

Electronic structure and spin-to-charge conversion in the chalcopyrite CdGeAs₂

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Ternary semiconductors with chalcopyrite structure are of growing interest for electronic, energy-conversion, and spintronic applications. Using angle-resolved photoemission spectroscopy, we directly map the band structure of CdGeAs₂, the prototypical chalcopyrite described by a modified Kane model that predicts the coexistence of flat bands and highly dispersive linear states. The combined effect of tetragonal distortion and broken inversion symmetry reduces the band degeneracy, allowing us to resolve three distinct states at the top of the valence band, with band velocities comparable to those reported in Dirac semimetals. We further probe the spin-to-charge conversion properties of CdGeAs₂ by optically injecting spin-polarized carriers and detecting the resulting inverse spin Hall effect (ISHE). The photon-energy dependence of the ISHE signal and theoretical calculations of the optically injected spin polarization allow us to identify the specific valence-to-conduction transitions responsible for net spin accumulation and to estimate the spin diffusion length. These results demonstrate that chalcopyrite semiconductors provide a versatile platform for optospintronics.

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I. INTRODUCTION

The family of chalcopyrite ternary compounds ABC₂ comprises more than 50 semiconductors with highly tunable crystal and electronic structures, giving rise to a wide variety of physical properties [1–5]. Over the years, chalcopyrites have been widely studied for their large photovoltaic conversion efficiency [6,7], high thermoelectric performance [4], and bulk photovoltaic effect [8], making them a unique platform for multifunctional energy conversion [9]. Structurally, they can be described as distorted zinc-blende crystals in which the tetragonal crystal field lifts the zone-center degeneracy between the heavy- and light-hole bands. This effect can be exploited to generate photoelectrons with spin polarization approaching 100% [10].

The coexistence of bands with very different effective masses underlies many of these intriguing properties. In par-

ticular, the light-hole band exhibits linear dispersion and high carrier mobilities. Figure 1(a) illustrates this distinctive feature through a solution of the Kildal model, an extension of the Kane Hamiltonian [11] that incorporates the anisotropic crystal field to describe the low-energy states near the band gap [12]. In chalcopyrites, Kane electrons can emerge as three-dimensional massless charge carriers originating from a nearly vanishing band gap, where linearly dispersing states (in blue-green in Fig. 1) intersect a flat heavy-hole band (pink) near the Γ point [13,14]. The band degeneracy can be tuned by hydrostatic pressure [15] or by chemical composition, with the gap-closing point marking the boundary between a trivial semiconductor and a three-dimensional topological insulator [2]. Beyond its electronic structure, CdGeAs₂ is notable for its nonlinear optical properties [16]. Its broad transparency window (2.4–18 μm) combined with a large nonlinear optical coefficient [17,18] makes it an attractive material for midinfrared frequency conversion [19,20].

In this work, we present an angle-resolved photoemission spectroscopy (ARPES) study of the electronic structure of CdGeAs₂, the archetypal chalcopyrite originally modeled by Kildal [12]. We resolve three distinct states forming the top of the valence band: two with linear dispersion, displaying band velocities of $\sim 1.3 \times 10^6$ and $\sim 0.5 \times 10^6$ m/s, and a third, flatter band well described by a parabolic dispersion with an effective mass of $\sim 1.1m_e$ (with m_e the free-electron mass). The bulk inversion asymmetry is expected to lift the

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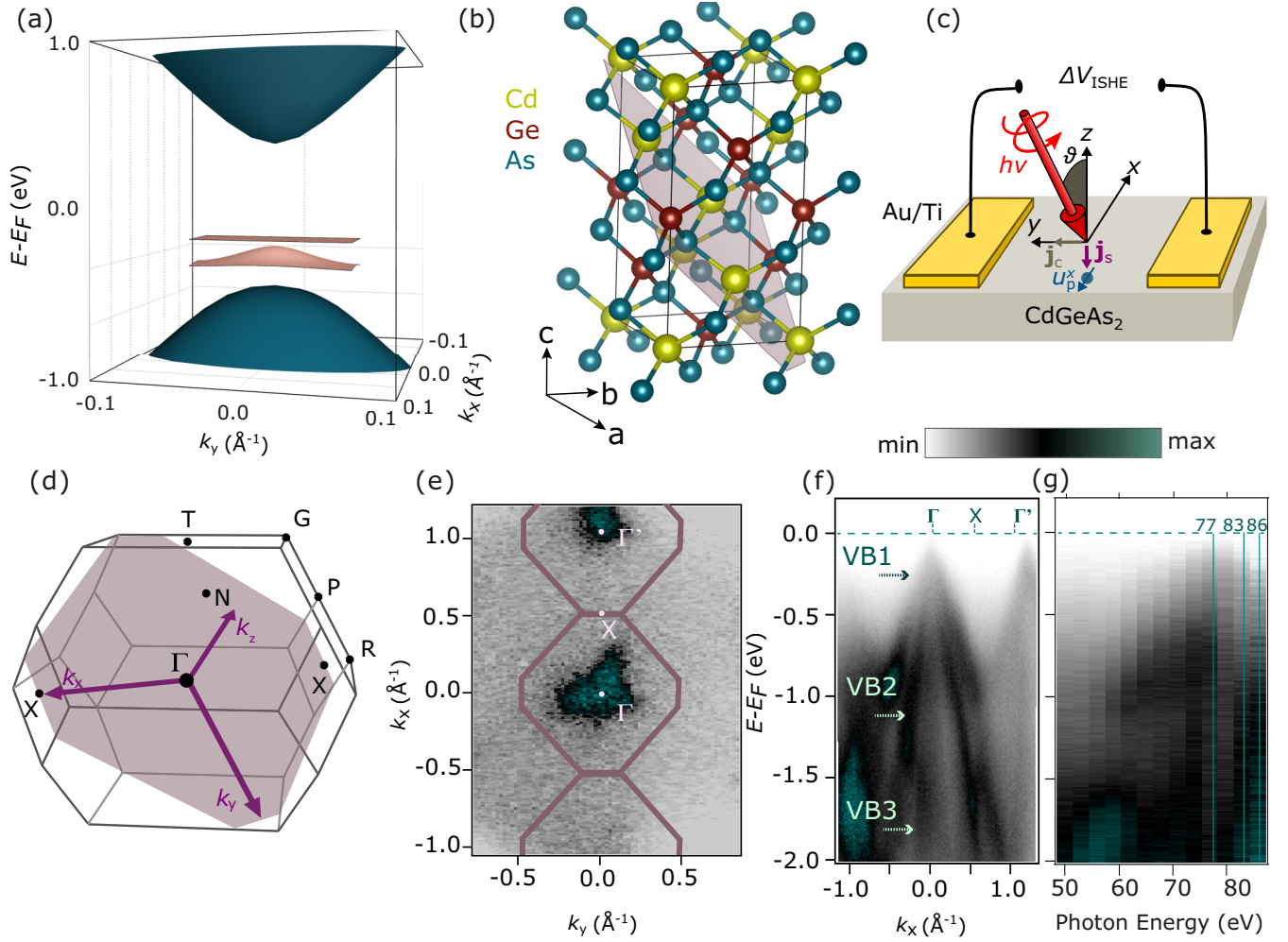


