

## Effects on the 3D pore network microstructure of consolidated building materials

Elena Possenti <sup>a, \*</sup>, Chiara Colombo <sup>a</sup>, Claudia Conti <sup>a</sup>, Nicoletta Marinoni <sup>b</sup>, Marco Merlini <sup>b</sup>, Riccardo Negrotti <sup>a</sup>, Marco Realini <sup>a</sup>, G. Diego Gatta <sup>b</sup>

<sup>a</sup> *Istituto per la Conservazione e la Valorizzazione dei Beni Culturali (ICVBC), Consiglio Nazionale delle Ricerche (CNR), Via R. Cozzi 53, 20125 Milano, Italy*

<sup>b</sup> *Dipartimento di Scienze della Terra, Università degli Studi di Milano, Via S. Botticelli 23, 20133 Milano, Italy*

**\* Corresponding author: [possenti@icvbc.cnr.it](mailto:possenti@icvbc.cnr.it), Phone number: +39 02 66173386**

*E-mail addresses: [possenti@icvbc.cnr.it](mailto:possenti@icvbc.cnr.it) (E. Possenti, ORCID 0000-0002-9041-7971), [c.colombo@icvbc.cnr.it](mailto:c.colombo@icvbc.cnr.it) (C. Colombo, ORCID 0000-0003-2735-539X), [c.conti@icvbc.cnr.it](mailto:c.conti@icvbc.cnr.it) (C. Conti, ORCID 0000-0002-5379-7995), [nicoletta.marinoni@unimi.it](mailto:nicoletta.marinoni@unimi.it) (N. Marinoni, ORCID 0000-0003-4969-4923), [marco.merlini@unimi.it](mailto:marco.merlini@unimi.it) (M. Merlini, ORCID 0000-0002-1146-2468), [negrotti@icvbc.cnr.it](mailto:negrotti@icvbc.cnr.it) (R. Negrotti, ORCID 0000-0003-1453-4823) [m.realini@icvbc.cnr.it](mailto:m.realini@icvbc.cnr.it) (M. Realini, ORCID 0000-0002-7212-3806), [diego.gatta@unimi.it](mailto:diego.gatta@unimi.it) (G. D. Gatta, ORCID 0000-0001-8348-7181)*

### Abstract

Inorganic-mineral treatments are applied to decayed stone substrates in order to slow the decay processes, through the crystallization of newly-formed crystalline phases within the matrix. In response to the treatment, the original stone material of the substrate is partially transformed into new compounds. The purpose of this study is to explore the effects induced by a promising consolidating treatment based on diammonium hydrogenphosphate (DAP) solutions on Noto limestone, a porous carbonatic matrix used as ornamental stone in the south of Italy. The results, obtained combining water absorption by capillarity measurements, mercury intrusion porosimetry (MIP) and synchrotron radiation X-ray micro-computed tomography (SR- $\mu$ CT), demonstrate that the DAP reaction within the stone induces apparent microstructural modifications. The consolidating treatment induces variations to the porosity

and to the pore size distribution, which, in turn, modify the capillarity absorption and decrease the sorptivity speed. Starting from an insight on a very specific lithotype, this study paves the way to a deeper investigation of the effects induced by a wider range of conservation treatments to the 3D microstructural features of porous geomaterials, by using an innovative multi-scale approach.

**Keywords:**

synchrotron radiation X-ray micro-computed tomography; natural stone material; inorganic consolidant; Cultural Heritage; mercury intrusion porosimetry

**Note for the print:**

All the figures can be printed in black and white in the paper print of the research article. Colours can be used in the digital version of the article.

## 1 Introduction

The carbonatic stones of buildings and sculptures are particularly sensitive to the action of the atmospheric agents, especially when carved and exposed in polluted urban environments. Over time, these ornamental materials are subject to decay processes, which promote decohesion and loss of material [1,2]. In order to slow down the decay process and to restore the loss cohesion among detached stone grains, consolidating treatments are commonly applied to stone materials. In the wide scenario of available treatments for carbonatic stones, the inorganic-mineral diammonium hydrogenphosphate (DAP) is among the most promising [3–8].

When applied to carbonatic matrixes in the form of water-based solutions, the DAP treatment penetrates inside the pores of the stone material, reacts with the substrate and forms newly-formed phases directly within the stone matrix. Reasonably, the crystallization of the new phases in the stone matrix is expected to modify some of the properties of the lithotype, *e.g.*, microstructure, porosity and sorptivity. Traditionally, the most common methods used to

study the modifications induced by the consolidants to the stone are SEM and thin-section study under transmitting-light microscope [9], while physical and mechanical standard tests (UNI EN 15886 [10], UNI EN 15801 [11], NORMAL 7/81 [12], NORMAL 29/88 [13], DRMS [14]) are usually used to evaluate the induced effects. Their coupling with additional techniques, such as mercury intrusion porosimetry (MIP) and capillarity measurements, is the natural and necessary research step [8,15–18].

However, recent studies highlighted [8,19–21] that a multi-scale approach based on the combination of “conventional” methods with advanced imaging techniques (*e.g.*, neutron and X-rays radiography and tomography) actually represents one of the best instigation option. X-ray micro-computed tomography ( $\mu$ CT) is known to be a highly valuable analytical method to study the stone materials microstructure [22], as it provides three-dimensional (3D) information with an excellent spatial resolution (down to the sub-micrometer scale) in a non-invasive way. Furthermore, it also offers an overview of the 3D pore structure, including its modification in terms of morphological and quantitative parameters. In the last few years,  $\mu$ CT has been widely used in conservation studies to investigate the relationship between structure and properties of building materials (stones, concretes [23], mortars [24–26]), their weathering/decay [9,27,28] and conservation [21,27,29–32].

$\mu$ CT studies can be carried out by using the conventional X-rays sources as well as a synchrotron radiation (SR) source, the latter providing several advantages in terms of quicker acquisition time, better sensitivity and contrast, higher voxel size resolution and a general reduction of image artifacts [33].

Here, the synchrotron radiation X-ray micro-computed tomography (SR- $\mu$ CT) is used in combination with conventional methods as determination of water absorption by capillarity and mercury intrusion porosimetry, to investigate the microstructural variations induced by phosphate-based consolidating treatments to the Noto limestone, a porous carbonatic lithotype used as ornamental stone for facades and sculptures in the south of Italy.

A critical comparison among these methods, which are established methods to investigate the properties of materials, is discussed in order to evaluate their peculiarities and complementarities for the study of conservation treatments applied to the preservation of porous stone materials.

## 2 Materials and methods

### 2.1 Materials

The Noto limestone is a calcarenite outcropping in the Val di Noto (south-eastern Sicily) used as building stone for the elaborated Baroque monuments since ancient time [34–38]. Among the several varieties of porous limestones of the Iblean Plateau, the *Noto Yellowish Limestone* variety was selected for the study. It is a biomicrite [38] mainly made of calcite, with subordinate clay minerals, quartz and iron oxides, and high porosity (25-37 %) in the range of the micro-pores [37].

A set of freshly quarried prismatic specimens (50×50×20 mm) were treated by poultice with a 0.76 M DAP water solution (DAP CAS Number 7783–28-0, assay  $\geq$  99.0%, reagent grade; dry cellulose pulp MH 300 Phase, Italy; poultice ratio  $\sim$  5:1 DAP solution: cellulose pulp). A poultice layer of about 1-1.5 cm was applied onto the specimens and a sheet of Japanese paper was placed between the paper poultice and the stone surface, to prevent damages at the specimen surface due to the sticking of the poultice after drying. During the treatment, the specimens were wrapped in a plastic film. After 2 h, the plastic film was removed and the specimens were left drying at room temperature for 24 hours with the poultice on top. The poultice was then removed and all the specimens were rinsed three times by immersion in MilliQ water and dried again.

### 2.2 Methods

A characterization was carried out by scanning electron microscopy coupled with energy dispersive X-ray spectrometer (SEM-EDS, JEOL 5910 LV with tungsten filament coupled EDS spectrometer IXRF-2000) and by X-ray powder diffraction (XRPD, Panalytical X'Pert PRO X-ray powder diffractometer equipped with a Cu-K $\alpha$  radiation) to check the morphology and mineralogical composition, respectively, of the stone matrix before and after the DAP treatment.

Measurements of the water absorption by capillarity were carried out on the same specimens before and after the DAP treatment, in order to explore the modification induced by the DAP treatment on the water uptake properties of the lithotype. The measurements, performed



accordingly with the European Standard UNI EN 15801:2010 [11], determine the water absorption of the specimens in contact with deionised water through a multiple layer of about 1 cm of filter papers (specimens dried for 7 days at  $60\pm 2$  °C before the investigations, experiments at room temperature in sealed boxes, measurements at regular steps: 10, 20, 30, 60 min, and 2, 4, 5, 24 h). The gravimetric increase is expressed as amount of absorbed water per surface unit  $Q$  ( $\text{mg cm}^{-2}$ ), water absorption curves ( $Q$  over square root of the absorption time) and capillary absorption coefficient  $CA$  ( $\text{mg (cm}^2\sqrt{\text{s}})^{-2}$ ) [39].

