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2	Multiresolution decomposition and wavelet analysis of urban aerosol fluxes in
3	Italy and Austria
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19	Abstract
20	Observations of turbulent aerosol fluxes are fundamental to understand basic transport processes that
21	govern changes of particle concentrations in the atmospheric boundary layer. The turbulent surface-
22	atmosphere exchange of atmospheric particles can be quantified using several methods, including the
23	eddy-covariance (EC) method and spectral flux estimation methods such as wavelet analysis and
24	multiresolution decomposition. In this work, turbulent time series obtained by EC measurements in
25	two different cities, Lecce (Italy) and Innsbruck (Austria), are spectrally analysed applying wavelet
26	analysis and multiresolution decomposition, and the respective turbulent spectra are compared in
27	these two European cities to quantify the contributions to turbulent fluxes in both the time and the
28	frequency domains. As expected, particle emission is dominant in both cities following a similar
29	diurnal cycle. Multiresolution decomposition reveals a similar cospectral peak of particle fluxes in
30	both cities, with a median normalized frequency of $n = 0.087$ in Lecce and $n = 0.086$ in Innsbruck.
31	Wavelet analysis shows that the $2 - 20$ s time scales contribute very strongly to the particle flux in
32	Lecce, while in Innsbruck the 20 – 200 s time scales are clearly dominant. In both cities, larger-sized
33	eddies contribute only sporadically to turbulent aerosol fluxes. These results suggest that spectral
34	similarity of urban particle number fluxes holds, to a large extent, even when comparing two very
35	different urban environments and different meteorological conditions.
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Keywords: Urban aerosol fluxes; spectral analysis; cospectral peak; spectral similarity, eddy covariance.



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18:00

Innsbruck

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06:00

12:00

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Lecce



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55 **1 Introduction**

Aerosols are continuously emitted from ground level sources and deposited back to the surface.
Aerosol surface/atmosphere exchange is dominated by turbulent transport in so-called "eddies" (e.g.
Reynolds, 1894; Foken, 2008). The net exchange is evaluated by measuring turbulent aerosol fluxes,
representing a key process governing the atmospheric aerosol burden and its impact on climate,
ecosystem health, and human health.

Our present knowledge of turbulent aerosol fluxes is incomplete, and thus, we lack a precise 61 62 understanding of the transport processes that govern changes in atmospheric particle concentrations. 63 The present paper aims to spectrally analyse turbulent time series and compare turbulent spectra in 64 two different European cities, Lecce (Italy) and Innsbruck (Austria) using eddy covariance (EC; e.g. 65 Aubinet et al., 2012) flux measurements. Wavelet analysis and multiresolution decomposition are applied to the EC data to compare co-spectra of atmospheric turbulent time series and quantify the 66 67 spectral flux contributions. The importance of analysing data with wavelets lies in the time-frequency localization that allows to study features of the signal both in the time and the frequency domains. 68

69 The turbulent surface-atmosphere exchange of atmospheric particles is usually quantified with the EC method. This approach requires fast measurements of turbulent fluctuations of the vertical 70 71 wind speed and aerosol concentration, typically with a measurement frequency of 10 Hz, under steady 72 state conditions, i.e. negligible changes of the statistical properties of the vertical wind and aerosol time series during the measurement interval (typically 30 min). Then, turbulent particle fluxes are 73 74 calculated as the covariance between the particle concentration and the vertical wind velocity. The 75 first studies in urban areas were performed starting from the 2000s (e.g. Nemitz et al., 2000; Dorsey et al., 2002; Longley et al., 2004; Mårtensson et al., 2006; Martin et al., 2009). 76

77 Particle counters are typically not sufficiently fast for a measurement frequency of 10 Hz, and sudden changes in particle concentration inherently violate the steady state assumption. Therefore, 78 79 due to limited instrument performance and non-ideal meteorological conditions, the post processing 80 of EC particle flux data must include the application of corrections, e.g. for slow response of particle instrumentation, de-trending of time series, coordinate rotation of wind measurements, and rigorous 81 82 quality assurance/control. To date, there is no best practice procedure for measuring the surfaceatmosphere particle exchange, and no standard protocol for data processing and analysis. As an 83 alternative to standard EC data processing, wavelet analysis is a spectral flux estimation method that, 84 in contrast to EC, does not require the steady-state assumption. Even though spectral flux estimation 85 methods such as wavelet analysis have been used to calculate turbulent fluxes (e.g. Katul and 86 87 Parlange, 1995; Saito and Asanuma, 2008; van den Kroonenberg and Bange, 2007), these methods 88 have barely been used with respect to particle fluxes.