FIG. 1. (a) Schematic band dispersions near the fundamental gap of a chalcopyrite, obtained from the Kildal model. Pink and blue-green colors indicate flat and dispersive states, respectively. (b) Crystal structure of CdGeAs₂ with Cd (yellow), Ge (red), and As (blue-green) with diamondlike coordination. Black line traces the conventional tetragonal cell and the red area highlights the intersection with a plane parallel to the surface termination. (c) Sketch of the ISHE geometry, with two Au/Ti ohmic pads deposited on top of a (4×2) -mm²-wide and 1-mm-thick CdGeAs₂ sample; circularly polarized light beam illuminates the sample at polar angle ϑ with respect to the sample normal in the xz plane. u_p^x is the detected x -axis component of the spin polarization unit vector, $\mathbf{j}_s$ the spin current density, and $\mathbf{j}_c$ the charge current density. (d) Bulk Brillouin zone corresponding to the body-centered tetragonal primitive cell; labels indicate the high-symmetry points along with the convention adopted in the paper to indicate (k_x, k_y, k_z) . (e) Constant energy map acquired at $E - E_F = -200$ meV with 72.5 eV photon energy. The Γ , X, and Γ' points are shown along with the BZ for $k_z = 0$ $\text{\AA}^{-1}$, corresponding to the red plane shown in panel (d). (f) Band dispersion measured at 72.5 eV along k_x ; the three bands forming the highest valence manifold are labeled VB1, VB2, and VB3, with irreducible band representation Γ_7 , Γ_6 , and Γ_7 . (g) ARPES image made by energy distribution curves collected at Γ for photon energies between 50 and 86 eV.

spin degeneracy of the bands near the Γ point; we therefore investigate how this unique spin-polarized electronic structure influences the spin-to-charge interconversion properties by measuring the photon-energy dependence of the inverse spin Hall effect (ISHE) signal, which originates from spin-dependent scattering of optically injected spins in CdGeAs₂. Comparison with theoretical models of electrons spin polarization as a function of photon energy suggests that the ISHE spectrum can be captured by a simple diffusion model that accounts for the photon-energy dependence of the spin-injection rate. Taken together, the results establish CdGeAs₂ as a promising semiconductor platform for optospintronics applications.

II. EXPERIMENTAL DETAILS

High-quality CdGeAs₂ single crystals are grown by chemical vapor transport using bromine as the transport agent, a method known to yield large crack-free crystals [21]. Polycrystalline CdGeAs₂ is first synthesized by solid-state reaction: stoichiometric amounts of 4N purity Cd (chunk), Ge (slug), and As (slug) are sealed under high vacuum in a carbon-coated quartz ampoule. The mixture is heated at 550 °C and 650 °C for 24 h, with intermediate grinding in an argon-filled glovebox. For crystal growth, the powders are mixed with 2 $\mu\text{l}/\text{cm}^3$ of liquid bromine and sealed in a 40-cm-long quartz ampoule at an internal pressure of $\sim 10^{-1}$ Pa. The charge and growth ends of the ampoule are placed in

a horizontal two-zone furnace held at 675 °C and 650 °C, respectively, for 200 h. After growth, the furnace is cooled to room temperature at 2 °C/min, and single crystals are collected from the growth end of the ampoule.

Like other ternary chalcopyrites, CdGeAs₂ crystallizes in space group *I42d* (No. 122), with body-centered tetragonal symmetry and lattice parameters $a = 5.94$ Å and $c = 11.21$ Å, giving a tetragonal distortion $c/a = 1.89$ [21]. Figure 1(b) shows the conventional tetragonal cell comprising four formula units: Cd (yellow) and Ge (red) lie on the four-fold axis, while As (blue-green) sits on the twofold axis. The structure is diamondlike, with atoms adopting sp^3 hybridization and tetrahedral coordination: each Cd and Ge atom is bonded to four As atoms, and each As atom is coordinated by two Cd and two Ge cations [22].

ARPES measurements are performed at the APE-LE beamline of the Elettra synchrotron (Trieste), using a Scienta DA30 electron analyzer equipped with electrostatic deflecting lenses to acquire angular maps without moving the sample. Linear horizontal and vertical polarizations are used in the photon-energy range of 50–86 eV to probe the three-dimensional dispersion of bulk bands. The angular resolution is 0.5° and the combined energy resolution (beamline+analyzer) is 30 meV. Samples are cooled to 130 K, providing a good compromise between enhanced spectral quality and minimal charging effects. Thermal and electrical contact is ensured with conductive silver epoxy. The zero of the energy scale is referenced to the Fermi level (E_F) measured on polycrystalline silver in electrical contact with the sample.

