

Assisted Color Acquisition for 3D Models

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Abstract

Capturing surface appearance precisely is paramount for modeling realistic materials. Nevertheless, the spatially varying nature of most materials is difficult to measure. State-of-the-art methods often rely on complex apparatus and controlled environments, and even if they are able to acquire reliable SVBRDFs, the whole process usually takes a long time and generates a large amount of data, that is often redundant.

In this work we propose a method for fast and assisted acquisition of material properties on-site. The system has a simple setup, requiring only a generic camera and a light source. Consequently, it is also very portable and appropriate for a broad range of object sizes and scenarios. The system guides the acquisition process, allowing for a fast capture session while at the same time producing high-quality per vertex diffuse colors. To help in achieving a complete coverage it suggests missing light directions, reducing the amount of necessary input images and the acquisition time. The system is designed to work *in situ*, therefore the whole acquisition process works with immediate feedback and interactive integration of new data.

We show results for a variety of objects differing in size and materials.

Keywords: Digitization and Image Capture, Reflectance

1. Introduction

The fast improvement of depth cameras and scanning devices allowed for faster geometric acquisition of objects and environments. Nevertheless, the issue of color quality of the objects has been only partially taken into account, and real-time (or near real-time) material acquisition has not received the adequate attention. A method that is robust and efficient enough for *in situ* acquisition, and that, at the same time, can handle a broad variety of materials and geometries, is still a great challenge in the field. In this work, we propose an acquisition method to narrow this gap.

Capturing the material appearance requires extra care with illumination conditions. Unfortunately, state-of-the-art acquisition methods rely on complex setups or impose severe ambient or geometric limitations in order to have a controllable light environment. Additionally, to achieve high quality results, often a massive amount of input data is acquired, and the result can only be properly visualized after a long post-processing step. To aggravate these issues, it is not uncommon during real acquisition sessions to notice only afterward that the input data is incomplete. Since no immediate feedback is usually available, there is no straightforward way to check coverage and completeness before arriving at the end of the process. In certain campaigns this may be a major problem, since another trip to the site may not be viable.

Another issue is the size of the produced dataset itself, that

creates problems for distribution, operation, and storage of the data, specially when the goal is to digitize a collection of objects. Thus, compact and easy-to-use representations are more than desirable in this field.

In this work, we describe a general method for appearance acquisition that works with off-the-shelf equipments, and tackles the aforementioned issues. To use our system it is only necessary a camera, a portable light source, and the 3D geometric model of the object in question. Our assumptions are that the light source is predominant, and that the material is isotropic.

Briefly, the method works as follows. An initial camera position is chosen and calibrated in respect to the object (image to geometry alignment). Then, keeping the camera fixed, photos are acquired while placing the light source at different positions around the object. For each photo, the light direction is estimated and reflectance samples are stored per vertex. After the first few photos the system is able to suggest new light positions in order to achieve a complete coverage of the reflectance function per vertex in an efficient manner. When enough samples have been acquired for a viewpoint, the camera is moved or the object is rotated, recalibrated, and the process is repeated. At any given time it is possible to compute a fast polynomial approximation of the reflectance function per channel for each vertex, allowing for an immediate feedback about the overall acquisition progress. The main contributions and strong points of our method are:



Figure 1: Three datasets with different materials captured with our method.

53 *The appearance acquisition process is simple and requires no*
 54 *special gear or setup.* This is important since many prior meth-
 55 ods are not compatible with *in situ* digitization campaigns (such
 56 as large domes [1]). Methods that can work with off-the-shelf
 57 low cost equipments can also reach a broader audience, espe-
 58 cially in contexts such as Cultural Heritage.

59 *It is able to work with sparse data (only a few samples per ver-*
 60 *tex).* Because the light is manually positioned, minimizing re-
 61 dundancy by acquiring the least amount of photos is important
 62 to reduce acquisition time.

63 *It requires no previous knowledge about the target material.*
 64 Fitting more complex BRDFs usually requires some knowledge
 65 of the target material, and often it is necessary to adjust at least
 66 a few parameters to achieve good results. A more generic, even
 67 though not as accurate, reflectance function that requires no pre-
 68 vious knowledge or parameter setting offers an attractive advan-
 69 tage, specially for non-expert users. Furthermore, many BRDF
 70 models, in particularly those that model specular effects such
 71 as Fresnel, require a large amount of samples, which would go
 72 against our sparse data assumption. Some previous work, such
 73 as Lensch et al. [2] and Palma et al. [3], cluster BRDFs in or-
 74 der to handle this issue, but by doing so, lose the small intrinsic
 75 variations of more complex materials and significantly increase
 76 computational time.

77 *Results are compact and can be visualized with very simple ren-*
 78 *dering shaders.* Apart from a few extra per vertex parameters
 79 to represent the polynomial function per channel, no extra data
 80 is produced (such as textures). Compact representations are im-
 81 portant in order to easily store, disseminate and share 3D mod-
 82 els.

83 *Immediate feedback during acquisition.* Most digitization cam-
 84 paigns are *in situ* and not in a lab environment. Immediate
 85 feedback is a very important feature since it allows the user to
 86 quickly evaluate the acquired data and take action where nec-
 87 essary, for example acquiring photos from a new view point or

88 adding images with new light directions. Methods that rely on
 89 BRDF fitting usually require long processing times. For exam-
 90 ple, Lensch et al. [2] reported times in the scale of hours, while
 91 our polynomial fitting takes at the maximum a few seconds even
 92 for dense meshes.

93
 94 We acquired the appearance of a variety of objects com-
 95 posed of different materials to show the robustness of the method.
 96 We believe the ensemble of the above points are unique and ren-
 97 ders our method very useful for a broad audience of users that
 98 are not experts in appearance modeling and acquisition, that
 99 cannot afford expensive systems, that can greatly benefit from
 100 having immediate feedback of the acquisition process during
 101 the digitization campaign without long post-processing compu-
 102 tations, and that must work in scenarios where the use of large
 103 apparatus may not be possible due to access restrictions.