The present work compares the meteorological conditions and turbulent fluxes in Lecce (Italy) 89 and Innsbruck (Austria), and then analyse the source areas (footprints) of particle concentration and 90 flux measurements to estimate the contribution of different source areas to the measurement. After a 91 comparison of diurnal cycles of meteorological parameters and turbulent fluxes, multiresolution 92 93 decomposition is applied in order to compare normalized cospectra of particle number and buoyancy fluxes and their diurnal evolution, and quantify the normalized frequency of the cospectral peak. 94 Finally, wavelet analysis is applied to extract the dominant time scales of the turbulent fluxes, and to 95 spectrally estimate 1 min particle number flux averages. The overall aim of this study is to 96 97 characterize the temporal dynamics of particle fluxes in two different cities with high resolution both in the time and frequency domains. 98

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100 2 Sites and methods

101 **2.1 Measurement sites and experimental setup**

102 Turbulent aerosol fluxes from two different cities, Innsbruck (Austria) and Lecce (Italy), were 103 compared. The measurements were carried out between 10 March and 24 April 2015 in Lecce, and 104 between 27 July and 21 August 2015 in Innsbruck. Both of the experimental sites, Innsbruck and 105 Lecce, were located on the rooftop of university buildings within the respective city centres.

106 Innsbruck is situated in the Alpine Inn Valley, with a population of about 130000 inhabitants. The Innsbruck site (Karl et al., 2020; latitude 47°15′51.50″ N; longitude 11°23′6.77″ E) is located 107 south west of the city centre, and it is characterized by a mountain-valley wind system (Deventer et 108 109 al., 2018; von der Heyden et al., 2018). The prevailing wind direction during the measurement period was ENE, and the maximum wind speed was 7.8 m s⁻¹ (Fig. 1a). The Innsbruck site is surrounded by 110 office and commercial areas, close to the Inn river and close to a busy state road (B171 "Innrain") 111 where vehicular traffic reached a maximum of 650 vehicles per hour. The measurements for this study 112 were carried out with a sonic anemometer (CSAT3, Campbell Scientific Inc., Logan, USA) and a 113 Condensation Particle Counter (CPC, Model 3772, TSI Inc., Shoreview, USA). 114

Lecce is situated in South-Eastern Italy close to the sea, with a population of about 95000 inhabitants. The Lecce site (latitude $40^{\circ}21'22''$ N; longitude $18^{\circ}10'02''$ E) is located in a street called "student's street" for the high presence of schools and university buildings, and where traffic reached a maximum of 2400 vehicles per hour. The main wind direction during the experimental campaign was N and the maximum wind speed was 5.4 m s⁻¹ (Fig. 1b). The experimental setup for this study comprised an ultrasonic anemometer (Gill R3-100, Gill Instruments, Lymington, UK) coupled with a CPC (Grimm 5.403, Grimm Aerosoltechnik, Ainring, Germany).

The two sites exhibit several characteristic differences, including (1) the geographical and 122 123 topographical conditions, (2) the experimental setup, and (3) the surface properties. First, the streetlevel elevation at the Innsbruck site is 570 m above sea level, i.e. much higher than at the Lecce site 124 at 55 m above sea level. Innsbruck is situated in the Inn valley that represents the transition zone from 125 Mediterranean to continental climate, while the Lecce site is about 12 km from the coastline of the 126 Adriatic Sea. Second, the eddy-covariance instrumentation was located on the roof of a university 127 building for the Innsbruck and Lecce sites at a height above ground level of 38.6 m and 14 m, 128 respectively. Furthermore, to minimize potential flow distortions due to the presence of high buildings 129 surrounding the sites, a wind sector between 140° and 190° was discarded from the Innsbruck data 130 (leaving 90 % of the total measurements), and a sector from 20° to 202° was eliminated from the 131 Lecce data (leaving 59 % of the total measurements). The first-order time constant of the CPC, used 132 in the Lecce site, was determined by estimating in laboratory the time response to a concentration 133 134 step. The results obtained in several repeated laboratory experiments was 1.3±0.05 s (Conte et al., 2018). The size range of the instrument is between 0.009 µm and 0.25 µm. At the Innsbruck site, the 135 136 CPC has a nominal size range between 0.010 μ m and > 1 μ m, and the experimentally determined response time was 0.46 s (von der Heyden et al., 2018). Third, to characterize the surface properties 137 138 of the urban canopies, the zero-plane displacement height (d_0) and the roughness length (z_0) parameters were evaluated for both sites. These parameters were evaluated for Lecce using a fitting 139 of measured EC data under unstable conditions (Toda and Sugita, 2003). The value of d₀ was derived 140 from the standard deviation of temperature and of vertical wind speed; the value of z_0 , instead, was 141 derived from a wind profile equation including the derived d₀ value. These values were estimated to 142 be $d_0 = 7$ m and $z_0 = 1.3$ m (Conte et al., 2018). For Innsbruck, the parameters were evaluated with a 143 height-based morphometric method (Grimmond and Oke, 1999), a mean building height of $z_B = 20$ 144 m, $d_0 = 0.7z_B$, and $z_0 = 0.1z_B$. The values were estimated to be about $d_0 = 14$ m and $z_0 = 2$ m (von der 145 Heyden et al., 2018). 146

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148 **2.2 Source area analysis**