Mercury intrusion porosimetry (MIP) is used to study the porosity of the lithotype and the measurements were carried out with a Thermo Scientific mercury intrusion porosimeter Pascal 140 + Pascal 240. MIP data are collected in the pore radii range 50-0.0037  $\mu\text{m}$  (the pressure can be varied 0.02 - 200 MPa), which comprises from mesopores to megapores according to the IUPAC classification [40,41]. The volume resolution is 0.1  $\text{mm}^3$  and accuracy  $> 0.2$  %. The pores are then subdivided in 20 pore size classes to describe the pore size distribution and to evaluate the contribute of smaller classes of pores to the total open porosity. The Student's t-test was carried out on MIP results to determine if the two datasets are significantly different from each other.

Due to the destructive nature of this technique (mercury impregnates the sample so that it is not completely removable after the investigation; pressure carried out by mercury porosimeter might occasionally generate spurious micro-cracks [23]), it was not possible to repeat the MIP investigations on the same sample before and after the treatment; then, a first set of 3 samples was analyzed to study the lithotype microstructure before the treatment and a second group of 9 samples to highlight to modifications occurred after the crystallization.

Synchrotron radiation X-ray micro-computed tomography (SR- $\mu\text{CT}$ ) was used to investigate the pore network and to explore the influence of DAP treatments on its 3D features. SR- $\mu\text{CT}$  investigations were carried out at the ID11 beamline of ESRF (European Synchrotron Radiation facility; Grenoble, France). The hard X-ray imaging experiments were carried out using a parallel monochromatic 25 keV X-ray beam. The samples were mounted onto a high-resolution rotation stage and 1440 X-ray projections were acquired with constant angular step over a  $180^\circ$  rotation, with a sample-to-detector distance of 80 mm (phase-contrast mode), exposure time/projection 1.5 s and effective pixel size of 0.9  $\mu\text{m}$ . The scintillator screen used to convert X-rays into visible light consists of a gadolinium oxysulfide layer of 60  $\mu\text{m}$  thickness. The image on the scintillator was recorded with a Fast Readout Low Noise

detector (FReLoN), equipped with a 14 bit dynamic CCD camera and a 2048×2048 pixel chip.

To reconstruct a 3D image of the specimens, the tomographic projections were elaborated with the *SYRMEP Tomo Project* (STP), an open-source software tool designed for post-beamtime use [42,43]. In order to enhance the reliability of morphological and quantitative analysis of porosity, a single-distance phase-retrieval algorithm was used to increase the contrast between solid portion and voids. The 2D reconstructed slices were pre- and post-processed by using the ImageJ freeware software [44,45].

The segmentation (or binarization) of digital images was carried out in order to distinguishing elements of the stone matrix (voids, calcite of the substrate, newly-formed phases), initially detectable by their different grey values. During the process, the use of suitable thresholds isolated the voids from the stone matrix and provided an estimation of the total porosity. The segmentation resulted into binary images where similar elements are visualized as sets of contiguous voxels. Filtering has been necessary to homogenize the images, to enhance the contrast, to reduce the background noise of the reconstructed slices (which might negatively affect the segmentation process) and to enhance borders of the pores original volume stacks [46,47].

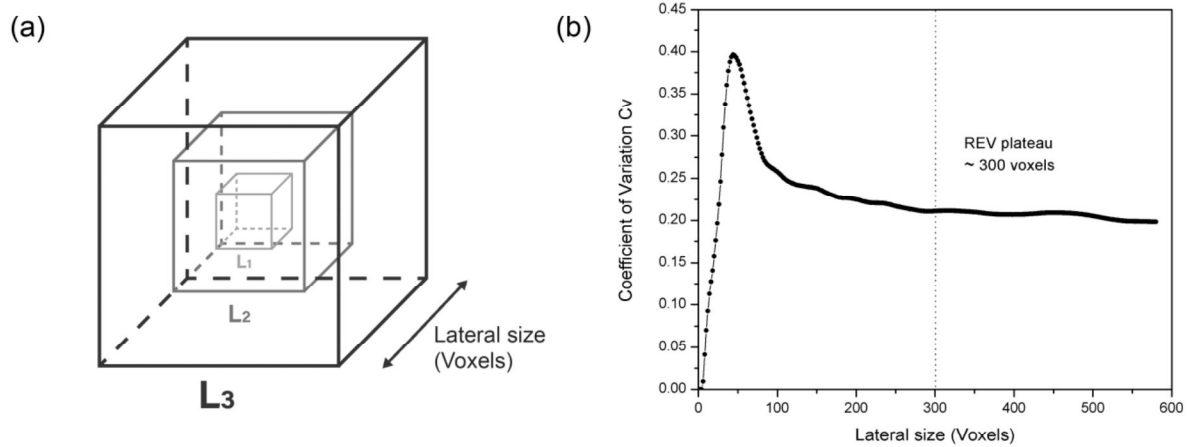
The connected porosity was extracted from the segmented images using the tool “Find connected regions” of the FIJI software. Isolated pores were extracted by the total porosity by subtraction and separately analyzed.

The quantitative 3D image analysis of the porosity was carried out with the software library *Pore3D* [46].

In order to analyze the basic textural features of the pore structure and the connectivity of the pores, the following quantitative morphometric parameters of *Minkowskii functionals* were obtained: i) the volume density ( $V_v$ ), a dimensionless parameter ( $0 < V_v < 1$ ) expressed as the ratio of the number of voxels belonging to the object phase with respect to the total number of voxels in the considered VOI. In this study, the object phase is the pores, thus  $V_v$  corresponds to the porosity; ii) the Euler characteristics ( $X_v$ ), a descriptor index of the connectedness of a 3D pore network, indicating the number of connections between void structures per unit volume.  $X_v$  is expressed in  $\text{mm}^{-3}$  and it is positive when the number of isolated pores exceeds the number of multiple interconnections between the pores or negative for connected pore networks [48].

Several volume of interest (VOI) were selected assuming that the VOI is big enough to enclose a representative amount of the sample heterogeneity (Representative Elementary

Volume, REV) [46,49]. The REV size was determined by using the box-counting method [50], namely by studying the variation of the volume density for multiple concentric increasing sub-volumes (Figure 1a) and calculating the variability at each step in the form of a dimensionless coefficient of variation  $C_v$  (arithmetic mean divided by the standard deviation) [51]. In this study, representative 3D subvolumes of  $300 \times 300 \times 300$  voxels each (corresponding to a cube of  $\sim 300 \mu\text{m}$  side length) are initially extracted from the original dataset, considering the criterion suggested by Zhang et al. [52], which defines the REV on the basis that the mean reaches a reasonable plateau ( $C_v < 0.2$ ) as shown in Figure 1b.



**Fig. 1** (a) scheme, not in scale, of the REV size determination by using the box-counting method [46,49]. The volume density ( $V_v$ , the ratio of the number of voxels belonging to the voids with respect to the total number of voxels in the considered VOI) is the investigated variable to determine the REV. (b) REV determination by plotting the coefficient of variation  $C_v$ , defined as the ratio of the arithmetic mean divided by the specimen standard deviation, vs the lateral size, a progressive and concentric number of voxels. A reasonable plateau is reached for cubes of about 300 voxels per side

Skeletonization, a thinning procedure to a simpler visualization of the “backbone” of the pore object, was carried out on the connected pores by applying the GVF algorithm [48,53]. As the skeletonization preserves the geometrical and morphological feature of the pore object, the skeleton and its 3D volumes are used to investigate and visualize the actual connectivity of the pore network.

The 3D renderings were obtained using the commercial software VGStudio 3.1.2.