104 The rest of the paper is organized in the following way. In
 105 Section 2 we present the works that inspired and that are most
 106 related to ours. In Section 3 we explain the required setup and
 107 give a brief overview to illustrate a typical acquisition session
 108 using our approach. Section 4 describes the main points of our
 109 method that allow us to achieve the mentioned contributions:
 110 a per vertex polynomial fit of the reflection function; and a
 111 guided acquisition approach that indicates optimal light posi-
 112 tions to cover as many and as best as possible the vertices. To
 113 illustrate the robustness of our approach, we show and analyze
 114 results for a variety of different materials in Section 5, followed
 115 by some validations. Finally, we discuss the method’s limita-
 116 tions in Section 6 and present our conclusions in Section 7.

117 2. Related work

118 The estimation of SVBRDFs and material properties in gen-
 119 eral became a topic of interest as soon as active acquisition de-
 120 vices (i.e. 3D scanners) started to reach a mature level. A com-
 121 plete overview of the literature in this field goes well beyond the
 122 scope of the paper. We mainly focus on approaches that share
 123 features with our proposed work. Please refer to [4] or [5] for

124 an overview on acquisition and digital modeling of appearance.
125 One of the first generic approaches was proposed by Lensch
126 et al. [6]. They implemented a fitting process of the Lafortune
127 BRDF model using only a professional digital camera, a reflect-
128 ing sphere and a dark room. Instead of having a BRDF model
129 per vertex, they segmented the mesh into clusters of BRDFs.
130 Due to the clusterization, however, some areas may not be well
131 represented. The authors extended the previous work by chang-
132 ing the calibration of the light source position and estimating
133 normal maps in order to refine the geometric details [2]. The
134 approach obtains accurate results, but the specificities of the
135 setup and the amount of input needed make it impractical for a
136 wide use. Therefore, especially for on-site acquisition, several
137 efforts toward more applicable solutions have been made.

138 **Simplifying the description.** A first direction of research was
139 the creation of simplified models to represent materials. Among
140 them, the work of Malzbender et al. [7] allows for a much sim-
141 pler and faster acquisition procedure. It fits a Polynomial Tex-
142 ture Map (PTM) by solving a linear system for N given im-
143 ages using singular value decomposition. They also show that
144 it is possible to apply filter behaviors on the PTM and some
145 lighting models such as anisotropic surfaces and Fresnel effects.
146 Nevertheless, this approach was intended to acquire data from
147 a single point of view in order to produce texture maps that
148 can change their appearance with respect to the light direction.
149 In a similar fashion, Goldman et al. [8] propose an approach
150 based on photometric stereo to recover at the same time ge-
151 ometry and spatially-varying BRDFs using the isotropic Ward
152 shading model. In the same line, the work of Alldrin et al. [9]
153 acquires shape and BRDF simultaneously. The material is ob-
154 tained from a bi-variate approximation of measured isotropic
155 BRDFs, and the authors argue that it can represent a broader
156 number of materials. These methods do achieve good results
157 but rely on a very accurate acquisition, and are not trivially ex-
158 tensible to larger objects.

159 **Controlling the acquisition.** Another possible direction of work
160 is to build ad-hoc devices to automatically acquire the massive
161 amount of data needed for appearance properties estimation.
162 Holroyd et al. [10] designed a complex coaxial optical scanner
163 capable of synchronously acquiring shape and spatially varying
164 reflectance using the Cook-Torrance model. Their device con-
165 sists of a pair of assemblies, each containing a coaxial camera
166 and a light source. Schwartz et al. [1] created a dome con-
167 sisting of 151 DSLR cameras taking HDR sequences and one
168 LED-Projector mounted on a tripod placed at five to eight dif-
169 ferent positions, projecting 38 different patterns. Instead of fit-
170 ting BRDFs, it produces a *Bidirectional Texture Function* for
171 the mesh. With a similar setup, the dome proposed by Nöll
172 and colleagues [11] is also able to acquire the bottom side of
173 objects since they are posed on a transparent surface. CultLab
174 3D [12] proposes an automatic modular digitization pipeline,
175 which is able to acquire geometry and appearance at the same
176 time. All the devices above present limitations due to their re-
177 stricted portability and, more importantly, to the size of the ob-
178 ject that they are able to handle (not more than a few tens cm).

179 **Simplifying the acquisition.** Given these limitation, research
180 efforts have been placed in the direction of limiting the com-

181 plexity of the acquisition setup and the amount of input data
182 needed. Material properties can be inferred even from a sin-
183 gle image, trying to classify the properties of types of mate-
184 rials [13], or by analyzing a single image with known geom-
185 etry [14], but are limited to a single BRDF. Focusing on the
186 acquisition of real objects, some recent works propose the ac-
187 quisition of the SVBRDF of real object with very simple pro-
188 cedures, requiring only the light of mobile devices [15, 16] or
189 even the screen of a laptop [17]. While they obtain very inter-
190 esting results, these methods are limited to smaller and nearly
191 planar objects.

192 The acquisition of larger and more demanding objects usually
193 imply in slightly more complex acquisition setup and data. Palma
194 et al. [3] propose a statistical method for estimating Spatially
195 Varying BRDFs. The approach is based on video sequences
196 with fixed but general lighting conditions. A user assisted clus-
197 tering process is also performed, since in the video some re-
198 gions may not have been appropriately specularly sampled. Some
199 limitations are presented in this work due to the input data and
200 the employed Phong model, and it may also present blur effects
201 in some cases. In addition, the clustering step may sometimes
202 require a significant amount of manual intervention. The work
203 presented by Dong et al. [18] also tackles the unknown lighting
204 conditions using a video, but in this case the object is rotated
205 around its axis. As BRDF model they chose the isotropic mi-
206 crofacet model. The greatest limitation of their work is that
207 it only handles convex geometry, and thus is not applicable to
208 most real objects.

