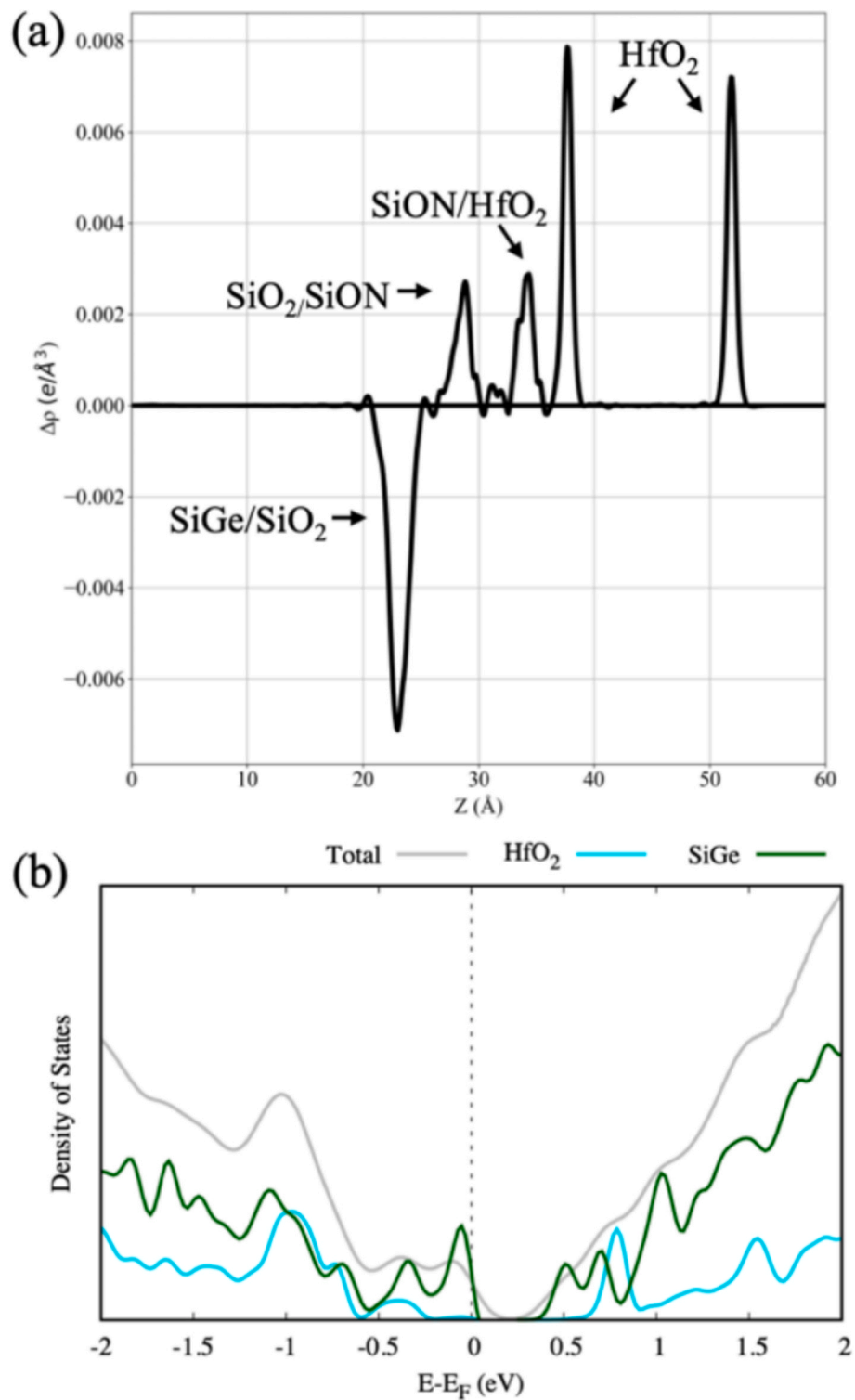


Fig. 8. The q-value distribution along the z-direction for (a) SiGe/HfO<sub>2</sub> and (b) the SiGe/SiO<sub>2</sub>/SiON/HfO<sub>2</sub> interfaces. Red vertical lines identify the spatial position of the interfaces along the z-axis.



**Fig. 9.** (a) Charge density difference profile along the  $z$ -direction, across the SiGe/ $a$ -SiO<sub>2</sub>/ $a$ -SiON/ $a$ -HfO<sub>2</sub> interface. (b) Local PDOS of SiGe and HfO<sub>2</sub> in the interface system showing that SiGe lies in the band gap of HfO<sub>2</sub>.

#### CRediT authorship contribution statement

**Ibrahim B. Adetunji:** Writing – original draft, Investigation, Formal analysis, Data curation. **Francesco Tavanti:** Writing – review & editing, Investigation. **Alessandra Catellani:** Writing – review & editing, Supervision. **Arrigo Calzolari:** Writing – review & editing, Supervision, Conceptualization.

#### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.apsusc.2025.165552>.

## Data availability

Data will be made available on request.

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