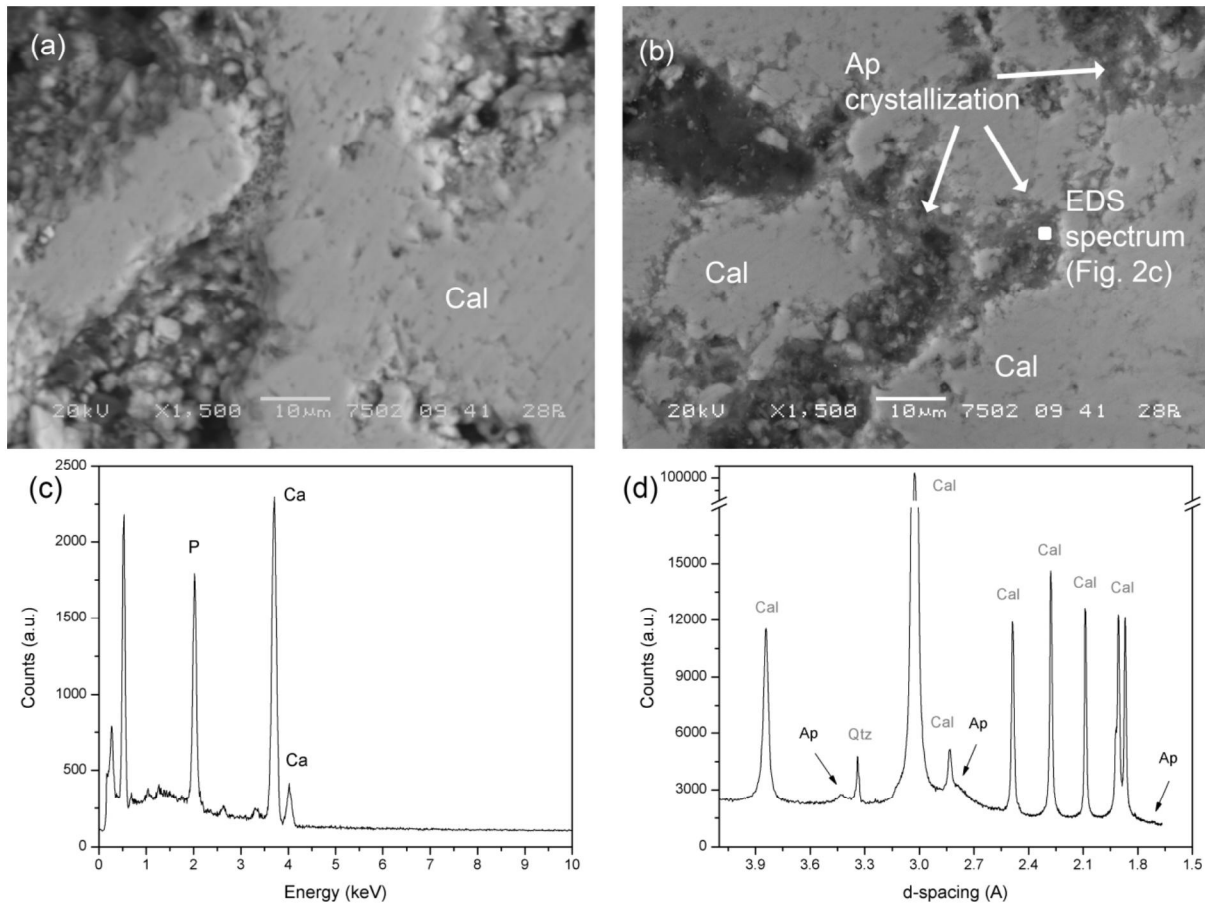
SR- $\mu$ CT investigations were not carried out on the same specimen before and after the consolidation as small samples ( $2 \times 2 \times 20$  mm) are required in order to collect high resolution datasets.

For these reasons, suitable fragments for MIP (7×7×2 mm) and SR- $\mu$ CT (2×2×20 mm) were sampled from the 50×50×20 mm specimens, before and after the DAP treatment. This condition does not negatively affect the study, which is aimed at obtaining an overview of the porous network modification trend induced by the treatment to the stone matrix

MIP and SR- $\mu$ CT investigations are referred to the first 2 millimeters of the treated surface, as the crystallization and the microstructure modification was found to be more apparent in the portion of material closer to the treated surface (unpublished data).

### 3 Results

The reaction of DAP water-based solutions with calcite of Noto limestone gives rise to the formation of calcium phosphates on pore walls, as demonstrated by the morphological observations and by the elemental distribution of calcium and phosphorus (Figure 2a-c). The untreated lithotype has neat grain boundaries while the treated matrix shows a crystal growth in dark grey values at the interface at the walls of the pores and the voids. The newly-formed phases are calcium phosphates (most likely nanocrystalline hydroxyapatite) as revealed by the X-ray diffraction peaks at  $\sim 3.43 \text{ \AA}$ ,  $2.77 \text{ \AA}$ ,  $1.71 \text{ \AA}$  highlighted in Figure 2d.



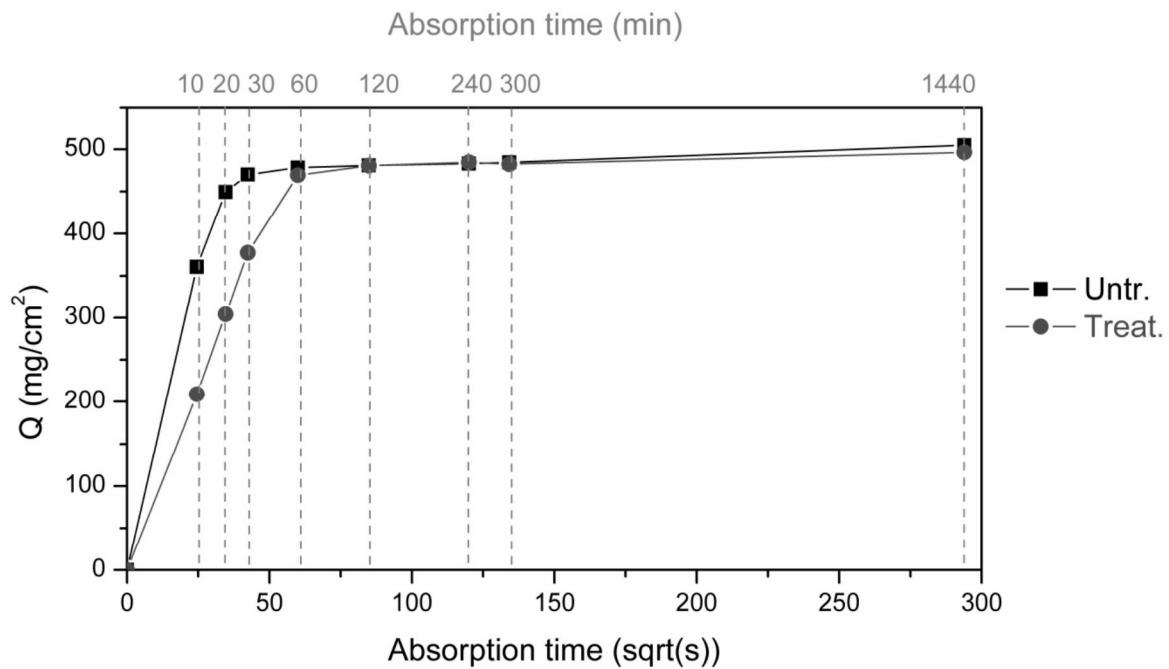
**Fig. 2** SEM images of untreated (a) and treated (b) Noto limestone. In (a) the grain boundaries of calcite are neat while in (b) the pore walls show irregular boundaries and the overgrowth of newly-formed phases in darker grey value (pointed out by the arrows). The EDS microanalyses showed in (c) is carried out on a representative dark grey area of the (b) image and displays the well distinguishable formation of the Ca- and P-bearing phases on the boundaries of calcite grains. XRD pattern of the treated Noto limestone (d). Cal = calcite, Qtz = quartz, Ap = apatite and calcium phosphates

### 3.1 Water absorption by capillarity

A comparison of the water absorption curves of Noto limestone specimens before and after the DAP-based consolidation is plotted in Figure 3, as the average of the measurements carried out on 6 specimens. A modification after the application of the treatment is unambiguously detected: the  $Q$  values (amount of water absorbed per surface unit,  $\text{mg cm}^{-2}$ ) decrease after the DAP treatment and that this decrease occurs at each absorption time. At the end of the measurements, the treated specimens show a total  $Q$  slightly lower than in the untreated specimens.

The capillary absorption coefficient  $CA$  (the curve slope) shows that the almost complete saturation of the specimens is slower for the treated stone material. In fact, the plateau of the curve is reached in  $35\text{-}42 \sqrt{s}$  ( $\sim 20\text{-}30$  min) in the untreated stone and in  $60 \sqrt{s}$  ( $\sim 60$  min) in the treated one.

The variation of the sorptivity properties is correlated to the porosity modification, which in turn depends on the DAP reaction with calcite of pore walls. To explore these changes, the microstructure and the 3D pore system are investigated by MIP and SR- $\mu$ CT.