209 Ren et al. [19] proposed a portable acquisition setup that in-
210 cludes a BRDF chart to recover the object materials in a similar
211 fashion as with color charts. Treuille et al. [20] extended the
212 idea by using references of known BRDFs to reconstruct the
213 object using multi-view stereo. These two methods depend and
214 are limited, however, on the amount and quality of the reference
215 BRDFs used.

216 Recently Wu et al. [21] presented AppFusion, an interactive
217 material acquisition system that uses the Kinect to estimate the
218 lighting environment and the material of the target object. The
219 system also takes advantage of the infrared data provided by the
220 Kinect device. While our proposed method follows a similar di-
221 rection by aiming at a fast acquisition system with immediate
222 feedback, AppFusion is unfortunately limited by the quality of
223 the acquired data by the Kinect (especially the image resolu-
224 tion). The results shown are on small objects, composed by a
225 single material.

226 **Reducing the amount of input.** A last and final interesting di-
227 rection of research is to reduce the amount of input data needed
228 to fit existing material models. The work by Ruiters et al. [22]
229 proposes an initial effort to deal with SVBRDFs, but requires
230 a very long processing time. In a more recent work, Nielsen et
231 al. [23] analyze several examples of BRDFs and show that most
232 of them can be acquired starting from a small number of sam-
233 ples (from five to twenty). This is a promising result, but has
234 yet to be extended to the SVBRDF case. Our proposed work
235 goes in the direction of acquiring an accurate material repre-
236 sentation by minimizing the number of acquired samples. We
237 also employ a more general model, instead of choosing a sin-

238 gle BRDF as done by many of the related works. To the best
239 of our knowledge, there is no other system that is as general as
240 ours, i.e., does not impose severe restrictions to object’s size,
241 location and shape, and does not make assumptions about the
242 material. In addition we provide immediate feedback that aids
243 in reducing the acquisition time and avoids redundant data.

244

245 3. System setup and example of usage

246 The system setup, shown in Figure 2 is quite simple, and
247 similar to the one used for the acquisition of RTI images. The
248 camera is fixed, preferably using a tripod, in front of the ob-
249 ject and the reflecting sphere. Regarding the illumination, the
250 assumption is that the light must be ”directional” (same light di-
251 rection for the whole object). To better approximate this effect,
252 the light source used must cover a significant larger volume than
253 the one occupied by the object.

254 Once the setup is ready, calibration is performed using a single
255 image, in two steps. First, since the light direction has to be
256 estimated, the position of the reflecting sphere is automatically
257 extracted from the image, using the standard method from RTI
258 acquisition [24]. Then, the image is aligned to the 3D model
259 by estimating the camera parameters using Corsini et al. [25]
260 Mutual Information method. The amount of user interaction
261 is limited to an initial rough alignment of the model, and usu-
262 ally does not require more than a few seconds. Optionally, a
263 color chart can also be used for color calibration. Even though
264 it is not mandatory, it may help to improve the final result and
265 achieve more natural and faithful colors. The color chart pro-
266 cess consists merely in detecting the squares with respective
267 colors in the image, and applying a linear regression for each
268 color channel to calibrate the photos.

269 Once the image is aligned with the 3D model, and the sphere
270 has been identified, a set of photos is acquired by displacing the
271 light source. For each photo, the light direction is automatically
272 detected, and the pixel colors are directly mapped onto the 3D
273 vertices.



Figure 2: An illustration of the system setup, containing the camera, a light source, a reflective sphere and the object.

274 After the first few photos have been acquired, the system
275 is able to suggest new light directions to optimize the process.
276 Figure 3 illustrates some steps of the acquisition process, and
277 how the suggested lights improve the fitting after each new
278 photo. Note that a vertex may be well represented from one

279 light direction, but lacks samples from other angular ranges.
280 For example, the second row in Figure 3 shows an improvement
281 on the lions breast using an approximately frontal light direc-
282 tion. However, the same vertices appear with arbitrary colors
283 (due to lack of samples) when illuminated from the side, so a
284 new light is suggested to better cover these angles, as shown in
285 the last row of the figure.

286 New photos are acquired using the suggested light direc-
287 tions, until a good coverage is achieved. This is mainly evalu-
288 ated visually by the user after fitting the polynomials. Never-
289 theless, this evaluation is straightforward since poorly sampled
290 vertices are rendered with arbitrary colors and can be easily
291 spotted, as shown on the top rows of Figure 3. At this point,
292 a new viewpoint is manually chosen by displacing the object
293 or the camera, and the process is restarted taking into account
294 the data acquired from the precedent view directions. Conse-
295 quently, a lower number of light directions is usually needed to
296 cover the new view point.

297 4. Method

298 Our approach aims at guaranteeing that at least the mini-
299 mum amount of information per vertex has been acquired in
300 order to reproduce its diffuse color and an approximate specu-
301 lar component for each color channel. Note that our goal is not
302 to have a minimum number of samples per vertex but a good
303 angular coverage for each one.

304 For each vertex we store all projected pixels from the acquired
305 photos. Other than the pixel intensity per color channel, we also
306 store the product $(R \cdot E)$ for each pixel sample, that is, the dot
307 product between the reflected light direction, and the eye vec-
308 tor. Even though we only use the product $(R \cdot E)$, it implicitly
309 contains information about the normal N and the light direction
310 L .

311 The next sections explain the model fitting, the mechanism
312 to suggest new light directions, and the neighbor expansion to
313 assign a material model to vertices that lack enough samples.

