

Retrieval of surface emissivity from FORUM-EE9 simulated measurements: optimization of constraints

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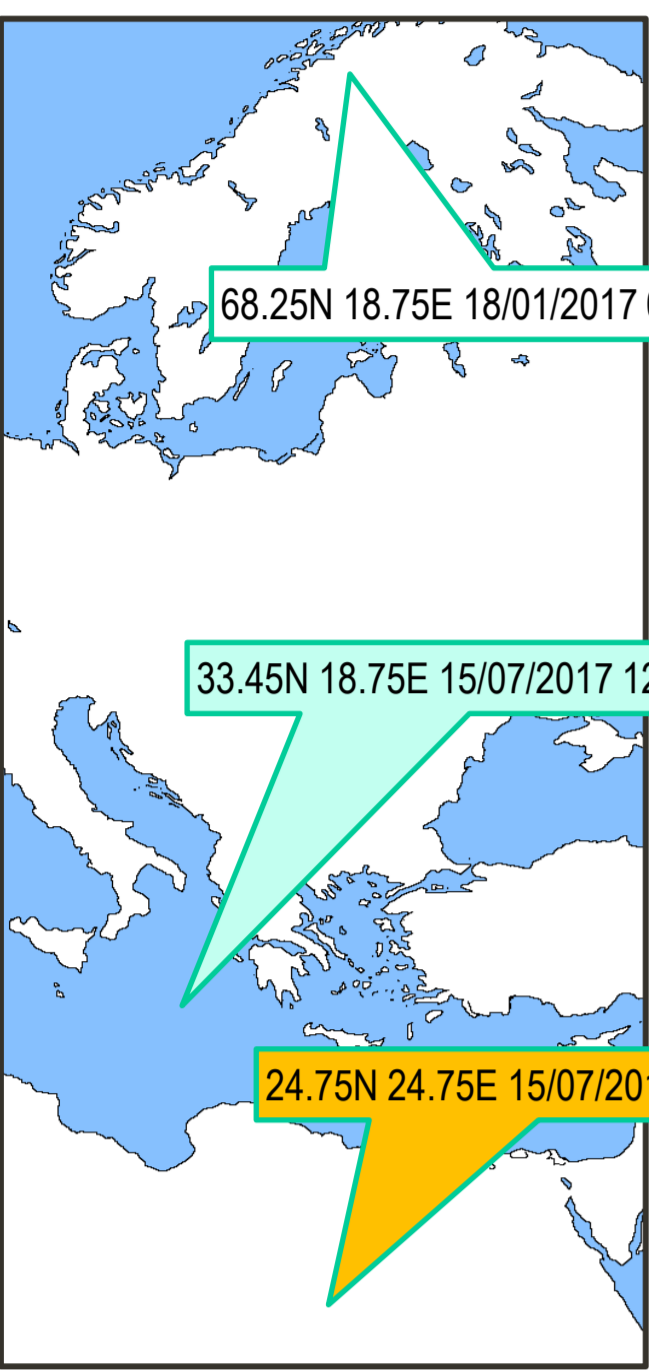
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The FORUM Mission:

FORUM (Far-infrared Outgoing Radiation Understanding and Monitoring) is a Fourier Transform Spectrometer (FTS) that will fly as the 9th ESA's Earth Explorer mission. FORUM will sound the atmosphere in the 100-1600 cm⁻¹ region, covering the Far Infrared (FIR) and part of the Middle Infrared (MIR), accounting for more than 95% of the outgoing longwave flux lost by our planet. The FORUM data will allow a better insight into the following targets:

- Upper Troposphere Lower Stratosphere (UTLS) Water Vapour
- Surface emissivity in polar and dry regions**
- Cirrus cloud characteristics

Joint Retrieval of Tskin, TEM, H2O, Emissivity in Clear Sky: Retrieval Setting



Model:
 EMISSIVITY: Huang database [1]
 TSKIN/TEM/H2O: ERA5 reanalysis [2]
 Other VMR: IG2 database [3]
 Cross Sections: LBLRTM database [4]