**Fig. 3** Water absorption curves of untreated (-■- Untr.) and treated (-●- Treat.) Noto limestone specimens. Each curve is the average of the water absorptions of 6 different specimens. Time is expressed also in minutes (min) for clarity's sake. All the treated specimens undergo a similar trend, namely, the decrease of the suction speed and the fraction of water absorbed in the short term

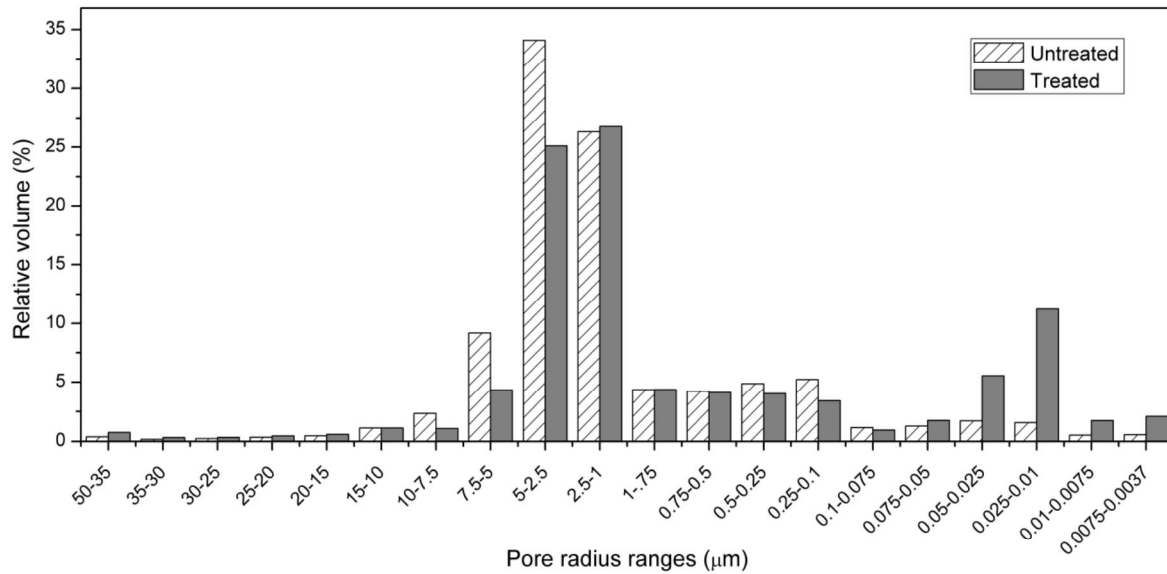
### 3.2 Mercury intrusion porosimetry (MIP) measurements

The results of mercury intrusion porosimetry measurements of untreated and treated Noto limestone are showed in Figure 4. The MIP data, their standard deviation and the results of the Student's t-test are given in the Appendix A.

The untreated Noto limestone is characterized by an average total open porosity between 36.05 % (standard deviation  $\sigma = 1.17$  %), which is in accordance with the values assessed in a previous study carried out on a even wider set of quarry specimens [35,37]. Its pore size distribution is characterized by an unimodal feature with the  $\sim 70$  % of the total open porosity

in the range of 7.5-1.0  $\mu\text{m}$ , while the remaining total open porosity is partitioned as following: about 18-19 % of the pores have a pore radius range between 1-0.1  $\mu\text{m}$ , 6-7 % have a pore radius lower than 0.1  $\mu\text{m}$  and about 5-6 % have a pore radius larger than 7.5  $\mu\text{m}$ . The average pore radius is 2.49  $\mu\text{m}$  ( $\sigma = 0.36 \mu\text{m}$ ).

The treated lithotype shows a different feature, with the average of the total open porosity of 33.62 % ( $\sigma = 2.99 \%$ ) and an average pore radius of 1.67  $\mu\text{m}$  ( $\sigma = 0.38 \mu\text{m}$ ).



**Fig. 4** Pore size distribution of Noto limestone before (Untreated) and after (Treated) the DAP consolidating treatment. The histograms are the average of 3 and 9 specimens for the untreated and treated lithotype, respectively

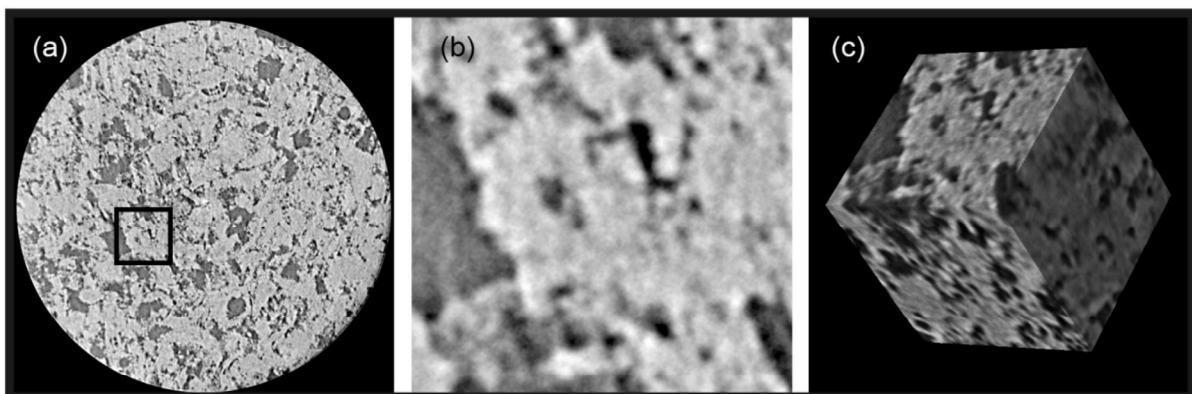
Regarding the pore size distribution, the treated stone specimens show differences with respect the untreated ones: i) the average pore radius is about 26-33 % thinner; ii) the % of coarser pores is lower, especially those having radius in the range 15-2.5 microns, while the % of finer ones (voids characterized by radius smaller than 1  $\mu\text{m}$ ) is higher.

Statistically, a significant difference between untreated and treated specimens is noted on the average pore radius and on the pore size distribution, as demonstrated by their standard deviation and by the low probabilities calculated by the Student's t test (for average pore radius:  $p = 0.01$ ; for pores with radius smaller than 0.5  $\mu\text{m}$ :  $0.00 \leq p \leq 0.23$ , Student's t test; complete data available in the Appendix A). Differences occurred also about the total open porosity ( $p = 0.21$ , Student's t test), even though the contribute of the DAP treatments is most likely partially blinded by the microstructural heterogeneity of the lithotype.

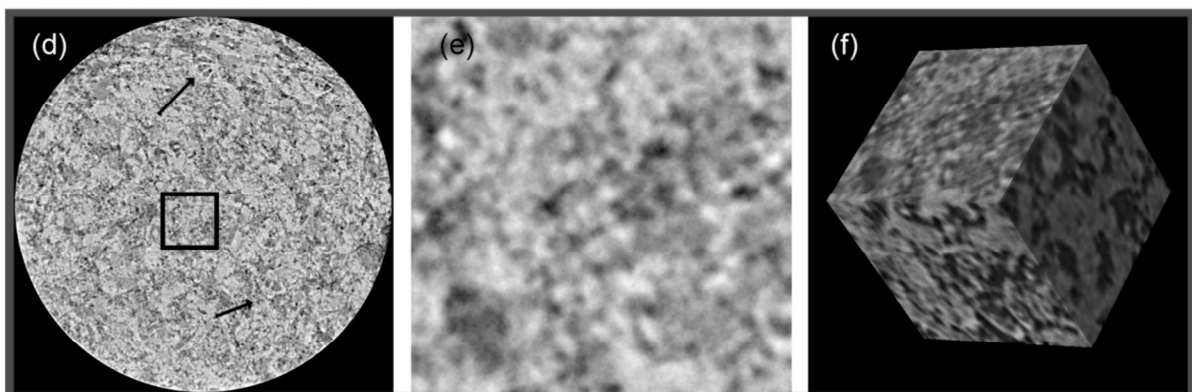
### 3.3 Synchrotron radiation X-ray micro-computed tomography (SR- $\mu$ CT)

Figure 5 presents the two external slices, the selection of a representative VOI and the descending volume rendering of untreated and treated Noto limestone. In the slices of untreated Noto limestone, mainly two grey values are visible: a dark grey, corresponding to the voids of the sample, and a lighter one, corresponding to calcite of the matrix. The slices of treated Noto limestone show a different morphology, with a third halfway grey value localized mainly inside the pores and on pore walls. It seems composed by micro-particles, suggesting that this third grey value is due to the formation of micrometric and sub-micrometric phases. These morphologies are very similar to those observed by SEM on an equivalent treated specimen (Figure 2b).

Untreated Noto limestone



Treated Noto limestone



**Fig. 5** Untreated and treated Noto limestone. Reconstructed slice of the surface (a, d), detail of an area of  $300 \times 300$  voxel<sup>2</sup> indicated by the black square (b, e) and volume renderings (c, f)