The spin-to-charge conversion properties of CdGeAs₂ are studied using optical orientation [23–25], a technique in which circularly polarized light excites spin-polarized electrons in the conduction band through dipole-allowed optical transitions. As the injected spins diffuse, they undergo spin-dependent scattering, generating an electromotive field through the inverse spin Hall effect (ISHE) [26]. In this process, the spin current density $\mathbf{j}_s$ is converted into a transverse charge current $\mathbf{j}_c$ according to

$$\mathbf{j}_c = \gamma \mathbf{j}_s \times \mathbf{u}_p, \quad (1)$$

where γ is the spin Hall angle, quantifying the efficiency of the ISHE, and $\mathbf{u}_p$ is the unit vector of the injected degree of spin polarization vector $\mathbf{P}$. The ISHE voltage ΔV_{ISHE} is measured across two Au(200 nm)/Ti(7 nm) electrodes evaporated at the edges of a $4 \times 2 \times 1$ mm³ CdGeAs₂ sample [Fig. 1(c)]. The excitation source is a monochromatized supercontinuum laser (SuperK FIANIUM FIR-20, NKT Photonics) covering the 0.65–1.15 eV photon-energy range with a typical bandwidth of ~ 10 meV. A double-modulation scheme is employed: the circular polarization of the light is modulated at 50 kHz by a photoelastic modulator (PEM), while the beam intensity is modulated at 23 Hz by a mechanical chopper. The laser beam is focused onto the sample at a polar angle ϑ with respect to the sample normal in the xz plane [Fig. 1(c)], using an off-axis configuration with a 0.65 numerical-aperture objective [27,28]. The optically generated spin current $\mathbf{j}_s$ propagates along the z axis [27], while the ISHE-induced voltage drop ΔV_{ISHE} is measured along y across the Au/Ti contacts. Under these conditions, only the x -axis component of $\mathbf{P}$ satisfies the ISHE geometry of Eq. (1) and can be detected. The

signal is demodulated using two lock-in amplifiers in cascade, tuned to the PEM and chopper frequencies, respectively. All ISHE measurements are performed at room temperature.

III. RESULTS AND DISCUSSION

ARPES requires atomically clean surfaces, obtained by postcleavage in ultrahigh vacuum. The crystal structure of CdGeAs₂ consists of As and Cd-Ge layers alternating along the [100] and [001] directions of the conventional cell, and it does not exhibit a single preferential cleavage plane. Crystals are generally prismatic and elongated along [111], naturally exposing optically smooth (112), (101), and (011) faces [21]. By fracturing more than 20 crystals, we observed band dispersion only from the (112) termination, with a success rate of $\sim 20\%$.

In reciprocal space, the periodicity is more conveniently described in terms of the body-centered tetragonal unit cell, which has half the volume of the conventional cell, i.e., two formula units. The primitive lattice vectors are $\mathbf{a}_1 = (a/2, -a/2, c/2)$, $\mathbf{a}_2 = (a/2, a/2, c/2)$, and $\mathbf{a}_3 = (-a/2, -a/2, c/2)$. Figure 1(d) shows the corresponding Brillouin zone (BZ); the colored area marks the plane parallel to the surface termination. Labels denote the high-symmetry points as well as the notation adopted in this work for the three components of the electron wave vector. We note that k_y and k_z are parallel to low-symmetry directions, whereas k_x is parallel to ΓX . Figure 1(e) displays a constant-energy map at $E - E_F = -200$ meV measured with 72.5 eV photons. The valence-band maxima form pockets centered at Γ and Γ' , confirming the sample alignment. Strong matrix element effects are responsible for the lack of spectral weight in the Brillouin zone at negative k_x values.

Figure 1(f) shows the band dispersion along k_x at 72.5 eV photon energy. Three distinct states are resolved at the top of the valence-band manifold. No evidence of an inverted band gap is found, consistent with hybrid functional calculations that include electronic correlations beyond the local density approximation [29]. In contrast, local-density-based calculations incorrectly predict a topological insulating phase [30]. The lower edge of the gap (VB1, irreducible representation Γ_7) corresponds to a singlet state that is nearly degenerate and may accidentally intersect with the heavy-hole band (VB2, Γ_6), owing to their different irreducible representations [31]. Experimentally, we confirm the splitting between VB2 and the light-hole band (VB3, Γ_7), induced by the tetragonal crystal field. The splitting of the spin degeneracy under the breaking of inversion symmetry cannot be fully resolved because of band broadening (see, e.g., the arrow at VB2 for negative k_x). This broadening is not limited by energy resolution but arises from k_z integration due to the surface sensitivity of ARPES and the bulk character of the bands. The dispersion of the bands in the k_z direction, orthogonal to the sample surface, is illustrated in Fig. 1(g), which shows energy distribution curves integrated at Γ as a function of the incoming photon energy. We observe the evolution of the upper valence band (VB1), which exhibits a clear parabolic behavior, reaching its maximum for photon energies in the 77–86 eV range. For a value of the inner potential $V_0 = 10$ eV, these energies fall close to the bulk Γ point at $k_z = 4.7$ Å⁻¹ [32].

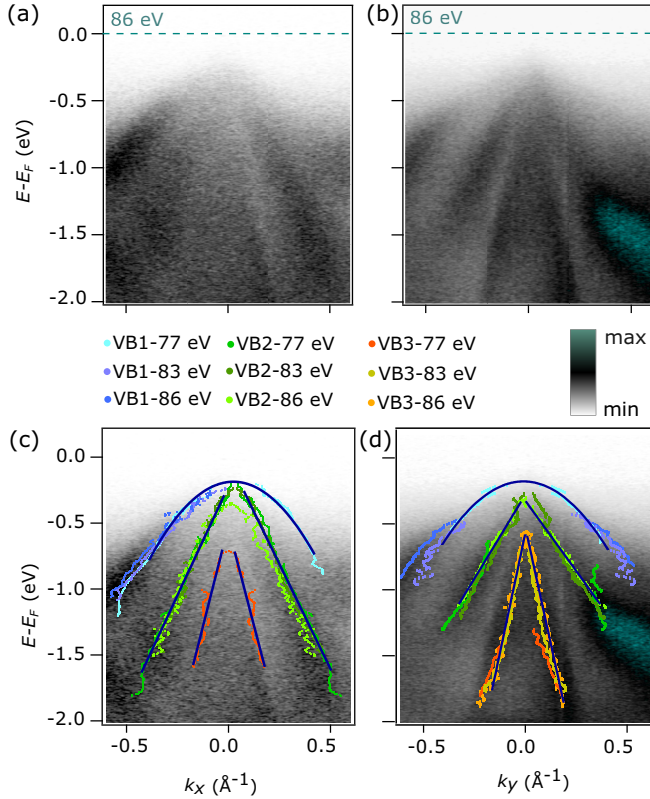


FIG. 2. (a) and (b) Band structure measured with a photon energy of 86 eV along k_x and k_y , respectively. (c) and (d) Same band dispersions with colored markers to indicate the position of the peaks extracted from the analysis of the momentum distribution curves (MDCs) integrated within a window of 25 meV between -1.75 and -0.25 eV. Different colors correspond to the dataset at 77, 83, and 86 eV. The position of the bands is obtained from a fit of the MDC with multiple Lorentzian functions and a polynomial background. Dark-blue lines indicate the best fit of the peaks dispersion: VB1 is well accounted for by a parabolic dispersion, whereas VB2 and VB3 exhibit linear dispersion with large band velocities, comparable to those reported in graphene and in Dirac semimetal candidates.