Source area (footprint) analysis is important to estimate the pollutants' relative weights at the measurement point. A source area is defined as the fraction of the surface containing effective sources and sinks contributing to the measurement point (e.g. Schmid and Oke, 1990; Kljun et al., 2002). In this study, the source area for particle concentrations and fluxes was determined as the characteristic dimension of the oval-shaped area representing 50 % of measured concentrations or fluxes. Following Schmid (1994), the parameters defining the shape of the source areas were evaluated analytically by two equations that represent the normalised source area dimensions, D_N. The source areas depend on the measurement height (z_m) , and surface-layer scaling parameters such as the surface roughness length (z_0) , the Obukhov length (L), the standard deviation of lateral wind speed fluctuations (σ_v) , and the friction velocity (u_*) :

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$$D_N = \alpha_1 \left(\frac{z_m}{z_0}\right)^{\alpha_2} \exp\left[\alpha_3 \left(\frac{z_m}{L}\right)^{\alpha_4}\right] \left(\frac{\sigma_v}{u^*}\right)^{\alpha_5} \quad \text{(stable cases)} \quad (1)$$

161 $D_N = \alpha_1 \left(\frac{z_m}{z_0}\right)^{\alpha_2} \exp\left[1 - \alpha_3 \left(\frac{z_m}{L}\right)^{\alpha_4}\right] \left(\frac{\sigma_v}{u_*}\right)^{\alpha_5} \quad \text{(unstable cases)} \quad (2)$

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163 The parameters α_i (i=1,5) referring to two types of equation, are numerical inputs evaluated separately 164 for stable (equation 1) and unstable (equation 2) conditions according to the tables given in Schmid 165 (1994). The numerical values α_i differ for concentrations and fluxes and determine the elliptical shape 166 of the source areas. In this work, the oval-shaped source areas were approximated by ellipses oriented 167 along the wind direction. For every 30-min period, a function was defined, equal to one inside the 168 elliptical domain and equal to zero outside the elliptical domain: the source area is finally the sum of 169 all these functions normalized by the total number of measurements.

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171 **2.3 Flux calculation and spectral analysis**

The EC data from Innsbruck and Lecce were studied applying wavelet analysis and multiresolution
decomposition in order to investigate the temporal dynamics of particle fluxes in detail. The EC
method is commonly used to calculate vertical turbulent fluxes between surfaces and the atmosphere.
It requires fundamental assumptions such as steady state conditions and horizontal homogeneity (e.g.
McMillen 1988; Foken & Wichura, 1996).

177 The EC method expresses a turbulent flux F_{EC} of a certain entity by the covariance between 178 the concentration *c* of that entity and the vertical wind velocity *w*:

$$F_{EC} = \overline{c'w'}$$
(3)

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where the prime (') denotes the fluctuating part of that entity. Equation 3 represents the turbulent 181 vertical transport of c by fluctuations of c and w around their mean values (Baldocchi et al., 1988; 182 Arya, 1999; Burba et al., 2012). The advantage of this method consists in the direct and in situ flux 183 measurement without perturbation of the analysed ecosystem (Aubinet et al., 2012). An averaging 184 185 period of 30 minutes is typically chosen. However, the 30-minute data obtained from EC need an accurate quality check and consistent post-processing. While the three-dimensional wind 186 187 measurements using sonic anemometers are expected to be fully resolved at the sampling frequency of 10 Hz, the particle concentration measurements are dampened with experimentally determined 188

response times of 1.3 s for the CPC used in Lecce, and 0.46 s for the CPC used in Innsbruck. The expected reduction of the EC flux estimate due to imperfect sensor response can be taken into account as proposed by Horst (1997). To minimize the impact of the imperfect sensor response on the comparison of EC flux calculations and spectral analyses, all following calculations in this study are based on 1 Hz data sets. The quality of the final data is mainly influenced by sensor configuration, by meteorological conditions, and depending on the validity of the steady state assumption (Foken & Wichura, 1996; Moncrieff et al. 1996, Aubinet et al., 1996).

A method which does not rely on the steady state assumption to evaluate the turbulent flux is the wavelet approach (e.g. Torrence and Compo, 1998; Schaller at al., 2017). The total flux $F_{Wavelet}$ is the integral of the cross-wavelet spectrum E_{cw} between the particle concentration c and the vertical wind velocity w, and can thus be computed as:

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 $F_{\text{Wavelet}} = \delta j \sum_{j=0}^{J} \frac{E_{cw}(j)}{s_j}$ (4)

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Equation (4) represents the sum over all scales s_j of the real part of the cross-wavelet spectrum E_{cw} , and δj is the scale step size. The cross-wavelet spectrum is defined as:

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$$E_{cw}(j) = \frac{\delta t}{R} \frac{1}{N} \sum_{n=0}^{N-1} [W_n^c(s_j) (W_n^w(s_j))^*]$$
(5)

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where $W_n^{c,w}(s_j)$ are the wavelet transforms of the time series of *c* and *w*, respectively, and the asterisk (*) indicates the complex conjugate of the wavelet transform, δt is the time step of the time series, R is a reconstruction factor specific to the applied wavelet (e.g. R = 3.541 for the Mexican Hat wavelet, cf. Torrence and Compo, 1998), and N is the number of data points of the time series in the averaging period. It is useful to recall that the wavelet transform of a generic discrete time series $x_n(t)$, n =0, ..., N - 1 is generally defined as the convolution of the series with a scaled "s" and time-shifted wavelet function $\psi(t)$:

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$$W_n(s) = \sum_{n'=0}^{N-1} x_{n'}(t) \times \Psi^*\left(\frac{(n-n')\delta t}{s_j}\right)$$
(6),

allowing to obtain information about variability both in time and frequency of the time series. For
further details see Torrence and Compo (1998) and Schaller at al. (2017).