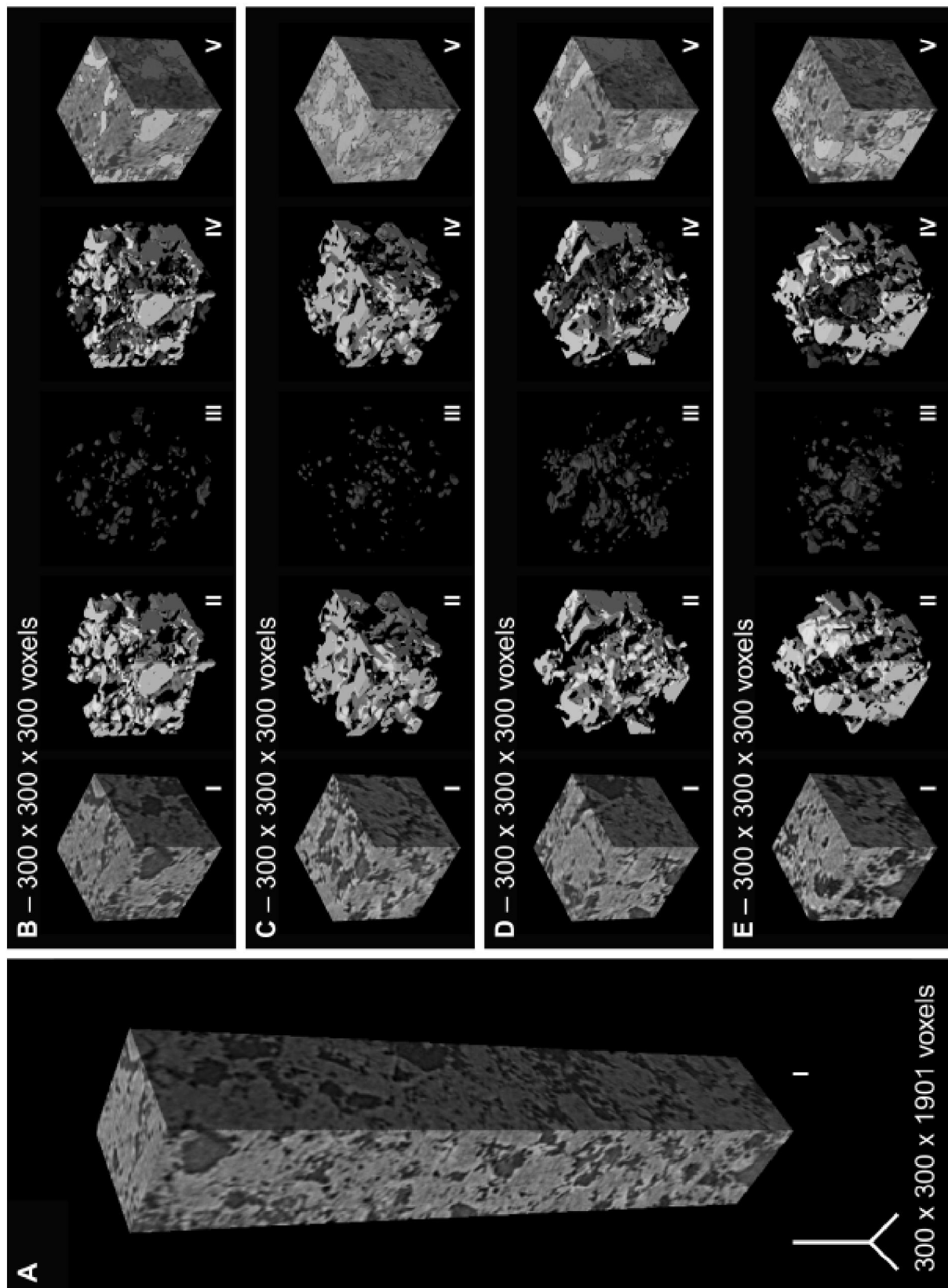
The clear presence of the morphology and the grey values attributed to phosphate phases in the reconstructed images is more visible in the most external slices (namely those closer to the treated surface), while this effect wanes as long as the slices are referred to inner portions. This feature reverses in the last slices, where the image reconstruction shows a further increase of halfway grey values attributed to phosphates in the voids. This can be attributed to a more abundant crystallization of new phases, which most likely occurs locally, in correspondence of preferential diffusion path. SR $\mu$ -CT images demonstrated that the new phases do not fill the voids but form a highly porous network of micrometric crystals nucleated on the pore surfaces.

In order to study the pore distribution and connectivity, the voids were digitally isolated from the bulk of the stone matrix by segmentation. In this SR $\mu$ -CT study, the total porosity estimated during the thresholding is  $\sim 24.91\%$  for untreated Noto limestone and  $\sim 22.79\%$  for the treated sample. As calculated by the morphometric analysis, about the  $\sim 95-96\%$  of the total porosity is composed by a system of open and interconnected cells (connected porosity), while the remaining fraction are isolated voids (Table 1, presented as volume density  $V_v$ ). The treated stone material shows a slightly higher percentage of connected pores with respect to the untreated one, even though the difference is rather negligible. The datasets generated by the segmentation of the voids on untreated and treated Noto limestone are showed in Figure 6 and Figure 7 as 3D renderings of interconnected and isolated pores.

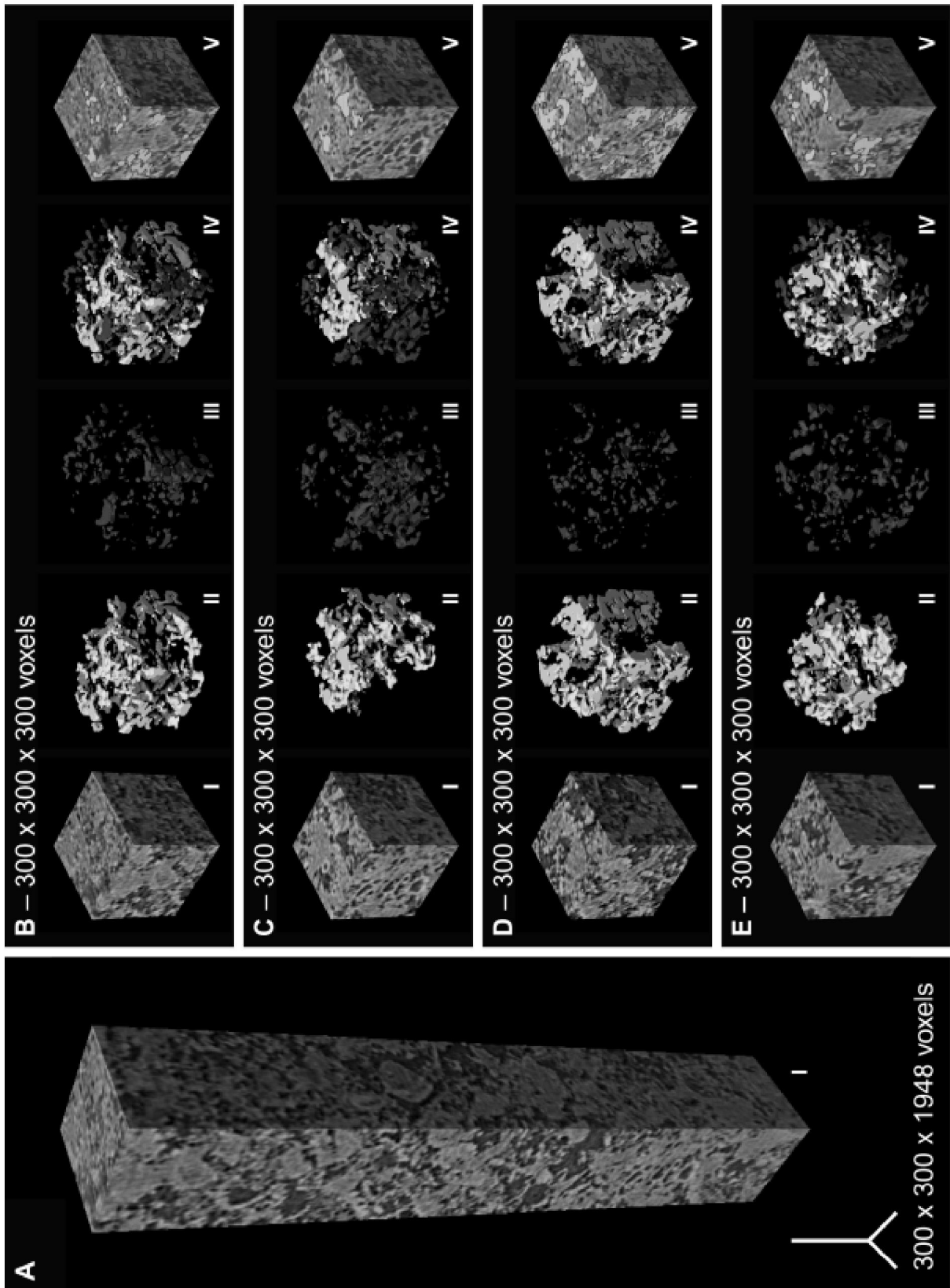
**Table 1** Morphometric analysis. The arithmetic mean (AM) and the standard deviation ( $\sigma$ ) are indicated for values obtained with the morphometric analysis

Feature of the VOI		Sample	
		Untreated Noto limestone	Treated Noto limestone
Volume of total voids (%)		$\sim 24.91$	$\sim 22.79$
Volume density $V_v$ of connected pores	AM	0.26	0.20
	$\sigma$	0.03	0.02
Volume density $V_v$ of isolated pores	AM	0.008	0.007
	$\sigma$	0.0009	0.002
Euler characteristics $X_v$ of	AM	-22583	-28549

<b>connected pores (mm<sup>-3</sup>)</b>	$\sigma$	12094	9537
--	----------	-------	------



**Fig. 6** Volume renderings of untreated Noto limestone: parallelepiped cropped from the whole SR $\mu$ -CT dataset (A) and VOIs (300 $\times$ 300 $\times$ 300 voxels) close to the surface (B), just below (C), from the middle (D) and close to the bottom (E). The renderings include: X-ray tomographic images (I), connected (II) and isolated (III) pores, combination of connected and isolated pores (IV) and their inset in the volume rendering



**Fig. 7** Volume renderings of treated Noto limestone: parallelepiped cropped from the whole SR $\mu$ -CT dataset (A) and VOIs (300 $\times$ 300 $\times$ 300 voxels) close to the surface (B), just below (C), from the middle (D) and close to the bottom (E). The renderings include: X-ray tomographic images (I), connected (II) and isolated (III) pores, combination of connected and isolated pores (IV) and their inset in the volume rendering