Initial guess:
 EMISSIVITY: Model – 0.05
 TSKIN/TEM/H2O: 10-years avg. of ERA5 [5]

A-priori:
 EMISSIVITY: Model – 0.05
 TSKIN: Model, 2K perturbation
 TEM/H2O: Model, perturbed according to a-priori VCM

A-priori error:
 EMISSIVITY: 0.15, no correlations
 TSKIN: 2K
 TEM/H2O: UK MET Office IASI assimilation error

Codes:
 Forward Model: LBLRTM, v12.11 [4]
 Retrieval Code: L2M_I, FORUM E2E inversion module [5]
 Retrieval Algorithm: Gauss-Newton (GN) Optimal Estimation (OE) IVS regularization [6,7]
 Instrument Characteristics/Response Function: FORUM project, phase B1 instrument concept

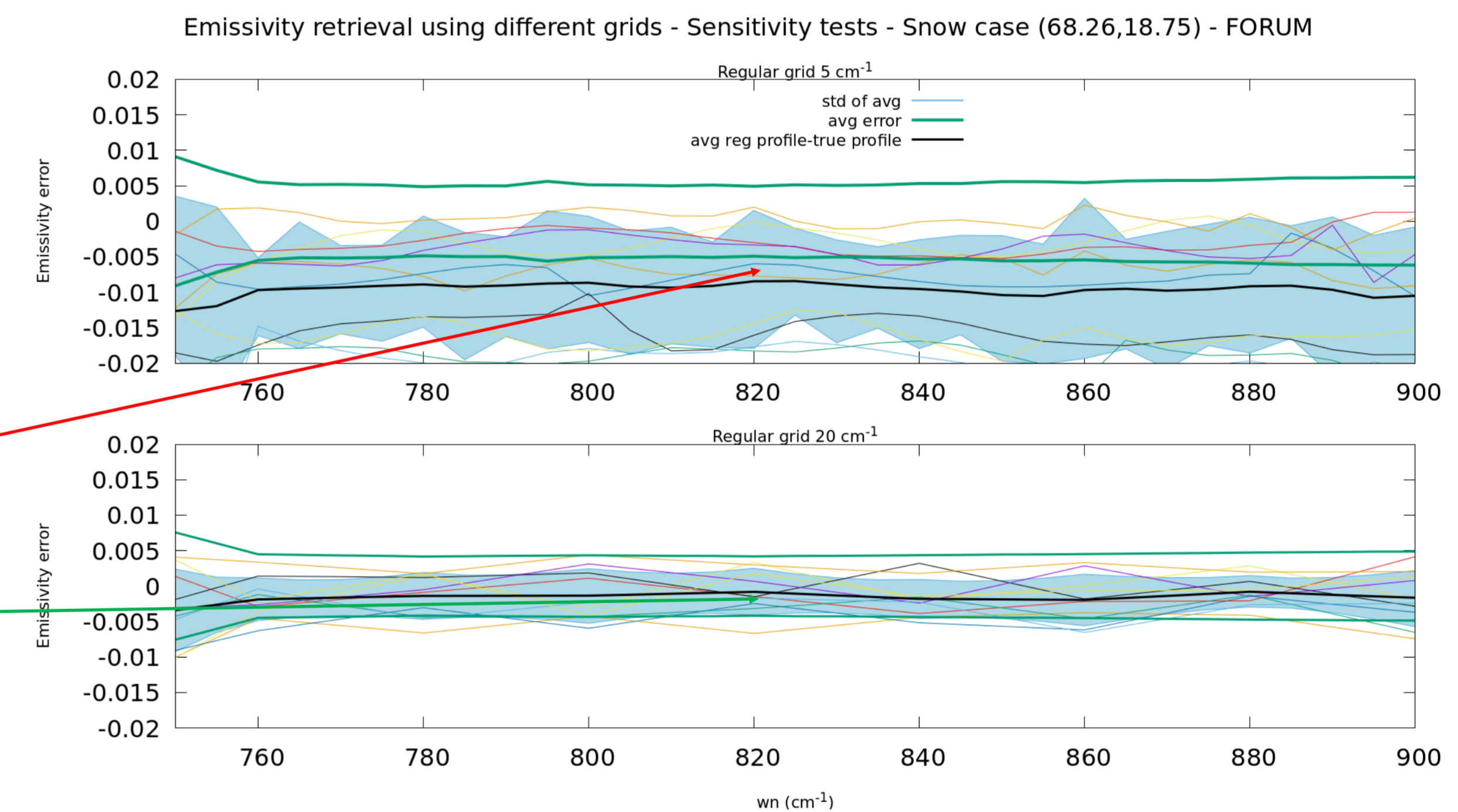
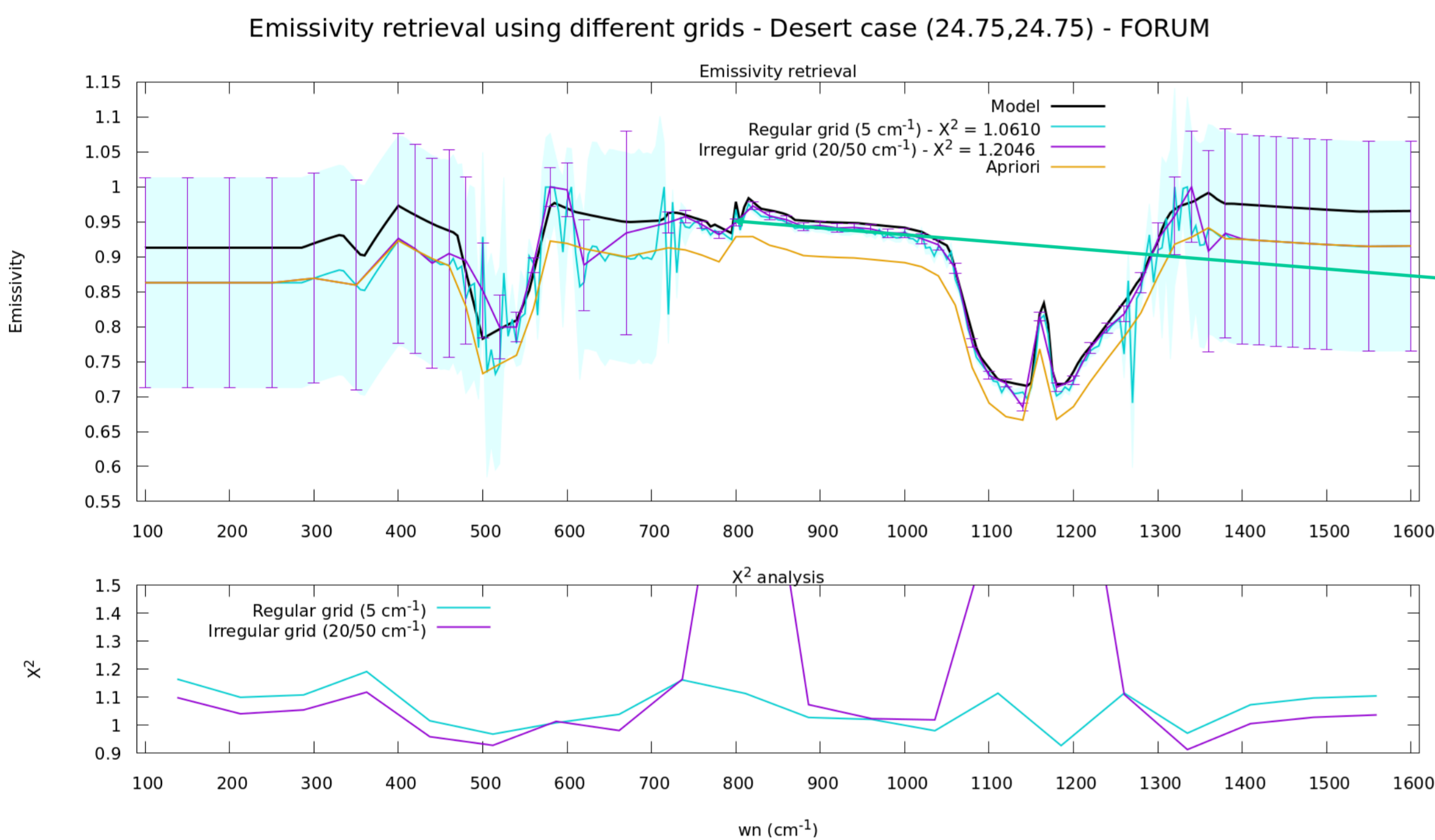
Emissivity grid step: fine vs. coarse