Figures 2(a) and 2(b) display dispersions along k_x and k_y , respectively, measured at 86 eV photon energy. To quantify the band dispersion, we extract momentum distribution curves (MDCs) integrated within a 25 meV window between $E - E_F = -1.75$ and -0.25 eV. Each MDC is fitted with a model including a variable number of Lorentzian peaks on top of a quadratic background, and markers in Fig. 2 report the central position of each peak. The same analysis is repeated for photon energies of 77 and 83 eV with the results shown in Figs. 2(c) and 2(d). Markers of different colors denote VB1, VB2, and VB3 for the different photon energies along k_x [Fig. 2(c)] and k_y [Fig. 2(d)]. The near-overlap of markers at different photon energies indicates that the valence bands exhibit only weak out-of-plane dispersion in this energy window, in agreement with Fig. 1(g). Dark-blue lines indicate the best fit of the peaks dispersion.

Both VB2 and VB3 display nearly linear dispersion over an energy range exceeding 1 eV, whereas VB1 is significantly flatter and well described by a parabolic dispersion. A linear

fit yields velocities for VB3 ranging from $\sim 0.9 \times 10^6$ m/s along k_x to $\sim 1.3 \times 10^6$ m/s along k_y . For VB2, the velocities are about a factor of 2 smaller, $\sim 0.5 \times 10^6$ m/s along both k_x and k_y . These values are large and comparable to those reported in graphene [33] and in Dirac semimetals such as Cd_3As_2 [34,35], Na_3Bi [36], and ZrTe_5 [37,38]. In contrast, VB1 yields effective masses of $\sim 1.09m_e$ and $\sim 1.06m_e$ along k_x and k_y , respectively. The close agreement of velocities and masses along the two directions highlights the isotropic character of the valence band on the investigated cleave plane.

The characterization of the band structure by ARPES provides crucial information about the electronic states and their parameters, key to understanding the spin-to-charge conversion in CdGeAs_2 , investigated here through optical spin injection and detection of the ISHE. In the investigated sample [Fig. 1(c)], the x and y axes form an angle $\eta \simeq 37^\circ$ with respect to the crystallographic directions $[110]$ and $[c/a, c/a, -a/c]$, expressed in the basis of the direct lattice vectors of the conventional cell [Fig. 1(b)]. The z axis is instead parallel to the $[112]$ direction. As a first step, we verified the consistency of the ISHE signal by measuring its dependence on the polar angle ϑ [Fig. 3(a)], the PEM retardation R_{PEM} in units of the wavelength λ [Fig. 3(b)], and the incident optical power W [Fig. 3(c)], for photon energy $h\nu = 0.8$ eV. In Fig. 3(a), the ΔV_{ISHE} normalized signal is reported as a function of the incidence angle ϑ . This curve is compared with the spin-injection rate $\dot{S}$ generated and detected in our geometry. The latter is evaluated modeling the band structure with an eight-band $\mathbf{k} \cdot \mathbf{p}$ Hamiltonian (details in Appendix A). The signal behavior as a function of ϑ is nicely captured by the model. Figure 3(b) shows the ISHE signal as a function of R_{PEM} , which modulates the degree of circular polarization of the incident beam. The data follow the first-order Bessel function $J_1(R_{\text{PEM}})$ with a maximum near $R_{\text{PEM}} \approx 0.3\lambda$, consistent with the fact that the PEM retardation determines the degree of circular polarization [25]. Finally, Fig. 3(c) displays ΔV_{ISHE} as a function of the incident optical power W , showing a linear dependence that reflects the proportionality between injected spin-polarized carriers and incident photon flux. These tests confirm the spin-related origin of the detected voltage.

The photon-energy dependence of ΔV_{ISHE} , normalized to photon flux Φ in the 0.65–1.15 eV photon energy range, is presented in Fig. 4 for $R_{\text{PEM}} = 0.3\lambda$ and $\vartheta = -27^\circ$. The latter corresponds to an angle of $\vartheta_{\text{in}} \approx -8.5^\circ$ inside CdGeAs_2 whose refractive index is $n \approx 3$ [39]. The photon flux is $\Phi = W/[\pi(\mathcal{D}/2)^2 h\nu]$, where $\mathcal{D}$ is the spot diameter on the sample ($\approx 10 \mu\text{m}$) and W varies within 50 and 1500 μW in the explored photon-energy range. A pronounced peak is observed at $h\nu \approx 0.7$ eV, followed by an almost constant signal up to $h\nu \approx 1.15$ eV. The ISHE spectrum is governed by three parameters: the light absorption coefficient α , the degree of spin polarization P , and the spin diffusion length L_s [27]. Since the value of L_s for CdGeAs_2 has not yet been established, while α and P can be directly evaluated from the electronic band structure, in the following we present how to use the ISHE spectrum to gain insight into L_s . To estimate α and P , we have calculated from the eight-band $\mathbf{k} \cdot \mathbf{p}$ model the carrier-injection rate $\dot{n}$ and $\dot{S}$ as functions of the photon energy [40–42] (see Appendix A). The results obtained for the experimental ISHE geometry are presented