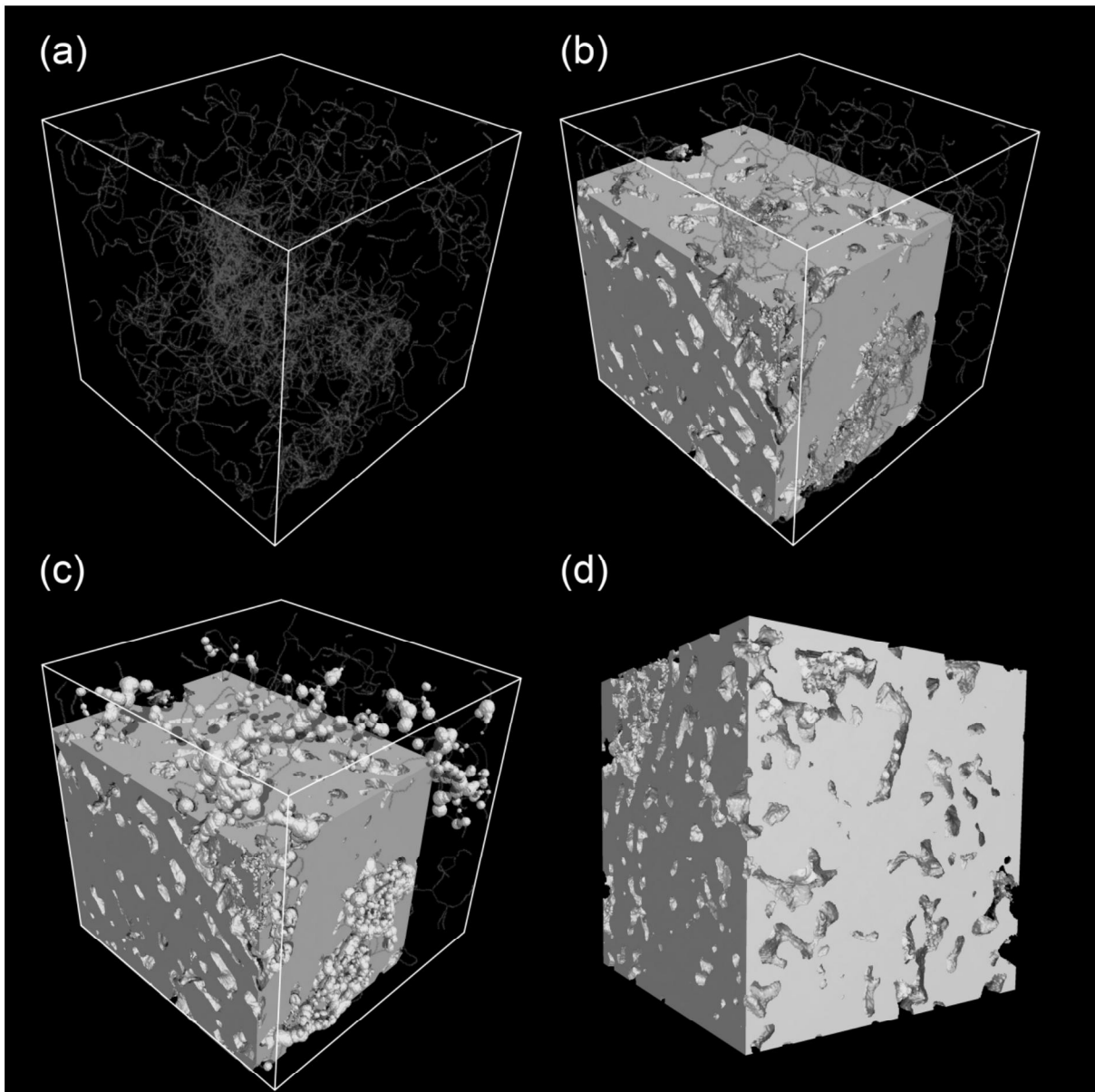
No cracks are detected, indicating that: i) the quarry lithotype used in this study has no natural discontinuities; ii) the crystallization of new phases within the matrix during the treatment do not introduce a mechanical stress to the microstructure, which in turn might generate cracks.

Focusing on the connected components, the so-called “open porosity”, the porous structure of all the VOIs is characterized by a complex system of branching. The image processing of connected regions, namely regions composed by contiguous voxels in at least one of the three direction (threshold used: 10000 voxels, connection with face-face, side-side or corner-corner), revealed that the porous structure is highly interconnected and that the connected pores are in a modest number in all the investigated VOIs. In many VOIs and depending on the use of filters, one, two or three “objects” (namely, pores) constitute a single highly branched void of a determined VOI. In other words, selecting a single and even small pore, its branching constitutes a relevant % of the total open porosity of the investigated volume. This feature is present either on the untreated matrix either on the treated one.

The high connectivity of the Noto limestone microstructure is explored by the quantitative morphometric analysis, and by the skeleton analysis [48] and its 3D renderings (Figure 8).

The Euler characteristics ( $X_v$ ), used as topological descriptors and calculated on binarized volumes, are shown in Table 1. The  $X_v$  values are negative either before and after the DAP treatment, thus demonstrating that the pores of both the stone matrixes are highly interconnected. The treated lithotype is characterized by  $X_v$  values more negative than those recorded on the untreated one, indicating that the treated matrix has a porous framework more interconnected than the untreated one. This aspect could be an effect induced by the DAP treatment, even though it is not possible to attribute this feature only to the consolidation as the investigations are carried out on different micro-specimens and considering the heterogeneity of the Noto microstructure.

The skeleton analysis confirm the high connectivity of the pore network, showing that the branching of the pore space is composed by an open cell structure linked by a high number of connecting channel. Figure 8 shows an isosurface rendering of the stone matrix of treated Noto limestone, with the inset of the skeleton and the volume rendering of the max spheres inflated in the nodes of the skeleton. The nodes are the “pore bodies” [48], namely the junction voxels among three or more branches. The connected pores are represented by the skeleton and they compose a dense framework of branches mutually interconnected.



**Fig. 8** 3D rendering of the connected pores skeleton (in violet) of treated Noto limestone (a). The white cube represents the VOI of  $300 \times 300 \times 300$  voxels; inset of the skeleton in a clipped isosurface rendering of the VOI (b); pore nodes (in yellow) of the skeleton, namely the volume rendering of the max spheres inflated in the nodes of the skeleton (c). The nodes are the “pore bodies”, namely the junction voxels among three or more branches; 3D rendering of the VOI with the inset of pore nodes and skeleton without clippings.

## 4 Discussion

The water absorption measurements show evidence that the stone matrix preserves its wetting and hydrophilic properties after the DAP consolidating treatment. At the same time, the stone material experiences a decrease of the amount of water uptake per surface unit and of the

suction speed. This effect is directly linked to a modification of the microstructure of the material, due to the crystallization of newly-formed phosphate phases on pore walls.

In fact, the treated Noto limestone specimens show evidence of a minor total open porosity, a minor average pore radius and a different pore size distribution with respect to the untreated matrix. It is conceivable that these differences between untreated and treated lithotype depends on the DAP consolidating treatment, in particular regarding the variation of the average pore radius and the pore size distribution, where the standard deviation of MIP measurements was pretty narrow and the statistical t-test results showed a noticeable differences between the untreated and treated datasets.

The crystallization of the new phases within the stone matrix and the descending microstructural effects are univocally attributed to the diffusion itself and not to a system of micro-cracks which might act as preferential diffusion paths. Both before and after the DAP treatment, the stone matrix is characterized by a system of highly interconnected communicating channels, which is the “spine” that rules to the consolidant impregnation and redistribution.

MIP and SR $\mu$ -CT results comply with the detection that the total open porosity is higher in the treated lithotype than in the untreated one, even though the SR $\mu$ -CT porosity values are different from MIP ones. This is due to several reasons: i) part of the open porosity of Noto limestone, treated and untreated, is below the detection limit of SR $\mu$ -CT. In fact, as in this study the voxel size is of 1  $\mu\text{m}^3$ , all the pore objects with size minor than 1  $\mu\text{m}$  are not detectable. More precisely, considering that at least two or three contiguous voxels are needed to be identified as a void and not as noise, pores with a radius minor than 1  $\mu\text{m}$  cannot be considered in the total porosity quantified by SR $\mu$ -CT; ii) in the case of SR $\mu$ -CT, the volume % is calculated by the software using threshold algorithms and image filters, thus differences in the calculated volume % of voids might rise by varying the threshold values; iii) the pore size distribution (assessed by MIP) of the treated lithotype is different from the untreated one, with a % volume decrease of the pore classes detectable by SR $\mu$ -CT and a % volume increase of not detectable voids.