The scales " s_j " entering in the equations (4) - (6) are typically conveniently chosen as fractional powers of two:

$$s_j = s_0 2^{j \delta j} \tag{7}$$

with j = 0 to the maximum number of scales J, the smallest resolvable scale $s_0 = 2\delta t$, and the scale step size δj , in this study set to 0.25. The wavelet function is chosen according to the characteristics of the time series. In this study, the Mexican Hat wavelet was used to obtain the wavelet transforms of the two time series, $W_n^2(s)$, and information about the contribution of different frequency and time domains to the cross-wavelet spectrum. Thus, it is possible to evaluate turbulent fluxes over short averaging intervals, e.g. 1 min flux estimates.

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The data collected during both experimental campaigns were processed also using the multiresolution flux decomposition method (MRD). This analysis allows to decompose a time series $x_n(t)$ into averages on different time scales, obtained by M subsequent divisions of the whole time series starting from coarse (the whole series) to finer divisions in 2^M averaging points. This procedure of averaging using different window lengths corresponds to viewing the data at different resolutions, with each mode of the multiresolution decomposition corresponding to a certain moving average with a given length (Howell and Mahrt 1995):

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$$\overline{x_n}(2^m) = \frac{1}{2^m} \sum_{i=(n-1)2^m+1}^{m2^m} x_i$$
(8)

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where n=1,2,...,2^{M-m} is the window and x_i denotes the "residual" of the time series, that is the difference between the series and its approximation of order n. Once the temporal series is transformed by MRD in a frequency series, considering again the concentration *c* and the vertical wind velocity *w*, it is possible to evaluate the turbulent flux *F_{MRD}*:

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$$F_{MRD} = \sum_{m=1}^{M} \frac{1}{2^{M-m}} \sum_{n=1}^{2^{M-m}} (2^{m-1}\overline{c_{2n}} - 2^m\overline{c_n})(2^{m-1}\overline{w_{2n}} - 2^m\overline{w_n}) \quad (9)$$

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The three methods, EC, wavelet and MRD, allow to evaluate turbulent fluxes of a certain quantity. The EC method allows to investigate a turbulent flux on the ecosystem scale but it does not allow to obtain information about short-time turbulent events due to a violation of the steady state assumptions, on which this method is based. To overcome the steady-state requirement of EC, the wavelet analysis provides a localization, and thus a detailed analysis, of the turbulent events in both time and frequency. Wavelet analysis can provide the variability of a specific turbulent event and how its variability changes in time (Torrence and Compo 1998). MRD can be defined as nonoverlapping spectral analysis that provides information about the time scales of atmospheric fluctuations of a certain scalar. MRD typically has a smaller resolution in the frequency domain than wavelet analysis. The MRD locally decomposes the turbulent flux trying to characterize the dominant local events that correspond to the different averaging lengths considered in the analysis.

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258 **3 Results**

259 **3.1 Overview of campaigns in Lecce and Innsbruck**

260 General overview

Figure 1 and Table 1 summarize the time series, median values, and 5 % and 95 % percentiles of 261 meteorological data and particle concentrations and fluxes in the Lecce and Innsbruck measurement 262 campaigns. Due to the earlier time of year, the range of the air temperature (Fig. 1) and the median 263 air temperature is lower during the Lecce campaign in March and April 2015 than during the 264 Innsbruck campaign in July and August 2015. In both locations, wind speed exhibits a clear diurnal 265 cycle with calm nights and higher wind speeds during the day. The median wind speed of 1.8 m s⁻¹ is 266 slightly larger in Lecce than in Innsbruck (median wind speed 1.1. m s⁻¹), however, a southerly Foehn 267 event in Innsbruck on 23 and 24 August is the reason for higher maximum wind speeds in Innsbruck. 268 269 The prevailing wind direction during the Lecce campaign is from the North, while the Innsbruck campaign is characterized by a pronounced mountain-valley wind system with wind from the ENE 270 during the day and from the SW at night. This regular change of wind direction in the Inn valley 271 typically occurs between 09:30 and 11:00 in the morning, and between 17:30 and 19:00 in the 272 273 evening. While the baseline particle number concentration (5 % percentile) of roughly 4000 cm⁻³ is similar in Lecce and Innsbruck, the median and the 95 % percentile values of particle number 274 concentration are considerably larger in Lecce (median: 11419 cm⁻³) than in Innsbruck (median: 8990 275 cm⁻³). Similarly, the particle number fluxes are larger in Lecce than in Innsbruck, and the fraction of 276 277 positive particle number fluxes, i.e. net particle emission, is considerably larger in Lecce (90.6 %) 278 than in Innsbruck (69.7 %) as well. The buoyancy flux reaches larger maximum values in Lecce than in Innsbruck. The stability conditions are mostly near-neutral ($|z_e/L| < 0.1$, where $z_e=z-d_0$ is the 279 effective measurement height) or slightly unstable in Lecce, while unstable conditions ($z_e/L \le -0.1$) 280 prevail in Innsbruck. 281