Fine grid (5 cm⁻¹):

- Minimizes smoothing error. The fine grid is able to reproduce sharp features in the emissivity model.
- Reduced precision. The larger random error may produce biases towards the AP. A contributing factor is the negative correlation in the retrieval between surface temperature and emissivity.

Coarse grid (20-50 cm⁻¹):

- May not reproduce sharp features. If the retrieval grid step is larger than the emissivity feature, the feature cannot be reproduced.
- Good precision. Each retrieval point is determined by a large number of measurements. Thus, the random error is smaller and there is no bias in the retrieved emissivity profile.



IVS regularization of emissivity retrieval

Why we need regularization:

- We do not use correlations in the a-priori VCM to avoid cross-talk between spectral ranges with different sensitivity to surface emissivity.
- With this choice, we obtain a better reconstruction in the transition intervals, but there might be oscillations in the retrieved profile, since no constraints are imposed on adjacent emissivity measurements in the a-priori.

IVS (Iterative Variable Strength) regularization:

- Introduced in [6] for ESA MIPAS retrieval and extended [7] to FORUM vertical profile retrievals.
- The optimal estimation x_{OE} and regularized retrieved solution x_{λ} have the form:

$$x_{OE} = x_k + (K_k^T S_y^{-1} K_k + S_a^{-1} + \alpha_k M)^{-1} [K_k^T S_y^{-1} (y - F(x_k)) + S_a^{-1} (x_a - x_k)]$$

$$x_{\lambda} = x_k + (K_k^T S_y^{-1} K_k + S_a^{-1} + \alpha_k M + R_{\lambda})^{-1} [K_k^T S_y^{-1} (y - F(x_k)) + S_a^{-1} (x_a - x_k) - R_{\lambda} x_k]$$

Where: x is the retrieval vector, $F(x)$ is the forward model, y is the measurement vector with S_y VCM, k is the GN iteration index at convergence, x_a is the a-priori with S_a VCM, $K_k = \nabla F(x_k)$, $\alpha_k M$ is the Levenberg-Marquardt term, and finally the regularization term $R_{\lambda} = L_{\lambda}^T \Lambda L_{\lambda}$ is such that L_{λ} is a linear operator

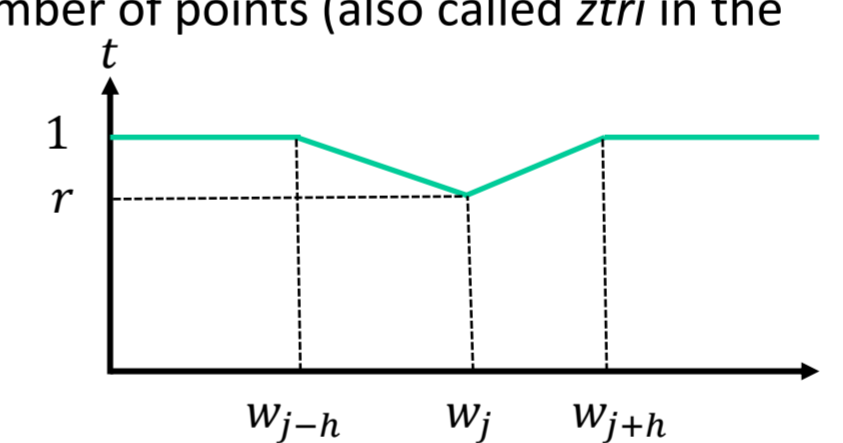
approximating the i -th derivative: $(L_{\lambda} x_k)_j \cong \frac{d^i}{dw^i} x_k(w_j)$, and Λ is a positive diagonal matrix, so that we may think: $\Lambda_{jj} = \lambda(w_j)$.