314 4.1. Model fitting

315 We chose a very simple, yet efficient, model: a cubic poly-
316 nomial for each color channel. This generates 12 parameters
317 per vertex, i.e., 4 coefficients for each channel. See Figure 4 for
318 some exemplary fitted curves.

319 The motivation for the cubic polynomial comes from our
320 established goals of visualizing objects during digitization cam-
321 paigns. Sometimes acquisition time may be short, and conse-
322 quently there may be a low amount of data available. For that
323 reason, we need a material appearance model that can be ob-
324 tained efficiently, does not require previous knowledge about
325 the reflectance function and does not need an initial solution.
326 More traditional BRDF models could be used, but they usually
327 require dense sampling and a nonlinear optimization, which
328 falls on the pit of a good initial solution and slower execution
329 times. Our fitting, on the other hand, takes only a few seconds
330 using our GPU implementation even for meshes on the order
331 of a million vertices. Since polynomials are good models for

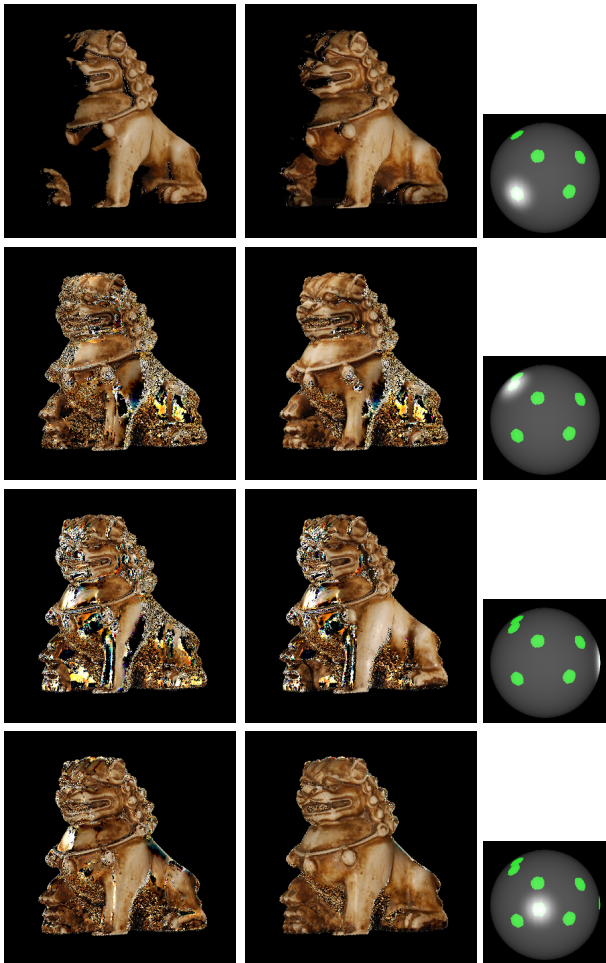


Figure 3: Top row: two input images projected directly onto the model before fitting the reflectance function. Bottom three rows: fitting the data before (left) and after (middle) a new photo is acquired from the suggested angle. Note how for each step the coverage improves significantly. Vertices with arbitrary colors do not yet have enough data, so their polynomial curve is unable to approximate the function well. The light direction is depicted on the right column, where the top row shows the five manually chosen light directions, and the bottom rows show the first three suggested light direction. The white spot is the current direction, the green spots are previously acquired directions.

low-frequency data [26], it suits our goal to guarantee a good diffuse color. As aforementioned, we are, however, restricted to isotropic materials.

An important point is that we do not divide our function into two components, such as diffuse and specular. Typically, a straightforward approach would be to plot each sample's intensity against two different products: $(L \cdot N)$ for the diffuse part and $(R \cdot E)$ for the specular part. However, as also noticed by Palma [3], specular information is particularly difficult to acquire. Only a small amount of photos cover a vertex in a specular manner since this behavior is usually concentrated around a small angular range. Fitting any interesting function with very scarce data is troublesome. Another option is to acquire more data until enough specular samples per vertex is obtained, but this would go against one of our main goals, which is to avoid an acquisition process that is excessively long. Thus, we treat all our input data equally, and try to make the most out of it in

our fitting process.

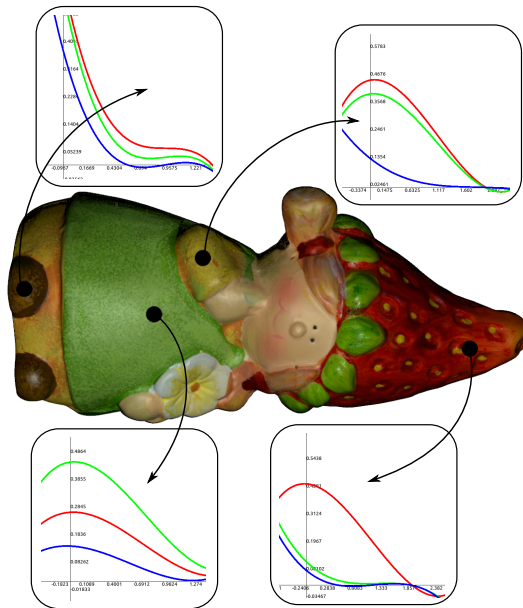


Figure 4: Exemplary fitted cubic polynomials from four different vertices of the Nana dataset. The vertical axis shows intensity, and the horizontal axis the product $(R \cdot E)$.

The fitting procedure is based on a simple Least-Squares polynomial fit [27], and can be applied at any time during the acquisition process, but usually at least five photos are needed to achieve any meaningful result. This can be very useful in understanding the amount and quality of coverage at any given moment during the acquisition session. If more data is needed, more photos can be acquired accordingly.

4.2. Suggesting new light directions

We try to reach the right balance between the amount of data gathered and the quality of the results. Hence, after acquiring the first few photos, the system suggests new light directions in order to optimize the vertex coverage. This initial number of photos is arbitrary, in the sense that during the acquisition process one can ask for a suggestion whenever needed. But in our tests we found that only around 3-5 initial photos are necessary. Furthermore, one can choose to mix the suggestions with a self-guided acquisition procedure in some cases.