Fig. 1: Time series of a,b) air temperature, c,d) wind speed (continuous line) and wind direction (dots), e,f)
particle number concentration, g,h) particle number flux, i,j) and buoyancy flux of the measurement campaigns
in Lecce and Innsbruck; grey flux data are from discarded wind sectors.

288	Tab. 1: Median values and 5 % and 95 % percentiles of air temperature, wind speed, particle number
289	concentration, particle number flux, friction velocity u*, buoyancy flux, and stability parameter z_e/L (Obukhov
290	length L=- $\frac{u^{*2}}{k(\frac{g}{T_0})T^*}$, where k is von Kármán constant, g /T ₀ is a buoyancy parameter and T* is the friction

temperature) of the measurement campaigns in Lecce and Innsbruck.

	Lecce			Innsbruck		
	5 %	median	95 %	5 %	median	95 %
air temperature [°C]	8.3	13.5	20.5	13.3	19.6	29.8
wind speed [m s ⁻¹]	0.6	1.8	3.8	0.3	1.1	4.6
particle number						
concentration [cm ⁻³]	4336	11419	34983	3826	8990	17151
particle number flux						
$[10^6 \text{ m}^{-2} \text{ s}^{-1}]$	-14.9	210.8	789.8	-209.4	40.2	307.2
u* [m s ⁻¹]	0.12	0.44	0.84	0.10	0.24	0.52
buoyancy flux [K m s ⁻¹]	-0.02	0.01	0.28	-0.01	0.02	0.12
ze/L [-]	-0.2	0.0	0.1	-7.0	-0.7	0.2

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295 Source area estimates

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Figure 2: a) Location and wind roses of the measurement sites in Innsbruck and Lecce, as well as average
 concentration source areas (b, c) and average flux source areas (d, e). The color scale represents the percentage
 of measures that gives contribution to the source area in any point.

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302 The source area estimates calculated using Eqs. 1 and 2 (section 2.2) are reported in Figure 2b and 2c for concentrations, and in Figure 2d and 2e for fluxes, for Innsbruck and Lecce, 303 respectively. In Innsbruck, the dominant concentration source areas are to the N/NE with the densely 304 305 built old town including a state road and public transportation to the city centre, and to a lesser extent 306 to the SW with University buildings and residential areas. The Innsbruck flux footprint is mostly affected by the nearby University buildings in the S/SW sector. In Lecce, the dominant concentration 307 308 and flux source areas are to the North of the measurement site with many buildings and roads with a high traffic density. The colour scale ranges from red, corresponding to the most influential areas, to 309 blue for the areas minimally influencing the measurements. Normalized over all measurement 310 periods, the most influential areas with respect to concentrations (red colours in Fig. 2b,c) are about 311 312 24 % and 55 % of the average source area in Innsbruck and Lecce, respectively, while the areas of

- minimum influence (blue colours) are about 2 % and 5 % of the average source area. For fluxes (Fig. 313 2d,e), the most influential areas are 10 % of the average flux source area in Innsbruck, and 12 % in 314 Lecce, while the minimum influential areas are about 1 % of the average flux source area in both 315 cities. In general, source areas for fluxes are smaller than those for concentrations (Contini et al., 316 2012; Vesala et al., 2008; Conte et al., 2018) because their values are proportional to the difference 317 between particles crossing the measurement level in upward and downward direction (Vesala et al., 318 319 2008), whereas particles crossing the measurement point always contribute positively to the evaluation of concentration source areas. Furthermore, flux measurements consider only the turbulent 320 321 transport of a scalar, while concentration measurements consider also transport by the mean flow. 322
- 323 Diurnal cycles



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Fig. 3: Median diurnal cycles of (a) wind speed, (b) air temperature, (c) particle number concentration, (d)
friction velocity, (e) buoyancy flux, and (f) particle number flux in Lecce (orange) and in Innsbruck (blue);
EC data after "bad" wind sectors removed.