The IVS method starts with a large $\Lambda_0 = \lambda_0 I$, and decreases the profile until both conditions below are fulfilled:

- The regularized profile are within a fraction w_e of the error bars of the OE solution.
- The vertical resolution (for profiles) or spectral resolution (for emissivity) of the regularized profile is degraded no more than a multiple w_r of the vertical resolution of the OE solution.

Decreasing the lambda profile:

To decrease the $\lambda(w)$ profile, for each point w_j where the conditions are not satisfied, we multiply by a triangular function $t_j(w)$. We fix $r = 0.99$, the amplitude of the decreasing is set either with the independent variable, or in number of points (also called $ztri$ in the plots). For emissivity, sensible choices are: $h = 1$ or $h = 2$.



Retrieval Qualifiers:

- χ^2 : Chi-square statistic of the retrieval.
- DOF: Number of degrees of freedom of the solution.
- POQ: Profile Oscillation Quantifier Ω_1 . Given any profile $x_i = x(z_i)$, measures the oscillations of the profile.

$$\Omega_1 = \frac{1}{n-2} \sum_{i=2}^{n-1} \frac{|x_i - x_{i-1} - \frac{x_{i+1} - x_{i-1}}{z_{i+1} - z_{i-1}} (z_i - z_{i-1})|}{\sqrt{(x_{i+1} - x_{i-1})^2 + (z_{i+1} - z_{i-1})^2}}$$

Three test scenarios

Sensitivity to emissivity in the FIR depends on the Precipitable Water Vapour (PWV) of the atmosphere.

Water:

Control case. Retrieval over sea. Large water vapour atmospheric content. No sensitivity to emissivity in FIR.

Snow:

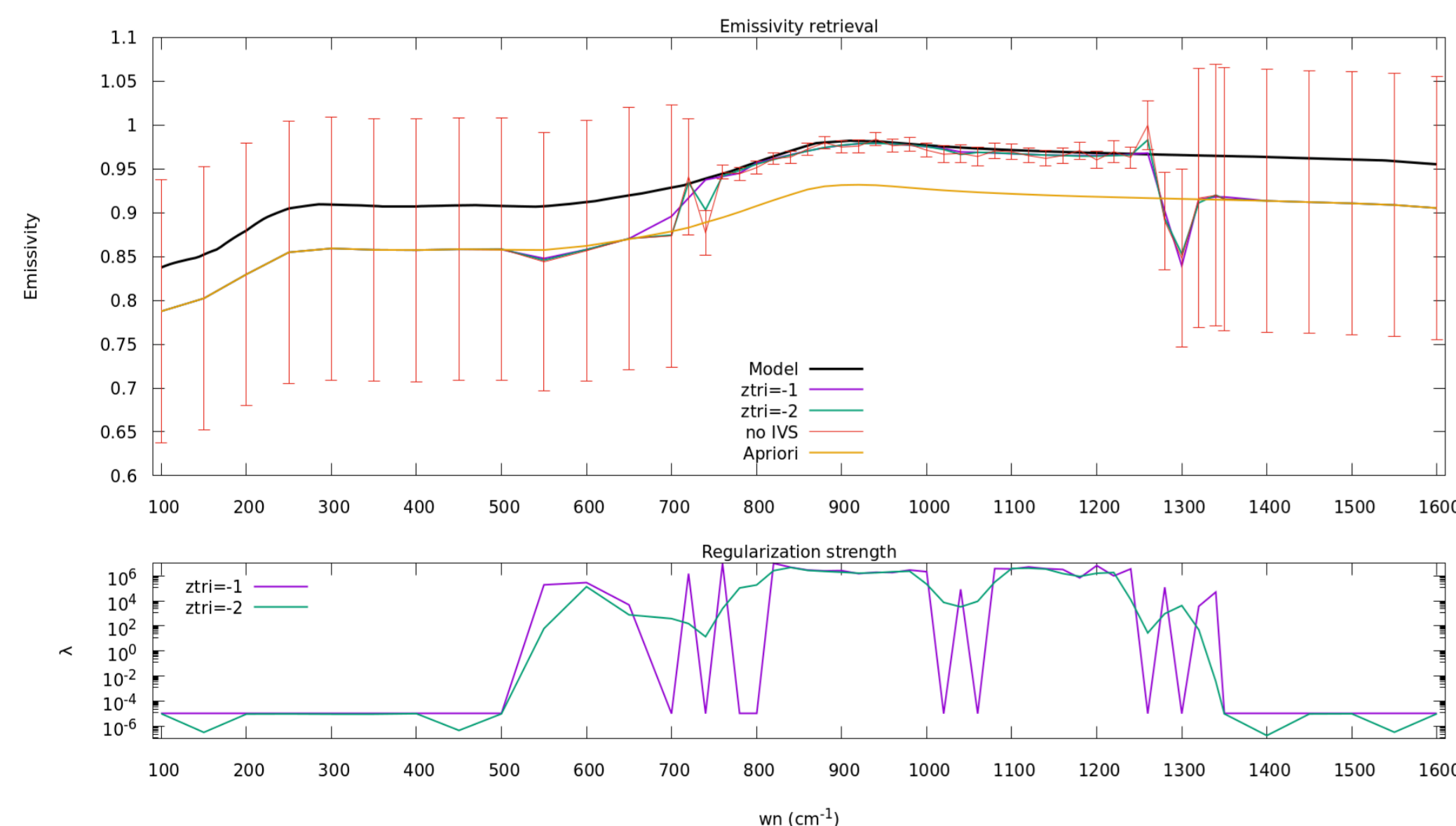
Retrieval over fine snow in winter. Dry atmosphere. Good sensitivity to emissivity in FIR.

Desert:

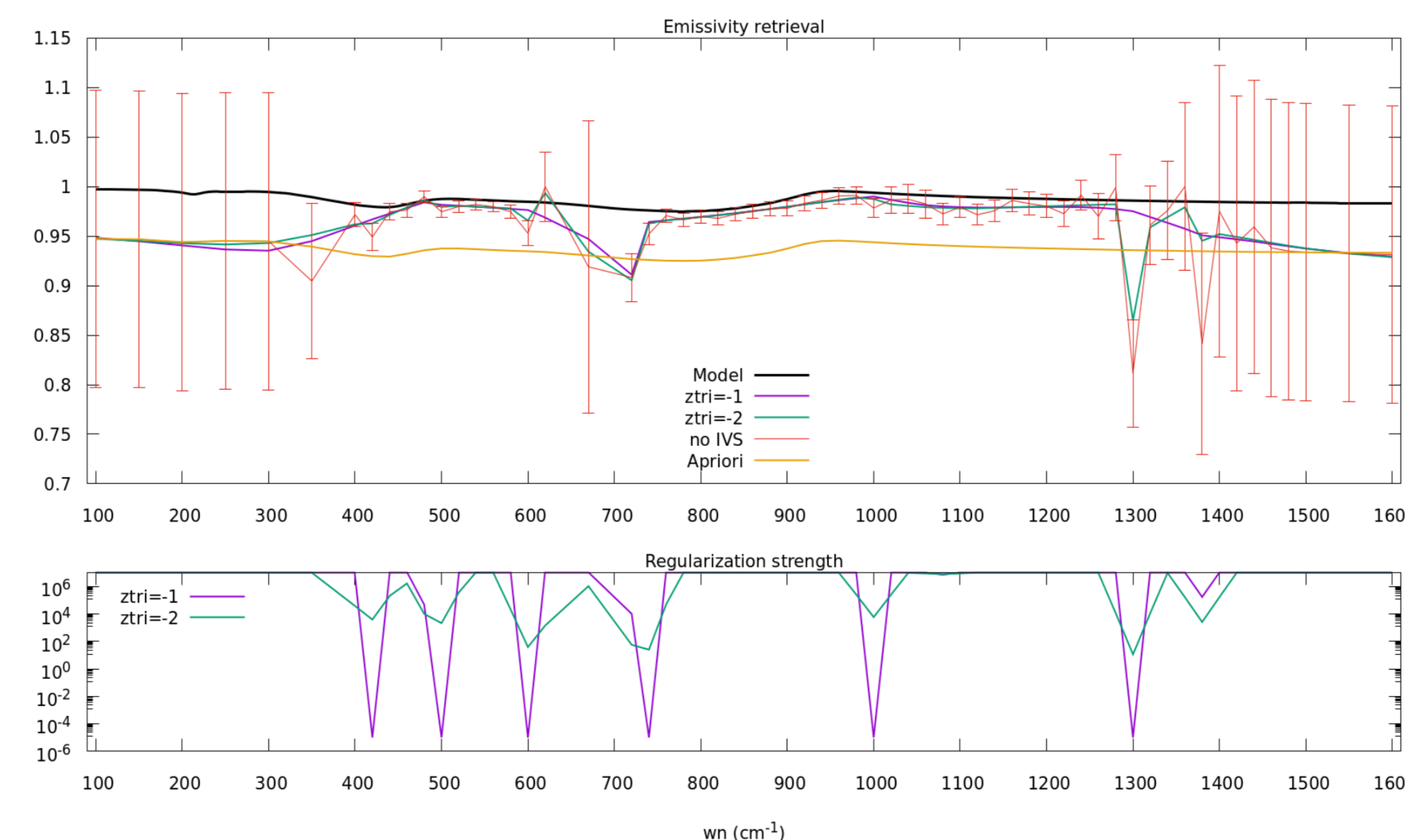
Retrieval over desert in summer. Fairly dry atmosphere. Some sensitivity to emissivity in FIR.

	WATER CASE PWV: 36.33 mm			SNOW CASE PWV: 3.31 mm			DESERT CASE PWV: 23.14 mm		
	BEFORE IVS	AFTER IVS ($\lambda_0 = 10^7, w_e = 1, w_r = 5, h = 1$)	AFTER IVS ($\lambda_0 = 10^7, w_e = 1, w_r = 5, h = 2$)	BEFORE IVS	AFTER IVS ($\lambda_0 = 10^7, w_e = 1, w_r = 5, h = 1$)	AFTER IVS ($\lambda_0 = 10^7, w_e = 1, w_r = 5, h = 2$)	BEFORE IVS	AFTER IVS ($\lambda_0 = 10^7, w_e = 1, w_r = 5, h = 1$)	AFTER IVS ($\lambda_0 = 10^7, w_e = 1, w_r = 5, h = 2$)
DOF	29.167	9.524	11.048	45.343	10.920	14.809	38.403	17.605	19.535
POQ	271E-6	97E-6	165E-6	473E-6	34E-6	166E-6	422E-6	254E-6	283E-6
χ^2	1.0287	1.0365	1.0356	1.0262	1.0376	1.0341	1.2046	1.2506	1.2409