4.2.1. Vertex coverage

To compute a vertex's coverage, we look at the distribution of its acquired samples, and analyze angular regions that are sub-sampled. As we do not know beforehand the true distribution of the function, we aim at sampling the domain as uniformly as possible. Thus, vertices with good coverage should have small maximum distance between two samples.

Note also that for each light direction, we check if the vertex is visible from the light source and discard samples that are in shadows.

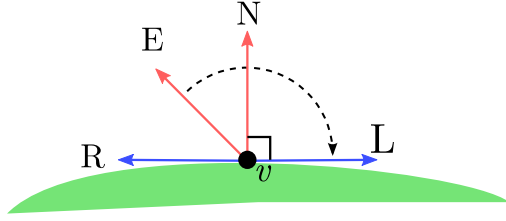


Figure 5: The maximum possible angle between L and E happens when R and N are perpendicular.

4.2.2. Optimal light direction

To suggest a new light direction, vertices cast weighted votes on their preferred direction according to their current coverage. For each vertex, we search for the largest interval between two samples. First the samples are ordered by the value $(R \cdot E)$. We further include the two extremes $angle_{min} = 0$ and $angle_{max}$ as anchor points. $angle_{max}$ is the maximum angle between a possible light vector and the eye vector while still being visible from the light source: $\angle EN + \pi/4$, as illustrated in Figure 5.

Once the samples are ordered, we define the optimal angle α of the vertex as the medium point of the largest gap, i.e., where it most lacks samples. This process is depicted in Figure 6. Finally, to compute the actual light direction that would generate a sample at that position, the eye vector is rotated by α , and reflected back about the normal, as illustrated in Figure 7. The vertex votes on this direction with weight equal to half the length of this largest interval.

After all vertices have voted, we proceed to select the best global direction. The directions are clustered using regular angular bins. For our tests we used 36^2 bins. For each bin the weights of its contributing directions are accumulated. For the ten bins with highest total weights, we analyze their contribution to all visible vertices in the following manner. For each bin the average of the contributing light directions is used as its representative direction. The scene is rendered from the ten representative directions, and for each one, we sum the contribution of all visible vertices. Each vertex contribution is the distance from the product $(R \cdot E)$ using the representative direction, and the closest stored sample so far, as illustrated in Figure 8. Finally, the bin with the highest contribution is the suggested next optimal light direction.

4.3. Sample propagation

The coverage of the whole surface of a real object may be a difficult task, since it may be hard to frame all the portions of the surface due to self occlusions. Moreover, for some cases, it may not be possible to obtain light directions to cover the whole hemisphere around the object. Therefore, based on the assumption that the material properties are locally coherent, samples are shared between neighboring vertices in order to improve the coverage of those that lack samples.

Given a vertex, we use two metrics to spread the information around neighbors: ratio of covered photos, i.e., how many photos from the total set cover this vertex, and the standard deviation of the vertex's samples. The motivation for the first metric is very straightforward, if a vertex is covered by a small

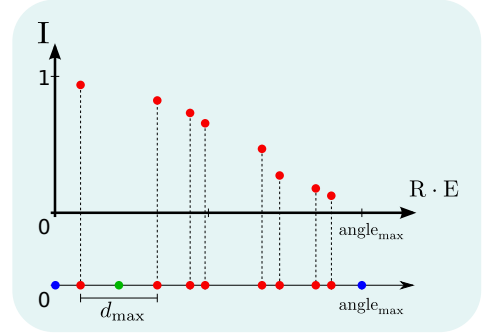


Figure 6: For each vertex we search for the largest interval between its acquired samples (red points). The green point represents the desired new optimal angle between R and E for this vertex. The blue points are anchor samples to create the first and last interval. The vertex weight to the containing bin is $d_{max}/2$.

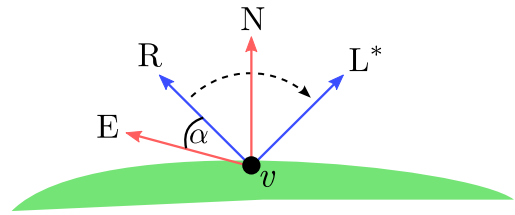


Figure 7: Once we find the candidate angle α for a vertex, we reflect back the R vector to get the corresponding optimal light direction L^* .

number of photos it requires more samples in order to achieve a good reflectance approximation. The second metric comes from the fact that, since we have no previous knowledge about the function, our best guess is to aim for a uniform distribution on the angle domain. Sparse sampling usually has a high standard deviation, therefore, we try to increase the standard deviation of each vertex with low ratio.

To propagate the samples to neighbors that lack information, the following steps are performed: for each photo that does not cover a vertex, we check if one or more neighbors are covered. If so, we choose the neighbor that most increases the standard deviation. The process is repeated until all vertices have been covered or convergence is achieved. We restrict the propagation to neighbors that have similar normals. In our tests we used a threshold of 30° for the angle between normals, and 0.5 for the ratio metric. Figure 9 illustrates the result of the described propagation procedure.

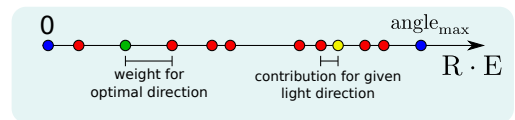


Figure 8: The sampling distribution of a given vertex. The vertex's optimal angle is depicted as the green point, which also defines its weighted contribution to the bin it falls into. The yellow point represents another bin's representative light direction, and in this case it will only add a small contribution to this vertex, since it already has a sample close to this direction.



Figure 9: The Pulcinella before (left) and after (right) the neighbor sample propagation process. Note how difficult to reach vertices inside the cloth folds had their coverage significantly improved.