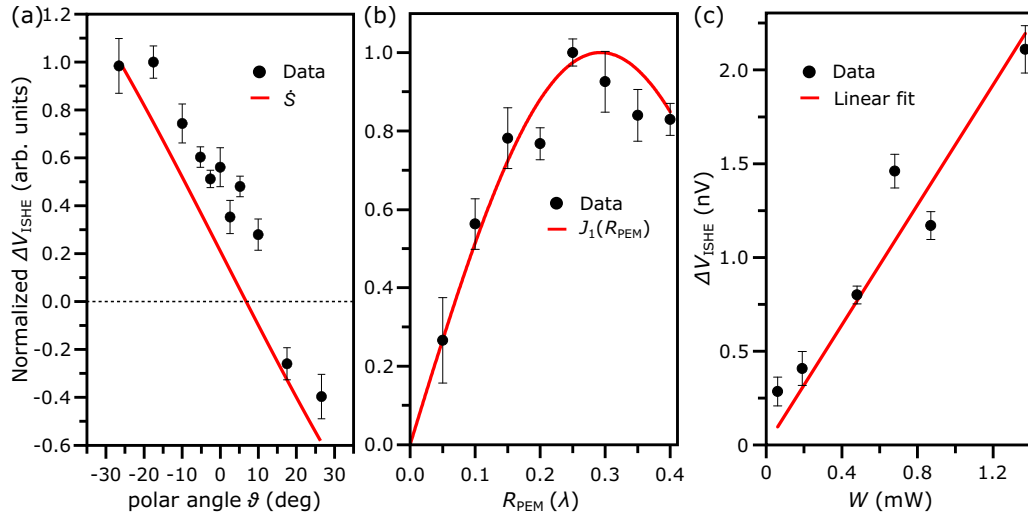


FIG. 3. (a) ΔV_{ISHE} signal normalized to its maximum value as a function of the polar angle ϑ , for $h\nu = 0.8$ eV, $R_{\text{PEM}} = 0.3\lambda$, and $W = 1.37$ mW. This is compared with the spin-injection rate $\hat{S}$ in Eq. (A2) corresponding to the solid red line, estimated from the eight-band $\mathbf{k} \cdot \mathbf{p}$ model for the geometry of Fig. 1(c). (b) Dependence of ΔV_{ISHE} upon the PEM retardation R_{PEM} , for $h\nu = 0.8$ eV, $\vartheta = -27^\circ$, and $W = 1.37$ mW. The solid red line represents the Bessel function of the first order $J_1(R_{\text{PEM}})$, which describes the dependence of the light circular polarization upon the PEM retardation R_{PEM} . (c) ΔV_{ISHE} as a function of the light incident power W , for $h\nu = 0.8$ eV, $R_{\text{PEM}} = 0.3\lambda$, and $\vartheta = -27^\circ$. The straight red line represents a linear fit of the data.

in Figs. 5(a) and 5(b). Then P is derived according to the definition $P = \hat{S}/\hbar$ [40,41], while the absorption coefficient α is related to the carrier injection rate as $\alpha = \hbar\nu/(2nc\varepsilon_0)$, with c being the light velocity and ε_0 the vacuum permittivity [43]. The spectral dependence of the calculated α and P values are reported in Figs. 5(c) and 5(d), respectively. Within a one-dimensional spin diffusion model for optically injected carriers (see Appendix B for the derivation) and assuming the spin Hall angle γ as a constant, the normalized ISHE signal follows:

$$\frac{\Delta V_{\text{ISHE}}}{\Phi} \propto \frac{P\alpha L_s^2}{1 + \alpha L_s}. \quad (2)$$

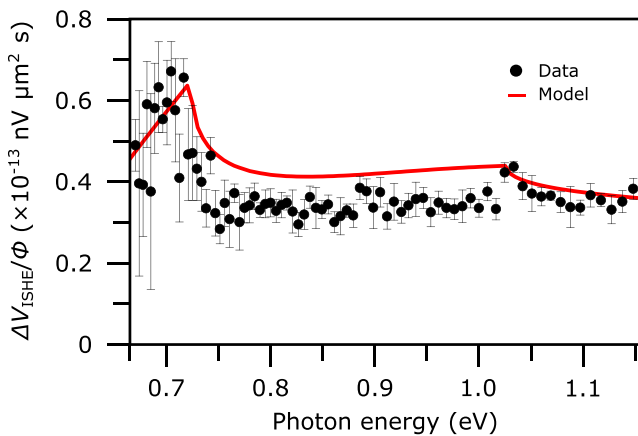


FIG. 4. Photon-energy dependence of ΔV_{ISHE} , normalized to the incident photon flux, for $\vartheta = -27^\circ$ and $R_{\text{PEM}} = 0.3\lambda$. The solid red line shows the spectral dependence obtained from the spin diffusion model described in the text.

At this point, we exploit the calculated parameters P and α to estimate the L_s value, assumed constant, which allows best reproducing the spectral dependence of the ISHE signal. The right side of Eq. (2) is shown in Fig. 5(e) for $L_s = 10$ μm (blue curve), 1 μm (gray), and 100 nm (orange). It is worth noting that the $L_s = 10$ μm curve is representative of the limit $L_s \gg \alpha^{-1}$ of Eq. (2), yielding $\Delta V_{\text{ISHE}} \propto PL_s$, while the $L_s = 100$ nm curve is representative of the opposite regime $L_s \ll \alpha^{-1}$, yielding $\Delta V_{\text{ISHE}} \propto P\alpha L_s^2$. In the latter case, since $P = \hat{S}/\hbar$ and $\alpha \propto \hbar$, we get $\Delta V_{\text{ISHE}} \propto \hat{S}L_s^2$. By comparing the (measured) ISHE spectrum in Fig. 4 and the (computed) $P\alpha L_s^2/(1 + \alpha L_s)$ in the gray shaded area of Fig. 5(e) we observe that the increase of the detected signal up to $h\nu \approx 0.7$ eV is reproduced only by the $L_s = 100$ nm curve. In contrast, the 10 μm curve exhibits a strong decrease in the 0.6–0.7 eV energy range, while the 1 μm remains roughly constant. For $h\nu > 0.7$ eV, all curves feature a sharp decrease due to the onset of transitions from VB2, which have spin polarization opposite to that of VB1 [see Fig. 5(d)]. Nevertheless, the decrease is less pronounced for the $L_s = 100$ nm curve, which, again, better mimics the experimental results (Fig. 4). At higher photon energies, the model for $L_s = 100$ nm predicts a gradual decrease of the signal, not observed experimentally. This discrepancy likely arises from the assumption of constant L_s and γ even when hot electrons are photogenerated well above the conduction-band minimum. Indeed, we already observed that when electrons are photogenerated with a photon energy several hundreds of meV larger than the direct gap, γ increases significantly in semiconductors [27,28,44], and this is commonly responsible for enhancing the ISHE signal with increasing photon energy [27,28]. The spin Hall angle in semiconductors empirically varies with photon energy as $\gamma(h\nu) \propto e^{C h\nu}$, where C is a phenomenological parameter. This behavior is observed both in Ge, with $C \approx 5$ [27], and in