Figure 3 shows median diurnal cycles of wind speed, air temperature, particle number concentration, friction velocity, buoyancy flux, and particle number flux obtained by EC method in Lecce (orange) and Innsbruck (blue). As mentioned before, there is a clear diurnal cycle of wind speed (Fig. 3a) with calm nights and higher wind speeds during the day, from about 06:00 to 21:00 in Lecce and from about 09:00 to 20:00 in Innsbruck. The peak wind speed of about 3 m s⁻¹ is reached in the afternoon between 13:00 and 16:00 at both sites. The diurnal cycle of air temperature (Fig. 3b) is very similar but shifted to higher temperatures in Innsbruck during the summer season. Temperatures begin to rise

at 07:00 in the morning at both sites. Particle number concentrations (Fig. 3c) show several peaks 336 during the course of the day: First, at both sites there is a steep increase in particle number 337 concentration from 04:30 in the morning reaching the peak value of 15000 cm⁻³ in Innsbruck at 06:00, 338 and 22000 cm⁻³ at 07:00 in Lecce. A second, slightly lower peak can be observed at both sites in the 339 evening hours around 21:00. Only in Lecce, a clear third peak is found around noontime in 340 correspondence of the maximum in solar radiation. Since the central peak happens around midday at 341 noon, in correspondence of the maximum in solar radiation, it was possible that this increase in 342 concentrations was related to local nucleation. The absence of this central peak in the suburban 343 344 environment excluded a regional nucleation process pointing to an urban nucleation event. The presence of this peak in the Lecce data set has already been discussed by Conte et al. (2015) and 345 346 Conte et al. (2018). This feature cannot be found in the Innsbruck data.

The friction velocity (Fig. 3d) is clearly enhanced during daytime both in Lecce and in 347 348 Innsbruck, which indicates well-developed turbulent conditions. The median friction velocity in Lecce is between 0.6 and 0.8 m s⁻¹ from 08:00 to 18:00, while the peak median friction velocity in 349 Innsbruck is much lower, around 0.3 m s⁻¹ from 11:00 to 18:00. The buoyancy flux (Fig. 3e) is mostly 350 positive and exhibits a clear diurnal cycle with values close to zero during the night, and an increase 351 352 after sunrise, which occurs earlier in the Innsbruck summer data (July/August) compared to the Lecce data from March/April. Again, the peak median buoyancy flux in Lecce is more than double 353 compared to the Innsbruck peak value. Both in Lecce and Innsbruck, the median buoyancy flux drops 354 back to values close to zero in the evening around 18:00. The particle number fluxes (Fig. 3f) are 355 mostly positive both in Lecce and in Innsbruck, indicating net particle emission especially during the 356 day. From 00:00 to 04:00 the net particle number fluxes are close to zero, and start to increase at the 357 same time when particle number concentrations increase. During daytime, median particle number 358 fluxes in Lecce are between 300 and 400 10⁶ m⁻² s⁻¹, while the median particle number fluxes in 359 Innsbruck are between 50 and $150 \cdot 10^6 \text{ m}^{-2} \text{ s}^{-1}$. Interestingly, in Innsbruck there is a brief period of net 360 particle deposition in the evening from 18:30 to 20:00, which cannot be observed in Lecce. 361

Adding data from the "bad" wind sectors does not considerably change the diurnal cycles in Innsbruck with respect to wind speed, air temperature, particle number concentration, and friction velocity but it slightly decreases the median estimates of the buoyancy flux and the particle number flux in Lecce. When taking into account only near-neutral and unstable conditions ($z_e/L < 0.1$), there is no considerable change of the diurnal cycles of wind speed, air temperature, particle number concentration, friction velocity and buoyancy fluxes both in Lecce and in Innsbruck. However, particle number fluxes are slightly enhanced in Lecce compared to Fig. 3.

3.2 Spectral analysis by multiresolution decomposition 371

We use multiresolution decomposition (MRD) as a simple tool to calculate cospectra of the vertical 372 wind speed w, temperature T, and particle number concentration C, respectively. The integrals of the 373 MRD cospectra, as given by Eq. 8, represent the total covariances w'T' and w'C', i.e. the buoyancy 374 and particle number fluxes. Due to the fact that the typical length scales of eddies increase with 375 increasing height in the surface layer, it is common practice to investigate cospectra as a function of 376 the normalized frequency $n = f z_e/u$, where f is the frequency $[s^{-1}]$, z_e is the effective measurement 377 height [m], and u is the horizontal wind speed [m s⁻¹] (e.g. Foken, 2008). To compare the contributions 378 of different frequencies to the total flux, individual cospectra are normalized by the corresponding 379 flux to yield the unit area normalized cospectral density. The normalized cospectra indicate the 380 381 contributions of different frequencies to the buoyancy and particle number fluxes.

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Comparing MRD cospectra in Lecce and Innsbruck

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386 Fig. 4: a) Median normalized cospectra of particle number fluxes in Lecce (orange) and Innsbruck (blue) 387 during daytime (11:00-17:00, solid) and night-time (23:00 - 05:00, dotted) conditions; b) cumulative median 388 normalized cospectra of particle number fluxes (solid) and buoyancy fluxes (dotted) in Lecce and Innsbruck. 389

Figure 4a compares the median normalized cospectra of particle number fluxes measured in Lecce 390 and Innsbruck during daytime conditions from 11:00 to 17:00, and during the night from 23:00 to 391 05:00. The location of the cospectral peak n_m is close to a value of $n_m = 0.085$, which is expected 392

cumulative normalized cospectral density [-]

under neutral and unstable conditions (Kaimal et al., 1972). In Lecce, the median cospectrum at night is broader than during the day, with equal flux contributions in the normalized frequency range between 0.01 and 1. In Innsbruck, the cospectrum is narrower compared to Lecce, and very similar during daytime and night-time, indicating a narrower distribution of eddy sizes compared to Lecce. This indicates that the typical eddy size associated with the normalized frequency of the cospectral peak is more dominant in Innsbruck compared to Lecce, possibly due to a larger heterogeneity of the urban canopy in the flux footprint of Lecce compared to Innsbruck.