To explore the variations of these sub-micrometric pore classes (micropores IUPAC range), the MIP contribute is fundamental, even though approximated to a system of cylinder-shaped capillaries. On the other side, SR $\mu$ -CT volume renderings showed that in many cases the pores are pretty different by an idealized system of cylinders, as their morphology frequently presents throats, bigger pores connected by thinner channels, pore-to-end branches, irregular-shaped cavities, etc. For these reason, SR $\mu$ -CT investigations allowed visualizing and

quantifying the real morphology of the voids (in the resolution limit), bypassing the cylinder-shaped model used by MIP (which, as drawback, suffer of the ink-bottle effects and is subjected to the overestimation of finer pores).

## Conclusions

The evolution of microstructure and capillarity property of Noto limestone consolidated with DAP treatments have been investigated. The results show evidence that the crystallization of phosphates within the stone matrix modifies the internal microstructure of the lithotype, which, in turns, determines a modification the properties of the stone matrix. At the same time, the treatment do not revolutionize the lithotype in its peculiar features (*e.g.*, hydrophilic properties, permeability to water flow, capability to absorb water by capillarity), which actually experiences positive modifications in terms of suction speed. This variations are expected to give positive implication especially in outdoor conditions, where a minor capacity to absorb water might preserve the stone material by the quick absorption of harmful water-based solutions (*e.g.*, acid rains or rising of soluble salts solutions).

The combination of water absorption measurements with MIP and SR- $\mu$ CT resulted to be a powerful multi-analytical protocol to study the 3D textural feature of porous stone materials and to understand how these materials are modified when treated with inorganic-mineral products. Further innovative studies are already ongoing to deeper investigate the morphology of stone boundaries after the DAP reaction, the diffusion of the new phases within the stone matrix and their arrangement in cavities and pore walls. In this view, the present study opens the scenario to new set of multi-scale studies focused to explore with a high resolution a wide spectrum of porous geomaterials treated with innovative conservation products.

## Acknowledgements

The authors gratefully acknowledge the ESRF for beamtime allocation and Dr. Roberta Possenti for her support in the image processing.



## Declaration of interest

None

## Funding

This research did not receive any specific grant from funding agencies in the public, commercial, or not-for-profit sectors.

## Supplementary information

Electronic supplementary material: The online version of this article contains supplementary material, which is available to authorized users (Appendix A).

## Data availability

The raw/processed data required to reproduce these findings cannot be shared at this time as the data also forms part of an ongoing study.

## References

- [1] Commissione Tecnica UNI, UNI 11182:2006 Beni culturali - Materiali lapidei naturali ed artificiali - Descrizione della forma di alterazione - Termini e definizioni, (2006) 1–33.
- [2] ICOMOS-ISCS, Illustrated glossary on stone deterioration patterns. English-French version, (2008) 1–78.
- [3] G. Graziani, E. Sassoni, G.W. Scherer, E. Franzoni, Phosphate-based treatments for consolidation of salt-bearing Globigerina limestone, in: IOP Conf. Ser. Mater. Sci. Eng., 2018: p. 12082. doi:10.1088/1757-899X/364/1/012082.
- [4] E. Possenti, C. Colombo, C. Conti, L. Gigli, M. Merlini, J.R. Plaisier, M. Realini, D. Sali, G.D. Gatta, Diammonium hydrogenphosphate for the consolidation of building materials. Investigation of newly-formed calcium phosphates, *Constr. Build. Mater.* 195 (2019) 557–563. doi:10.1016/j.conbuildmat.2018.11.077.
- [5] E. Possenti, C. Colombo, C. Conti, L. Gigli, M. Merlini, J.R. Plaisier, M. Realini, G.D. Gatta, Grazing incidence synchrotron X-ray diffraction of marbles consolidated with diammonium hydrogen phosphate treatments: non-destructive probing of buried minerals, *Appl. Phys. A.* 124 (2018) 383. doi:10.1007/s00339-018-1798-8.
- [6] E. Sassoni, Hydroxyapatite and Other Calcium Phosphates for the Conservation of Cultural Heritage: A Review, *Materials* (Basel). 11 (2018) 557. doi:10.3390/ma11040557.
- [7] E. Possenti, C. Colombo, D. Bersani, M. Bertasa, A. Botteon, C. Conti, P.P. Lottici, M. Realini, New insight on the interaction of diammonium hydrogenphosphate

- conservation treatment with carbonatic substrates: A multi-analytical approach, *Microchem. J.* 127 (2016) 79–86. doi:10.1016/j.microc.2016.02.008.
- [8] G. Graziani, C. Colombo, C. Conti, E. Possenti, E. Perelli Cippo, M. Realini, E. Sassoni, Neutron radiography as a tool for assessing penetration depth and distribution of a phosphate consolidant for limestone, *Constr. Build. Mater.* 187 (2018) 238–247. doi:10.1016/j.conbuildmat.2018.07.173.
- [9] J. Dewanckele, T. De Kock, M.A. Boone, V. Cnudde, L. Brabant, M.N. Boone, G. Fronteau, L. Van Hoorebeke, P.J.S. Jacobs, 4D imaging and quantification of pore structure modifications inside natural building stones by means of high resolution X-ray CT., *Sci. Total Environ.* 416 (2012) 436–48. doi:10.1016/j.scitotenv.2011.11.018.
- [10] UNI Ente Nazionale Italiano di Unificazione, UNI EN 15866: 2010, Conservation of cultural property–test methods–colour measurement of surfaces., (2010).
- [11] Commissione Tecnica UNI, UNI EN 15801:2010 Conservation of cultural property – test methods – determination of water absorption by capillarity, (2010).
- [12] C.- ICR, NORMAL 7/81 Natural Stones Test Methods: Determination of Water Absorption by Total Immersion, (1981).
- [13] C.- ICR, NORMAL 29/88 Determination of Drying Index, (1988).
- [14] J.D. Rodrigues, A.P.F. Pinto, D.R. da Costa, Tracing of decay profiles and evaluation of stone treatments by means of microdrilling techniques, *J. Cult. Herit.* 3 (2002) 117–125. doi:10.1016/S1296-2074(02)01172-X.
- [15] E. Sassoni, G. Graziani, E. Franzoni, An innovative phosphate-based consolidant for limestone. Part 1: Effectiveness and compatibility in comparison with ethyl silicate, *Constr. Build. Mater.* 102 (2016) 918–930. doi:10.1016/j.conbuildmat.2015.10.202.
- [16] G. Graziani, E. Sassoni, G.W. Scherer, E. Franzoni, Penetration depth and redistribution of an aqueous ammonium phosphate solution used for porous limestone consolidation by brushing and immersion, *Constr. Build. Mater.* 148 (2017) 571–578. doi:10.1016/j.conbuildmat.2017.05.097.
- [17] E. Franzoni, E. Sassoni, G. Graziani, Brushing, poultice or immersion? The role of the application technique on the performance of a novel hydroxyapatite-based consolidating treatment for limestone, *J. Cult. Herit.* 16 (2015) 173–184. doi:10.1016/j.culher.2014.05.009.
- [18] I. Osticioli, G. Botticelli, P. Matteini, S. Siano, R. Pini, M. Matteini, Micro-Raman analysis on the combined use of ammonium oxalate and ammonium phosphate for the consolidation and protection of carbonate stone artifacts, *J. Raman Spectrosc.* 48 (2017) 966–971. doi:10.1002/jrs.5150.
- [19] C. Conti, C. Colombo, G. Festa, J. Hovind, E.P. Cippo, E. Possenti, M. Realini, Investigation of ammonium oxalate diffusion in carbonatic substrates by neutron tomography, *J. Cult. Herit.* 19 (2016) 463–466. doi:10.1016/j.culher.2015.12.005.
- [20] M. Realini, C. Colombo, C. Conti, F. Grazi, E. Perelli Cippo, J. Hovind, Development of neutron imaging quantitative data treatment to assess conservation products in cultural heritage, *Anal. Bioanal. Chem.* 409 (2017) 6133–6139. doi:10.1007/s00216-017-0550-0.
- [21] S. Raneri, G. Barone, P. Mazzoleni, I. Alfieri, L. Bergamonti, T. De Kock, V. Cnudde, P.P. Lottici, A. Lorenzi, G. Predieri, E. Rabot, J. Teixeira, Multi-scale laboratory routine in the efficacy assessment of conservative products for natural stones, *MethodsX.* 5 (2018) 1095–1101. doi:10.1016/j.mex.2018.08.013.
- [22] V. Cnudde, M.N. Boone, High-resolution X-ray computed tomography in geosciences: A review of the current technology and applications, *Earth-Science Rev.* 123 (2013) 1–17. doi:10.1016/j.earscirev.2013.04.003.
- [23] V. Cnudde, A. Cwirzen, B. Masschaele, P.J.S. Jacobs, Porosity and microstructure