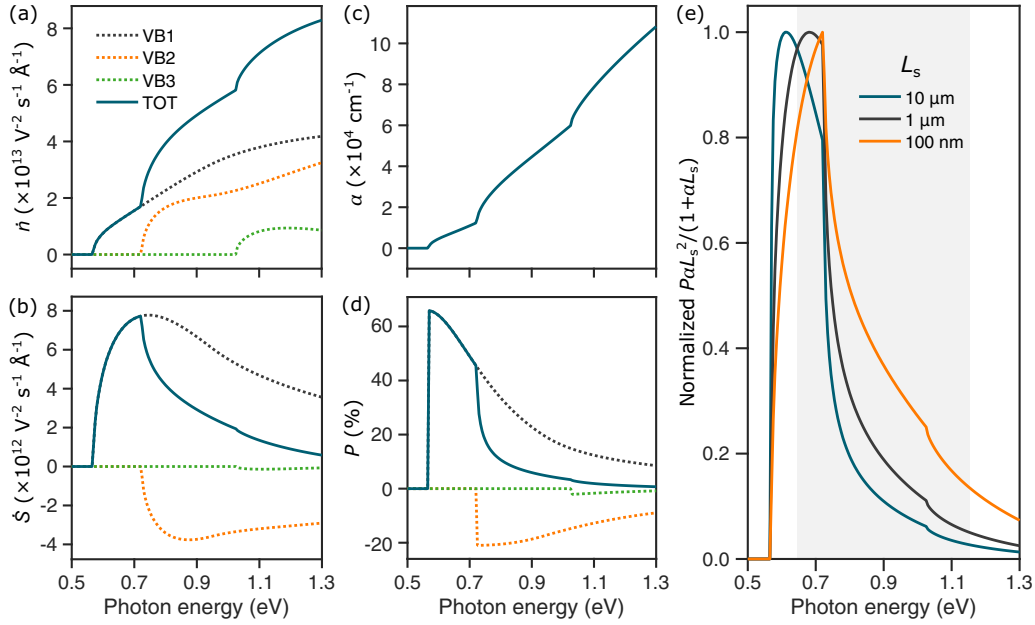


FIG. 5. (a) Carrier-injection rate $\dot{n}$, (b) spin-injection rate $\dot{S}$, (c) absorption coefficient α , and (d) degree of spin polarization P calculated from the $\mathbf{k} \cdot \mathbf{p}$ model described in Appendix A for direct optical transitions from VB1 (gray dashed line), VB2 (orange dashed line), and VB3 (green dashed line) to the conduction band. The blue line represents the total $\dot{n}$, $\dot{S}$, α , and P , as obtained from the sum of the individual contributions. (e) Photon-energy dependence of $PaL_s^2/(1+\alpha L_s)$ evaluated for $L_s = 10 \text{ } \mu\text{m}$ (blue line), $1 \text{ } \mu\text{m}$ (gray line), and 100 nm (orange line), with each curve normalized to the maximum. The gray area is the photon-energy range of the ISHE spectrum.

GaAs [44], where it is attributed to intervalley scattering of spin-polarized electrons from the Γ valley into the L valley. To account for a similar dependence of the spin Hall angle also in CdGeAs₂, we fit the ISHE spectrum using the results of the previous analysis and an exponential increase of the spin Hall angle with the photon energy. The best fitting parameter is $C \simeq 3.4$, yielding the ΔV_{ISHE} photon-energy dependence shown in Fig. 4, which nicely reproduces the whole spectrum and especially the nearly flat ISHE response above 0.8 eV. Furthermore, the model partially captures the small peak at $h\nu \approx 1.025 \text{ eV}$, which coincides with the absorption onset from VB3. These results point towards an exponential growth of the spin-to-charge conversion efficiency with photon energy also in CdGeAs₂. Although spin-polarized holes are optically injected together with spin-polarized electrons, their contribution is neglected in the discussion as the hole spin polarization is expected to vanish much faster than the electron one [45].

Overall, the analysis suggests $L_s \lesssim 100 \text{ nm}$ in CdGeAs₂, a value which is comparable to GaAs [46,47] but much smaller than Si and Ge where $L_s \sim 1 \text{ } \mu\text{m}$ [46,48–50]. This value is physically consistent with the electronic properties of CdGeAs₂, which is characterized by a strong spin-orbit coupling (SOC) and by the absence of bulk inversion symmetry [12,31]. As already established for GaAs [51], these two material-specific characteristics result in effective Elliott-Yafet and Dyakonov-Perel spin-relaxation mechanisms, which justify the small value of the spin diffusion length observed in the present study. In the $L_s \ll \alpha^{-1}$ regime applicable to CdGeAs₂, $\Delta V_{\text{ISHE}} \propto \dot{S} L_s^2$, so the small L_s strongly suppresses the ISHE amplitude. Nevertheless, the measured signal is higher than in Ge [27], suggesting a significantly larger γ value for thermalized electrons in CdGeAs₂

($\gamma \sim 10^{-4}$ in Ge [27]). The larger γ value is attributed to more effective spin-to-charge conversion mechanisms that scale with SOC [52]. A precise estimation of γ for CdGeAs₂ would require a precise estimation of L_s , which is beyond the goal of the present work. Finally, it is worth mentioning that a short spin diffusion length is the key ingredient to enable fast modulation of spin-dependent signals using high-frequency electric fields, which is promising for spin-based logic applications [47].