5. Results and Discussions

We tested our approach on a variety of objects composed of different materials. In this section, we present our rendering system to illustrate the results, and briefly describe and comment each test case. We also provide some visual error validation method, and a limited comparison with existing methods, since only a few made their data available upon request.

5.1. Rendering

The resulting datasets were stored in the Stanford PLY format with normal and polynomial coefficients per vertex. No extra texture or color information is necessary. In comparison to a dataset with RGB diffuse and specular coefficients, plus a shininess exponent, that typically stores 6 extra floats per vertex, we store 12 extra floats but achieve a much more precise and general approximation of the reflectance function. Moreover, during our initial experiments, we noted (as expected) that fitting the Phong model using cosine functions generated an unsatisfactory fit for most datasets, specially regarding the specular component.

The figures in this paper were produced using a simple custom real-time viewer using OpenGL and GLSL shaders. Given light and view directions, for each vertex the product $(R \cdot E)$ is computed and the resulting value is used as the parameter for the three cubic polynomials. A simple shadow mapping algorithm was also incorporated only to convey a little more depth information, but apart from this, no extra effects were employed, i.e., no extra material description, global or local illumination effects, or shading functions. The wooden table that serves as a placeholder for the objects was digitized and its reflectance information was also acquired using our method. Note that we rescaled the table to better fit under each dataset, so it does not serve as a size comparison between the objects. The accompanying video was produced exclusively with this simple renderer.

5.2. Results

The geometry of the test models were acquired using different laser scanners. We also used different cameras during

our tests, such as a Nikon D80 and a D5200. Simple and inexpensive spotlights were used to simulate the directional light. During an acquisition session the camera remains connected to a laptop, so the acquired photos are directly passed to our system and immediate feedback is provided. Apart from the reflection sphere and the color chart, no other extra apparatus was required.

During our tests we have simulated in the best way possible a common acquisition session, that is, we have acquired each dataset within a reasonable time, without aiming at a perfect vertex coverage, but at achieving a good trade-off between acquisition time, acquired data, and resulting dataset. Note that we could take an arbitrary large number of photos to achieve a near perfect acquisition for each model, but this would go against our main goals, as previously described. It would also mask our limitations that are discussed in the next section. As can be noted in the accompanying video some datasets have small holes or missing data in some regions, either due to lack of pixel samples or due to holes in the geometry. This may cause color artifacts or flickering in some cases, specially when the light hits the surface at grazing angles. These artifacts could actually be removed with some post-processing, but would show results that were not achieved solely during the online acquisition method, so we decided to leave them for a more fair illustration of the method capabilities and limitations.

Our method runs mostly in GPU with OpenGL shaders. Consequently, it has restrictions regarding the use of memory and processing time, especially in order to avoid GPU timeouts. Therefore, we try to balance the model size and the number of photos to avoid running into any hardware limitation. For the denser models, our limit was around 130 photos. Nevertheless, it did not severely impact the results.

Buddha. The Buddha is a small plastic statue composed of a highly specular golden paint representing the skin, and a less shiny, but still moderately specular surface composing its robe. The robe is painted in a dark red color, but there are a few physical painting artifacts, suggesting that it was actually hand painted. The hair is composed of a mostly dark diffuse surface with some golden spots. This is a particularly challenging scenario for appearance acquisition methods due to the highly specular materials. A few vertices were not sufficiently sampled, such as near the chin and its left foot. At these locations some artifacts can be noted, specially at grazing angles. Figure 10 shows some exemplary renders of the Buddha dataset.

Even though the golden painting is a rather hard material due to its intense shininess, our model was able to reliably replicate the location and general shape of the specular highlight. There is, however, a difference in specular intensity mainly due to the lack of highlight samples compared to diffuse ones, and due to the color saturation on the photos.

Book. Hardcover books usually have highly specular surfaces, as is the case with the dataset analyzed here. Furthermore, due to its predominantly flat geometry, aligning the model precisely is very challenging. In fact, due to some misalignments it is possible to note some degree of blurring in the results. On



Figure 10: Two renders of the Buddha plastic statue, painted with a challenging reflective material. Note that the red stain on its shoulder is present on the real object.

551 achieve a good approximation of the surfaces reflection func-
552 tion. Figure 12 illustrates the resulting dataset.

553 *Thai Lion*. This small souvenir Thai statue is made of some
554 kind of composite material. Apart for some unreached vertices,
555 specially between the front legs, the surface appearance was
556 well captured (Figure 13).

557 *Nana*. The Nana is a small statue composed of a very specu-
558 lar head and a more predominantly diffuse body. Furthermore,
559 groups of similar colors, such as the green belly, present high
560 local color variation, *i.e.*, many close points reflect different
561 shades of green, which renders our per-vertex approach specifi-
562 cally appropriate. The result can be seen in Figure 12.

563 In order to demonstrate the efficiency of our light suggestion
564 algorithm, we did not acquire this dataset using our method,
565 but used a dataset fabricated with a mini-dome, containing 114
566 light directions from a fixed view direction. We let our system
567 automatically pick 40 photos from this set to produce the poly-
568 nomial per-vertex fitting. For each suggested light direction the
569 method selected the photo with closest light direction. We also
570 produced a result with the full dataset. Figure 14 shows that our
571 algorithm is able to faithfully capture the appearance using only
572 approximately one third of the whole mini-dome dataset. We
573 expect this disparity to increase even more if more viewpoints
574 were available, as our method would profit from the sequential
575 information.

576 *Bas relief*. To further show the versatility of our method, we
577 also demonstrate how it behaves when dealing with data from a
578 Reflectance Transformation Imaging (RTI) acquisition, plus the
579 geometric model. This wall panel has dimensions 80x50cm,
580 and is a typical case where RTI works well, since it is pre-
581 dominantly flat. We show how our method enhances the RTI
582 paradigm by producing real 3D data. A rendering of the panel
583 can be seen in Figure 12.