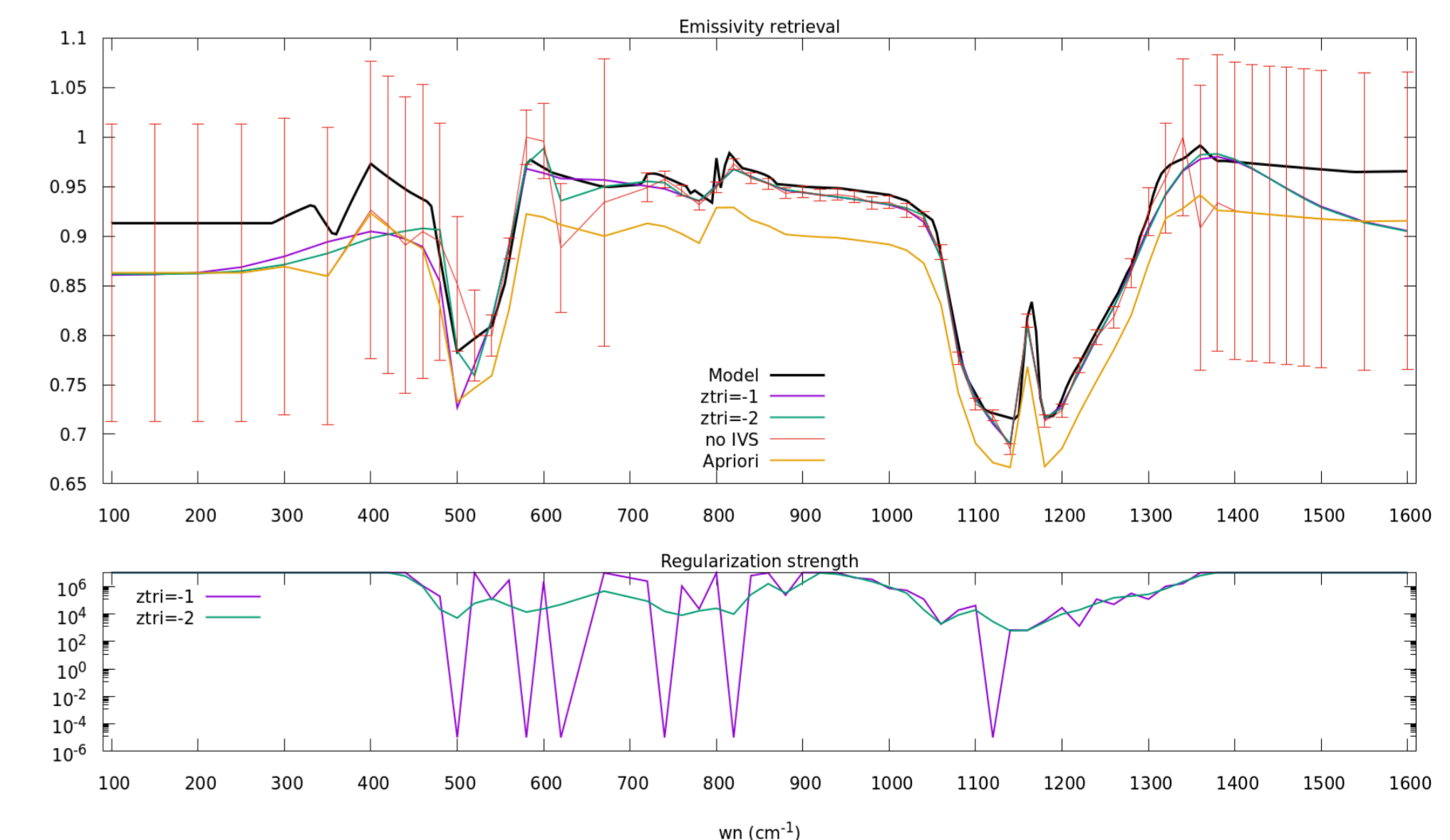
FORUM - Water case (33.75,18.75) - $\lambda_0=10^7 - w_r = 5$



FORUM - Snow case (68.26,18.75) - $\lambda_0=10^7 - w_r = 5$



FORUM - Desert case (24.75,24.75) - $\lambda_0=10^7 - w_r = 5$



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