IV. CONCLUSIONS

In this work, we have reported an experimental investigation of the electronic band structure of the chalcopyrite semiconductor CdGeAs₂ using angle-resolved photoemission spectroscopy and ISHE. We resolved three distinct states forming the top of the valence band manifold. Two of them exhibit nearly linear dispersions, with velocities as high as $\sim 1.3 \times 10^6 \text{ m/s}$ (VB3) and $\sim 0.5 \times 10^6 \text{ m/s}$ (VB2), values that are comparable to those reported in graphene and Dirac semimetals such as Cd₃As₂, Na₃Bi, and ZrTe₅. The third state (VB1) is significantly flatter and well described by a parabolic dispersion with an effective mass of $\sim 1.1 m_e$. The close agreement of these parameters along the orthogonal in-plane direction highlights the nearly isotropic character of the valence band within the cleave plane. These results directly validate long-standing theoretical predictions based on the modified Kane model and establish CdGeAs₂ as an archetype for studying the coexistence of dispersive and flat bands in chalcopyrite semiconductors.

The band-structure parameters obtained from ARPES provide the basis for interpreting the spin-charge interconversion properties of CdGeAs₂, investigated by means of optical spin

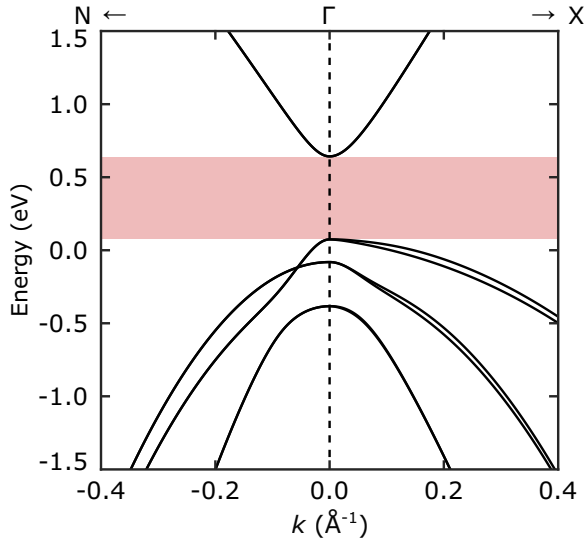


FIG. 6. Band structure of CdGeAs₂ around the Γ point of the Brillouin zone, calculated by means of an eight-band $\mathbf{k} \cdot \mathbf{p}$ model.

injection and detection of the ISHE. The ISHE signal exhibits a clear photon-energy dependence, with a pronounced maximum near $h\nu \approx 0.7$ eV followed by a plateau up to $h\nu \approx 1.15$ eV, in agreement with a model based on an eight-band $\mathbf{k} \cdot \mathbf{p}$ Hamiltonian. The model allowed us to compute carrier and spin-injection rates, $\dot{n}$ and $\dot{S}$, as well as the degree of spin polarization $P = \dot{S}/\dot{n}$ and the absorption coefficient α , under experimental conditions. The analysis shows that the normalized ISHE spectrum is mainly governed by VB1 $\rightarrow$ CB transitions up to 0.7 eV, where the onset of VB2 transitions produces a sharp drop of the signal. Comparison with a diffusion model further indicates that the measured voltage scales with $\dot{S}$, leading to $L_s \lesssim 100$ nm in CdGeAs₂.

By establishing CdGeAs₂ as a semiconductor hosting both high-velocity carriers, efficient optical spin injection and spin-to-charge conversion, this work highlights the potential of chalcopyrites as versatile materials for future optospintronics applications.

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DATA AVAILABILITY

The data that support the findings of this article are openly available [53].

APPENDIX A: EIGHT-BAND $\mathbf{k} \cdot \mathbf{p}$ MODEL

To analyze the ϑ -angle and photon-energy dependencies of the ISHE response, we employed an eight-band $\mathbf{k} \cdot \mathbf{p}$ model to compute the band structure (Fig. 6) and the carrier- and spin-injection rates [Figs. 5(a) and 5(b)] of optically oriented electrons in CdGeAs₂. The basis set includes the conduction- and valence-band states $|S \uparrow\rangle$, $|S \downarrow\rangle$, $|X \uparrow\rangle$, $|Y \uparrow\rangle$, $|Z \uparrow\rangle$, $|X \downarrow\rangle$, $|Y \downarrow\rangle$, and $|Z \downarrow\rangle$. Remote bands were neglected, since the optical orientation process involves only states near $\mathbf{k} = 0$, where the eight-band approximation is accurate. The Hamiltonian combines the 6×6 valence-band model of Limpijumng and Lambrecht [31], which includes linear and quadratic coupling terms, with the 8×8 model of Kildal [12] for the conduction band and conduction-valence coupling. The resulting coupling terms are consistent with those found in diamondlike semiconductors [54,55]. The Hamiltonian, excluding the free-particle kinetic energy, reads

$$\mathcal{H} = \begin{pmatrix} E_s & 0 & iPk_x & iPk_y & iPk_z & 0 & 0 & 0 \\ & E_s & 0 & 0 & 0 & iPk_x & iPk_y & iPk_z \\ & & d_1 & -i\Delta_{\parallel} & e_1 & 0 & 0 & \Delta_{\perp} \\ & & & d_2 & e_2 & 0 & 0 & -i\Delta_{\perp} \\ & & & & d_3 & -\Delta_{\perp} & i\Delta_{\perp} & 0 \\ & & & & & d_1 & i\Delta_{\parallel} & e_1 \\ & & & & & & d_2 & e_2 \\ & & & & & & & d_3 \end{pmatrix},$$

with:

$$\begin{aligned} d_1 &= (A_0 + A_2)k_x^2 + B_0k_y^2 + (B_0 + B_1 + A_1)k_z^2 + \Delta_c, \\ d_2 &= (A_0 + A_2)k_y^2 + B_0k_x^2 + (B_0 + B_1 + A_1)k_z^2 + \Delta_c, \\ d_3 &= (A_0 + A_1)k_z^2 + (B_0 + A_2)(k_x^2 + k_y^2), \\ e_1 &= C_0k_xk_z + iDk_y, \quad e_2 = C_0k_yk_z - iDk_x. \end{aligned}$$

The parameters $E_s, \Delta_c, \Delta_{\parallel}, \Delta_{\perp}, P, D, A_i, B_i, C_0$ correspond to the energy eigenvalues and spin-orbit splittings at Γ , and linear/quadratic coupling terms. The values were adjusted from Refs. [12] and [31] to account for both earlier reports and the ARPES data presented in this work. The complete parameter set is given in Table I.