When comparing median cumulative cospectra in Lecce and Innsbruck (Fig. 4b), high frequency 400 contributions are evidently higher for buoyancy fluxes than for particle number fluxes. There are no 401 considerable contributions to particle number fluxes at normalized frequencies greater than 1, 402 especially in Innsbruck. This illustrates the imperfect response of the particle counters to 403 concentration fluctuations, while the sonic anemometer measurement fully resolves the acoustic 404 405 temperature fluctuations at the measurement frequency. In contrast, low frequency contributions to buoyancy fluxes are much smaller than to particle number fluxes, indicating that scalar similarity of 406 407 temperature and particle number concentration is limited. In summary, the particle flux cospectra are shifted to lower frequencies compared to the buoyancy flux cospectra, and the particle and buoyancy 408 409 flux cospectra are more similar in Lecce than in Innsbruck. The same observations are found when separating daytime and night-time data. 410

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- 412

413 Diurnal evolution of MRD cospectra



415 Figure 5: Diurnal cycle of median normalized particle number flux cospectra in a) Lecce and b) Innsbruck;

416 the white line indicates the cospectral peak fitted to the median cospectra of all 30 min intervals.



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Figure 6: Diurnal cycle of median normalized buoyancy flux cospectra in a) Lecce and b) Innsbruck; the whiteline indicates the cospectral peak fitted to the median cospectra of all 30 min intervals.

Figures 5 and 6 show the diurnal evolution of the median normalized cospectra with respect to particle number fluxes and buoyancy fluxes in Lecce and Innsbruck obtained from multiresolution decomposition. The white line indicates the cospectral peak at the normalized frequency n_m fitted to the median cospectra of all 30 min intervals assuming a model for the normalized cospectrum Co according to Eq. 10 (e.g. Horst, 1997)

$$Co = \frac{2}{\pi} \frac{n/n_{\rm m}}{1 + (n/n_{\rm m})^2} \tag{10}$$

Thus, the cospectral peak indicates the normalized frequency n with the highest contribution to the flux, i.e. the inverse of the dominant time scale of turbulent transport. The red colours indicate the normalized frequency ranges with the highest contribution to the total fluxes at different times of the day.

For particle number fluxes (Fig. 5), the main contributions are in the normalized frequency 431 range from 0.01 to 1, both in Lecce and in Innsbruck. In Lecce (Fig. 5a), there is a lot of scatter from 432 00:00 to 06:00, when fluxes are generally small. In the morning after 06:00, there seems to be a slight 433 shift from higher frequencies to lower frequencies around noon, and then again a slight increase to 434 higher frequencies contributing to the particle number flux in the evening. In contrast, there is no 435 436 obvious diurnal pattern in the median normalized cospectra of buoyancy fluxes (Fig. 6a), and the contributing frequencies are clearly shifted to higher frequencies from 0.1 to 1. In Innsbruck, there is 437 438 no obvious diurnal pattern in the median normalized cospectra of particle number fluxes (Fig. 5b) but a shift from higher frequency contributions during night-time to lower frequency contributions to the 439 440 buoyancy flux during the day (Fig. 6b). This indicates that the dominant time scales of turbulent transport are different for the two studied scalars, particle number concentration and temperature. The 441 peak frequencies of the particle flux cospectra are similar in Lecce (median of $n_m = 0.087$) and in 442 Innsbruck (median of $n_m = 0.086$), close to the expected value of $n_m = 0.085$, and relatively constant 443 444 throughout the day (Lecce interquartile range 0.085-0.091; Innsbruck interquartile range 0.079-445 0.089). In contrast, the buoyancy flux cospectra show clearly higher peak frequencies (Lecce median of $n_m = 0.193$; Innsbruck median of $n_m = 0.445$) compared to the particle flux cospectra. The higher 446 median value in Innsbruck is mostly due to much higher peak frequencies during the night-time. In 447 the well-mixed convective boundary layer, the Eulerian integral scale Λ_i associated with the scalar 448 449 flux is related to the normalized frequency of the cospectral peak, n_m, and the effective measurement height z_e according to Eq. 11 (Mann and Lenschow, 1994): 450

451
$$\Lambda_i = \frac{z_e}{2\pi n_m} \tag{11}$$

For the particle fluxes, this length scale is relatively stable with a median value of $\Lambda_i = 13$ m in Lecce and $\Lambda_i = 45$ m in Innsbruck. In contrast, the median Eulerian integral scale of the buoyancy fluxes is $\Lambda_i = 6 \text{ m}$ in Lecce, and exhibits a diurnal cycle in Innsbruck with values around $\Lambda_i = 6 \text{ m}$ in the nighttime and Λ_i up to 20 m during daytime. It should be noted that the effective measurement height in Innsbruck is $z_e = 24.6 \text{ m}$, and $z_e = 7 \text{ m}$ in Lecce. Thus, both the ratio of the Eulerian integral scales of particle flux cospectra and the ratio of the effective measurement heights in Innsbruck and Lecce are approximately 3.5, and the different values of the Eulerian integral scale of particle flux cospectra are proportional to the different effective measurement heights above the two urban canopies.