584 In Table 1 we list a few more details about each dataset,
585 such as number of photos and views. The timing in the fourth
586 column is relative to the last performed fitting, that is, with all
587 acquired photos. Note that the first fitting procedures usually
588 take much less time.

589 We did not time precisely the whole acquisition session,
590 since it depends on the experience of the user and the time spent
591 on making decision about the coverage, among other factors.
592 For the largest datasets, such as the Thai Lion, it took around
593 one hour. Datasets with less view points and photos took con-
594 siderably lower times. Note however, that most of the time is
595 spent moving the light source around and calibrating new view-
596 points.

597 5.3. Validation

598 One way to verify the quality of the reflectance approxima-
599 tion is by not using some acquired photos, and comparing the
600 result against these control group. Figures 15 and 16 show this
601 analysis with a color-coded difference between the photo and
602 the render, where the scale goes from light green (low error) to
603 red (high error). As it can be observed, most of the surface is

531 the positive side, it shows that the fitting is somewhat robust
532 to small misalignments. Renders are shown in Figure 11.



Figure 11: A book cover made from a highly reflective material. Even with noticeable geometry-image misalignments responsible for ghosting artifacts, the reflectance functions are well approximated.

533 *Cloth*. Cloth is a challenging material to acquire properly. This
534 small statue is basically made from cloth with small red stones
535 attached, a black rigid mask and a dark wooden base. The main
536 problem was covering small holes due to the cloth folds. Align-
537 ment with non-rigid objects is also challenging for obvious rea-
538 sons. The scanners were not able to generate a very precise
539 geometry for this case, aggravating the problem. An illustra-
540 tive render is shown in Figure 12. Albeit these challenges, we
541 were able to produce a very compelling appearance model for
542 the Pulcinella statue. In this case, the information propagation
543 was crucial to cover vertices that are hidden from most combi-
544 nations of view and light directions.

545 *Vase*. This vase has a simple geometry with some carved motif.
546 The challenging part however, is the coat of specular paint, that
547 is an issue for many color acquisition methods. An illustrative
548 rendering can be seen in Figure 12.

549 *Boomerang*. The boomerang is a very simple object, basically
550 a painted flat wood surface. Only a few photos are necessary to



Figure 12: From left to right: the Pulcinella miniature offers two significant challenges, the dark mask and the cloth, that is particularly difficult to cover entirely (note that the small black holes are due to missing geometry); a terracotta vase with a coat of shiny paint that makes it specifically challenging; a painted wood boomerang acquired with a reduced number of photos; the small Nana statue composed of different surface appearances; and a marble wall panel, produced from an originally RTI dataset.



Figure 13: The Thai lion statue from two view points.

Object	# photos	# views	time(s)	# vertices
Buddha	110	6	25.91	1.440M
Thai Lion	120	12	12.08	386K
Vase	114	6	11.19	758K
Nana	114	1	9.30	1M
Book	47	4	4.46	1M
Boomerang	22	2	1.58	442K
Cloth	50	3	2.27	789K
Bas relief	105	1	2.85	400k

Table 1: Description of the acquired data. The fourth column refers to the fitting time for all views combined.

604 well represented. Higher error can be noticed mainly on high-
 605 light regions, as expected, and near shadows, though this can be
 606 due to inconsistencies in the shadow map, since our light model
 607 is very approximative.

608 The low error on the diffuse color support our claim that we
 609 can reproduce a good base color with a reasonable specular
 610 approximation. This is expected since polynomials are good
 611 models for low-frequency data, such as diffuse color and some
 612 wide specular lobes. Note that since our method consists of a
 613 model per vertex, even with high-frequency materials, such as
 614 the golden painting, our system can approximately replicate the



Figure 14: The result with 40 photos (left) and 114 photos (middle) from the Nana dataset. The color difference image (right) confirms that our light suggestion approach efficiently produced practically the same result as with a more dense uniform distribution of the light directions.

615 specular shape on the object, but not the intensity.

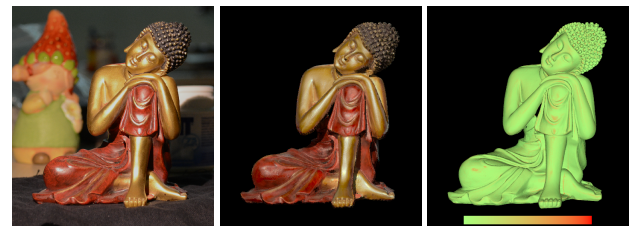


Figure 15: From left to right: original image, render, color-coded difference between the image and the render. We can notice how in general the error is very low, except on some highlight regions and near shadows. The color scale for the error is depicted below the image, where red represents a high error, and light green a low error.

616 We also provide a visual comparison with Palma’s method [3].
 617 Figure 17 shows a render from both methods and a real image
 618 at approximately the same position. As it is noticeable, our
 619 method better approximates the real image, since it is able to fit
 620 a per-vertex function independently, while Palma’s method re-
 621 lies on clustering and thus tends to blur the result. Their method
 622 also uses the Phong model to approximate the BRDF, which in
 623 many cases does not fit well to the real data.

624 We have also used an available dataset acquired with the



Figure 16: The same pattern of error can be noted on the vase. In general the error is very low, except at the center of some highlight regions.



Figure 17: A comparison between our method (left), the real photo (middle), and Palma's method, at approximately the same camera and light configuration.