- characterization of building stones and concretes, *Eng. Geol.* 103 (2009) 76–83. doi:10.1016/j.enggeo.2008.06.014.
- [24] N. Marinoni, M. Voltolini, L. Mancini, P. Vignola, A. Pagani, A. Pavese, An investigation of mortars affected by alkali-silica reaction by X-ray synchrotron microtomography: a preliminary study, *J. Mater. Sci.* 44 (2009) 5815–5823. doi:10.1007/s10853-009-3817-9.
- [25] M. Voltolini, N. Marinoni, L. Mancini, Synchrotron X-ray computed microtomography investigation of a mortar affected by alkali-silica reaction: a quantitative characterization of its microstructural features, *J. Mater. Sci.* 46 (2011) 6633–6641. doi:10.1007/s10853-011-5614-5.
- [26] N. Marinoni, M. Voltolini, M.A.T.M. Broekmans, L. Mancini, P.J.M. Monteiro, N. Rotiroti, E. Ferrari, A. Bernasconi, A combined synchrotron radiation micro computed tomography and micro X-ray diffraction study on deleterious alkali-silica reaction, *J. Mater. Sci.* 50 (2015) 7985–7997. doi:10.1007/s10853-015-9364-7.
- [27] V. Cnudde, P.J.S. Jacobs, Monitoring of weathering and conservation of building materials through non-destructive X-ray computed microtomography, *Environ. Geol.* 46 (2004) 477–485. doi:10.1007/s00254-004-1049-5.
- [28] V. Cnudde, T. De Kock, M. Boone, W. De Boever, T. Bultreys, J. Van Stappen, D. Vandevorde, J. Dewanckele, H. Derluyn, V. Cárdenes, L. Van Hoorebeke, Conservation studies of cultural heritage: X-ray imaging of dynamic processes in building materials, *Eur. J. Mineral.* 27 (2015) 269–278. doi:10.1127/ejm/2015/0027-2444.
- [29] S. Bugani, M. Camaiti, L. Morselli, E. Van de Casteele, K. Janssens, Investigation on porosity changes of Lecce stone due to conservation treatments by means of x-ray nano- and improved micro-computed tomography: preliminary results, *X-Ray Spectrom.* 36 (2007) 316–320. doi:10.1002/xrs.976.
- [30] V. Cnudde, J.-P. Cnudde, C. Dupuis, P.J.S. Jacobs, X-ray micro-CT used for the localization of water repellents and consolidants inside natural building stones, *Mater. Charact.* 53 (2004) 259–271. doi:10.1016/j.matchar.2004.08.011.
- [31] S. Bugani, M. Camaiti, L. Morselli, E. Van de Casteele, K. Janssens, Investigating morphological changes in treated vs. untreated stone building materials by x-ray micro-CT, *Anal. Bioanal. Chem.* 391 (2008) 1343–50. doi:10.1007/s00216-008-1946-7.
- [32] M. Slavíková, F. Krejčí, J. Žemlička, M. Pech, P. Kotlík, J. Jakůbek, X-ray radiography and tomography for monitoring the penetration depth of consolidants in Opuka – the building stone of Prague monuments, *J. Cult. Herit.* 13 (2012) 357–364. doi:10.1016/j.culher.2012.01.010.
- [33] M. Parisatto, A. Turina, G. Cruciani, L. Mancini, L. Peruzzo, B. Cesare, Three-dimensional distribution of primary melt inclusions in garnets by X-ray microtomography, *Am. Mineral.* 103 (2018) 911–926. doi:10.2138/am-2018-6216CCBYNCND.
- [34] M.F. La Russa, G. Barone, C.M. Belfiore, P. Mazzoleni, A. Pezzino, Application of protective products to “Noto” calcarenite (south-eastern Sicily): a case study for the conservation of stone materials, *Environ. Earth Sci.* 62 (2011) 1263–1272. doi:10.1007/s12665-010-0614-3.
- [35] G. Alessandrini, A. Bocci, R. Bugini, D. Emmi, R. Peruzzi, M. Realini, Stone materials of Noto (Siracusa) and their decay, in: *7th Int. Congr. Deterior. Conserv. Stone*, 1993: pp. 11–20.
- [36] C. Urzi, M. Realini, Colour changes of Noto calcareous sandstone as related to its colonisation by microorganisms, *Int. Biodeterior. Biodegradation.* 42 (1998) 45–54.

- doi:10.1016/S0964-8305(98)00045-6.
- [37] G. Barbera, G. Barone, V. Crupi, F. Longo, G. Maisano, D. Majolino, P. Mazzoleni, S. Raneri, J. Teixeira, V. Venuti, A multi-technique approach for the determination of the porous structure of building stone, *Eur. J. Mineral.* 26 (2014) 189–198. doi:10.1127/0935-1221/2014/0026-2355.
- [38] G. Barone, V. Crupi, F. Longo, D. Majolino, P. Mazzoleni, S. Raneri, J. Teixeira, V. Venuti, Neutron radiography for the characterization of porous structure in degraded building stones, *J. Instrum.* 9 (2014). doi:10.1088/1748-0221/9/05/C05024.
- [39] R. Peruzzi, T. Poli, L. Toniolo, The experimental test for the evaluation of protective treatments: a critical survey of the “capillary absorption index,” *J. Cult. Herit.* 4 (2003) 251–254. doi:10.1016/S1296-2074(03)00050-5.
- [40] K.S.W. et al. Sing, Reporting physisorption data for gas/solid systems with special reference to the determination of surface area and porosity (Recommendations 1984), *Pure Appl. Chem.* 57 (1985) 603–619. doi:10.1351/pac198557040603.
- [41] J. Rouquerol, D. Avnir, C.W. Fairbridge, D.H. Everett, J.M. Haynes, N. Pernicone, J.D.F. Ramsay, K.S.W. Sing, K.K. Unger, Recommendations for the characterization of porous solids (Technical Report), *Pure Appl. Chem.* 66 (1994) 1739–1758. doi:10.1351/pac199466081739.
- [42] F. Brun, L. Massimi, M. Fratini, D. Dreossi, F. Billé, A. Accardo, R. Pugliese, A. Cedola, SYRMEP Tomo Project: a graphical user interface for customizing CT reconstruction workflows, *Adv. Struct. Chem. Imaging.* 3 (2017) 4. doi:10.1186/s40679-016-0036-8.
- [43] E. Larsson, Quantitative Analysis of Bone Tissue Engineering Scaffolds and Skull Bones by means of Synchrotron and Conventional X-ray Computed Microtomography Quantitative Analysis of Bone Tissue Engineering Scaffolds and Skull Bones by means of Synchrotron and Conve, Linköping University, 2010.
- [44] M.D. Abramoff, P.J. Magalhães, S.J. Ram, Image processing with ImageJ, *Biophotonics Int.* 11 (2004) 36–42.
- [45] J. Schindelin, I. Arganda-Carreras, E. Frise, V. Kaynig, M. Longair, T. Pietzsch, S. Preibisch, C. Rueden, S. Saalfeld, B. Schmid, J.-Y. Tinevez, D.J. White, V. Hartenstein, K. Eliceiri, P. Tomancak, A. Cardona, Fiji: an open-source platform for biological-image analysis, *Nat. Methods.* 9 (2012) 676–682. doi:10.1038/nmeth.2019.
- [46] F. Brun, L. Mancini, P. Kasae, S. Favretto, D. Dreossi, G. Tromba, Pore3D: A software library for quantitative analysis of porous media, *Nucl. Instruments Methods Phys. Res. Sect. A Accel. Spectrometers, Detect. Assoc. Equip.* 615 (2010) 326–332. doi:10.1016/j.nima.2010.02.063.
- [47] M. Voltolini, D. Zandomenighi, L. Mancini, M. Polacci, Texture analysis of volcanic rock samples: Quantitative study of crystals and vesicles shape preferred orientation from X-ray microtomography data, *J. Volcanol. Geotherm. Res.* 202 (2011) 83–95. doi:10.1016/J.JVOLGEORES.2011.02.003.
- [48] F. Brun, Development of algorithms and methods for three-dimensional image analysis and biomedical applications, Università degli Studi di Trieste, 2011.
- [49] I.M. Gitman, H. Askes, L.J. Sluys, Representative volume: Existence and size determination, *Eng. Fract. Mech.* 74 (2007) 2518–2534. doi:10.1016/J.ENGFRACMECH.2006.12.021.
- [50] M.S. Costanza-Robinson, B.D. Estabrook, D.F. Fouhey, Representative elementary volume estimation for porosity, moisture saturation, and air-water interfacial areas in unsaturated porous media: Data quality implications, *Water Resour. Res.* 47 (2011) 2893–900. doi:10.1029/2010WR009655.
- [51] M. Zambrano, E. Tondi, L. Mancini, F. Arzilli, G. Lanzafame, M. Materazzi, S.

- Torrieri, 3D Pore-network quantitative analysis in deformed carbonate grainstones, *Mar. Pet. Geol.* 82 (2017) 251–264. doi:10.1016/j.marpetgeo.2017.02.001.
- [52] D. Zhang, R. Zhang, S. Chen, W.E. Soll, Pore scale study of flow in porous media: Scale dependency, REV, and statistical REV, *Geophys. Res. Lett.* 27 (2000) 1195–1198. doi:10.1029/1999GL011101.
- [53] F. Brun, D. Dreossi, Efficient curve-skeleton computation for the analysis of biomedical 3D images, *Biomed. Sci. Instrum.* 46 (2010) 475–480.