Using this Hamiltonian, we computed the carrier-injection rate $\dot{n}$ and the spin-injection rate $\dot{S}$ as functions of the photon energy for the geometry of Fig. 1(c), following Refs. [40] and [41]. Calculations include only spin-dependent direct transitions, evaluated with the linear tetrahedron method [56] over the first Brillouin zone [57], in line with previous works [42,55]. In particular, we have calculated the matrix elements of the carrier-injection tensor ξ^{aa} and ξ^{cc} , and of the spin-injection pseudotensor ζ^{abc} and ζ^{cab} . Here, the superscripts refer to Cartesian directions along the axes of the conventional cell [Fig. 1(b)]. In tetragonal systems, the only three nonzero elements in the carrier-injection tensor are $\xi^{aa} = \xi^{bb}$ and ξ^{cc} , and the six nonzero coefficients in the spin-injection pseudotensor are $\zeta^{abc} = \zeta^{bca} = -\zeta^{acb} = -\zeta^{bac}$ and $\zeta^{cab} = -\zeta^{cba}$.

We then computed the spin-injection rate components $\dot{S}_i = \zeta^{ijk} E_j^* E_k$ and the carrier-injection rate $\dot{n} = \xi^{ij} E_i^* E_j$, where the Einstein summation convention over repeated indices is employed. In these expressions, i, j , and k are generic Cartesian directions and E_i is the component along the i th axis of the electric field of the impinging light. Considering the specific direction of the light wave vector used in the experiments, the carrier-injection rate normalized to the beam intensity can be calculated as

$$\dot{n} = \frac{1}{4} \left\{ 3\xi^{aa} + \xi^{cc} + \frac{\xi^{aa} - \xi^{cc}}{\gamma'^2} [\gamma'^2 \cos(2\vartheta_{\text{in}})] \right\}$$

TABLE I. Parameters employed in the eight-band $\mathbf{k} \cdot \mathbf{p}$ model. Note that with respect to Ref. [31] we set another parameter C_1 to zero.

Description	Parameter	Value
Eigenvalue at $k = 0$	E_s	0.6424 eV
Crystal-field splitting at $k = 0$	Δ_c	-0.195 eV
Spin-orbit coupling at $k = 0$	$\Delta_{\parallel}$	0.114 eV
	$\Delta_{\perp}$	0.119 eV
Linear coupling terms	P	6.840 eV Å
	D	0.252 eV Å
Quadratic coupling terms	A_0	-17.533 eV Å ²
	A_1	-2.523 eV Å ²
	A_2	-0.704 eV Å ²
	B_0	-6.238 eV Å ²
	B_1	-6.764 eV Å ²
	C_0	-18.610 eV Å ²

$$\begin{aligned} & -2a^2 \cos^2 \eta - 2a^2 \cos^2 \vartheta_{\text{in}} \sin^2 \eta + 2a^2 \sin^2 \vartheta_{\text{in}} \\ & - 2ac\sqrt{2} \sin \eta \sin(2\vartheta_{\text{in}}) \}. \end{aligned} \quad (\text{A1})$$

Furthermore, by considering that the ISHE geometry allows the detection of only the x -axis component of the spin polarization, the spin-injection rate of carriers producing the ISHE signal normalized to the beam intensity assumes the following expression:

$$\begin{aligned} \dot{S} &= \frac{i}{\gamma'^2} [ac\sqrt{2}(\zeta^{abc} - \zeta^{cab}) \cos \vartheta_{\text{in}} \sin \eta \\ &+ \gamma'^2 \zeta^{abc} \sin \vartheta_{\text{in}} + a^2(\zeta^{cab} - \zeta^{abc}) \sin \vartheta_{\text{in}} \sin^2 \eta]. \end{aligned} \quad (\text{A2})$$

Here, $\gamma' = \sqrt{2c^2 + a^2}$. Eq. (A2) is used to reproduce the ϑ -angle dependence of ΔV_{ISHE} [Fig. 3(a)], and both expressions are employed to compute the photon energy dependence of α and P [Figs. 5(c) and 5(d)]. It is worth noting that, unlike materials with cubic symmetry, the directions of the light wave vector and spin-polarization unit vector do not lie in general along the same axis, leading to a nonzero ISHE signal even at normal incidence on the sample surface, as shown in Fig. 3(a).

APPENDIX B: SPECTRAL DEPENDENCE OF ISHE SIGNAL

From Eq. (1), and considering the experimental configuration shown in Fig. 1(c), we obtain $j_c(z) = \gamma j_s^x(z)$, where $j_s^x(z)$ is the spin current density flowing along the z axis and polarized along the x axis of Fig. 1(c). Accordingly, the ISHE voltage drop can be expressed as [27]

$$\Delta V_{\text{ISHE}} = \gamma \langle j_s^x(z) \rangle_z \rho d, \quad (\text{B1})$$

where ρ is the electrical resistivity, d the distance between the electrodes, and $\langle j_s^x(z) \rangle_z$ denotes the spatial average of the spin current density along the out-of-plane direction, i.e., the component that contributes to the measurable signal across the electrodes. Within a one-dimensional spin diffusion model, the spin current satisfies

$$\frac{1}{D_e} \frac{\partial j_s^x(z)}{\partial z} = -\frac{s_x(z)}{L_s^2} + \frac{P\alpha\Phi e^{\alpha z}}{D_e}, \quad (\text{B2})$$

where $j_s^x(z) = -D_e \partial s_x(z) / \partial z$, $s_x(z)$ is the x -polarized spin density, and D_e is the electron diffusion coefficient [27]. Equation (B2) is solved under the boundary conditions $j_s^x(0, -t) = 0$, reflecting the absence of spin leakage through the sample surfaces at $z = 0$ and $z = -t$, $-t$ being the position of the bottom one. The average spin current density, $\langle j_s^x(z) \rangle_z$, is obtained by averaging $j_s^x(z)$ over the sample thickness t . In

the limit $t \gg L_s$, α^{-1} , it can be approximated as

$$\langle j_s^x(z) \rangle_z = \Phi \frac{P\alpha L_s^2}{t(1 + \alpha L_s)}. \quad (\text{B3})$$

Substituting Eq. (B3) into Eq. (B1), the spectral dependence of the normalized ISHE signal, reported in Fig. 4, can be interpreted as $\Delta V_{\text{ISHE}} / \Phi \propto P\alpha L_s^2 / (1 + \alpha L_s)$.

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