625 Bonn Dome [1] to further evaluate our method. Since it is very
 626 densely sampled - 151 cameras with 151 light directions for
 627 each one - we have chosen a subset of the photos for our com-
 628 parison. For each suggested direction by our method, we pick
 629 the closest light direction from the dataset. For this test we have
 630 picked three viewpoints facing the front of the statue, and let the
 631 system choose the best 50 photos for each one, that is, a total
 632 of 150 photos. Figure 18 shows a comparison of a photo from
 633 the original dataset and the resulting model from our method
 634 rendered from the same viewpoint and with the same light di-
 635 rection. Even though our method is not able to reproduce all
 636 the fine specular details, the overall reflectance behavior is well
 637 captured with just a small fraction of the original dataset.

638 As a visual comparison, we have taken a frame from the
 639 BTF renderer demonstration video of Schwartz et al. [1] method.
 640 Figure 19 shows that even with a much simpler acquisition



Figure 18: Result using a dataset acquired with the Bonn Dome. We compare a photo (left) that was not used to produce the result using our system (center), and show the color scale difference (right). There is a more significant error around the neck due to a small variation on the rendered shadow.

641 methodology we can achieve comparable results, since not even
 642 very dense sampling can capture all the fine specular details that
 643 can be seen in the original image.



Figure 19: Comparison between: (left) a frame from Schwartz et al. [1] demonstration video; (middle) rendering with the model produced with our method using a reduced dataset; (right) one of the original photos from the dataset with approximately same viewpoint and light direction.

644 6. Limitations

645 Our method still depends on a reasonably fine and accurate
 646 geometric representation of the model, and it is somewhat sen-
 647 sitive to the camera alignment. In some cases, such as the book,
 648 the misalignment is noticeable, even though it did not greatly
 649 affect the appearance result. Nevertheless, if necessary, this is-
 650 sue can be corrected in a post-processing stage, followed by a
 651 simple refitting of the data.

652 Another issue comes from the fact that small regions not
 653 covered by enough light direction may not be included during
 654 the light directions suggestion. Nevertheless, these vertices can
 655 be spotted by visual inspection in most cases, and a new light
 656 direction can be intuitively set to complete the data. This is
 657 one of the great advantages of having a system with immediate
 658 feedback.

659 Our current implementation is very GPU intensive, and as-
 660 sumes that all data can fit in GPU memory. It thus restrains the
 661 maximum number of photos that can be used simultaneously.
 662 This restriction can be removed by using a multi-pass strategy
 663 to fit the data, where each pass would process a limited number
 664 of vertices.

665 The polynomial fit has its advantages, but it's probably not
 666 the best choice to model all materials. We cannot treat complex
 667 specular behaviors such as Fresnel effects, the main reason for
 668 this is the lack of high sampling density and the inability of
 669 the model to fit data with high variance. We are also limited
 670 to isotropic materials. Nevertheless, it is important to stress
 671 that the data acquired during the photographic session may be
 672 used, in a second stage, to fit other material models, possibly
 673 by clustering the main materials of the objects (like in Palma et
 674 al. [3]), or by taking advantage of the recent studies on BRDF
 675 sampling [28].

676 Finally, even though there is no hard restriction about the
 677 size and geometry, the object has to be illuminated by a pre-
 678 dominant light source for the method to work properly. The
 679 manual placement of the light source may also not fit exactly

680 with the proposed direction by the system, but we noted that
681 this was not an issue during the acquisitions, that is, the method
682 is able to work with a close enough direction. Occasionally the
683 system would suggest a new light direction very close to the
684 previous when the manually placement was too far off, but this
685 did not impose any significant overhead to the acquisition time.

686 7. Conclusion and Future Works

687 In this work we have presented a system for interactively
688 acquiring the material properties of an object using only a camera
689 and a light source. Apart from having a simple setup, the
690 method guides the acquisition by suggesting new light directions
691 to minimize the capture effort, and avoid long acquisition
692 sessions. Moreover, also due to the suggestion system the
693 model achieves overall better per vertex coverage, and the sample
694 distribution can faithfully approximate the reflection function.
695 We have shown results for a variety of materials, such
696 as plastic, plaster, ceramic, cloth, clay, marble and wood, and
697 different geometric complexities.

698 Even without a very sophisticated model, we are able to
699 achieve a good per vertex approximation of the reflectance function
700 by fitting a third degree polynomial to each color channel.
701 With an efficient implementation we provide immediate feedback,
702 which is crucial for *in situ* digitization campaigns. We believe
703 that our method can considerably ease the burden of quality
704 reflectance function acquisition while keeping the acquisition
705 system simple and portable.

706 In order to have immediate feedback we have also avoided
707 costly computational processes, such as clustering as proposed
708 by Lensch et al. [2], or more complex BRDFs non-linear fits.
709 Recent methods such as Nielsen et al. [23] only requires a few
710 samples to properly fit a reflectance function. Nevertheless,
711 their method works well for acquisition of homogeneous materials
712 since it requires sampling the surface from specific angles.
713 This is incompatible with the acquisition of complex spatially-
714 varying BRDFs for heterogeneous materials, where we have to
715 deal with thousands of vertices simultaneously.

716 As future work, we would like to improve a few points of
717 the system, that are not all directly related to the fitting method.
718 The alignment, for example, could be further refined using
719 approaches such as Dellepiane et al's [29] to avoid blurring artifacts
720 in the final results, even if, as previously explained, this
721 can also be corrected in a post-processing stage. Another direction
722 is to try to reduce even more the system setup, and allow for
723 acquisitions using a webcam for example, but our initial tests
724 show that it produces very unreliable colors, making a precise
725 fit an ever greater challenge.

726 We would also like to improve the acquisition itself by introducing
727 more sophisticated calibrations, such as modeling the light source,
728 and new ways to improve the vertex coverage. We have also not
729 addressed the view point selection, which is a task left to the user
730 in our system. Even though selecting view points to cover the object
731 is much more intuitive than selecting light directions, an optimized
732 set of view points would probably reduce even more acquisition times.
733 Finally, we would like to

734 test our system against other types of materials and its scalability
735 with larger objects.

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