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461 **3.3 Wavelet analysis**

Wavelet analysis yields cross-wavelet spectra of particle number concentration and wind speed with information about the contributions of different frequency ranges of the turbulent time series to the total fluxes in both the time and frequency domains. This allows to analyse the typical contributions of different time scales, i.e. eddy sizes, in more detail.



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Figure 7: Median diurnal cycle of particle number fluxes reconstructed from wavelet analysis for 30 min intervals (black) in Lecce (left) and Innsbruck right); flux contributions of 2 - 20 s scales in orange and dark blue, 20 - 200 s scales in yellow and light blue, and 200 - 2000 s scales in grey.

Figure 7 shows the median diurnal cycle of 30 min particle number fluxes in Lecce and Innsbruck reconstructed from wavelet analysis, and the contributions of three different frequency ranges corresponding to time scales of 2 - 20 s (small eddy sizes), 20 - 200 s (medium eddy sizes), and 200 - 2000 s (larger eddy sizes). Note that the contributions of scales can be positive or negative, and therefore, the sum of the three frequency ranges may be slightly larger or smaller at any time interval. Interestingly, the 2 - 20 s time scales (orange) contribute very strongly to the particle flux in Lecce, while in Innsbruck the 20 - 200 s time scales (light blue) are clearly dominant. This is consistent with

- the smaller Eulerian integral scale of the particle fluxes in Lecce compared to Innsbruck (cf. section 3.2). Both in Lecce and Innsbruck, the contribution of the 200 - 2000 s time scales to the total median particle flux is very small, i.e. less than $20 \cdot 10^6$ m⁻² s⁻¹. However, in many cases on individual days, quick changes in fluxes are due to larger-than-usual contributions of the 200 - 2000 s time scales. Thus, sporadically, larger eddies can contribute significantly to turbulent fluxes and may lead to sudden changes of the particle number concentration.
- Taking advantage of the localization in the time domain, an estimate of the particle number flux can
 be calculated from cross-wavelet spectra not only for 30 min intervals (like in EC) but also for shorter
 time intervals, e.g. 1 min.



487 Figure 8: Median diurnal cycle of particle number fluxes reconstructed from wavelet analysis for 30 min
488 intervals (black) and 1 min intervals (smoothed with a 30 min rolling average filter) in Lecce (left, orange) and
489 Innsbruck (right, blue).

490 Figure 8 shows the median diurnal cycle of particle number fluxes in Lecce and Innsbruck, reconstructed from wavelet analysis based on 30 min intervals and 1 min intervals. Apparently, the 1 491 min flux estimates are scattered around the 30 min flux estimates with deviations of about 30 % 492 during daytime. In Lecce, the deviations are quite small during the night and constant during the day. 493 In Innsbruck, the strongest deviations occur in the transition periods of wind direction reversal, i.e. 494 495 around 09:00 in the morning, and between 17:30 and 19:00 in the evening. During periods when the 1 min flux estimates are close to the 30 min flux estimates, steady state conditions are expected. 496 However, this interpretation should not be applied to median diurnal cycles of the 1 min and 30 min 497 wavelet flux estimates but to individual time periods of the Lecce and Innsbruck data sets. 498

499 Conclusions

On average, particle emission is dominant in both cities. The particle emission fluxes follow a similar 500 diurnal cycle but are much stronger in Lecce compared to Innsbruck. The diurnal cycle of the particle 501 number concentration shows three maxima in Lecce: one in the morning, one at noon and one in the 502 503 late afternoon. In Innsbruck, only the morning and late afternoon maxima are visible. These two peaks are probably associated with high traffic density in the morning and evening rush hours, and the 504 505 noontime peak in Lecce is likely due to local particle nucleation. The source areas for fluxes were 506 estimated to be much smaller than those for concentrations. The fact that the flux source areas include 507 the respective main roads located near the experimental sites, and that the diurnal cycle of particle emission fluxes is consistent with vehicular traffic activity, traffic is identified as a major emission 508 509 source of particles both in Lecce and in Innsbruck.

Multiresolution decomposition allowed to compare the normalized cospectra of vertical wind speed 510 511 and particle number concentration, and thus, the contribution of different frequencies to the total particle number flux. On the one hand, the shape of the median normalized cospectra of particle fluxes 512 was slightly different in Lecce and Innsbruck, with a broader distribution of frequencies contributing 513 to the flux in Lecce compared to Innsbruck, especially at night. On the other hand, the cospectral 514 peak, i.e. the frequency with the largest contribution to the particle number flux, was similar in Lecce 515 and in Innsbruck. The cospectral peak of particle fluxes was relatively constant throughout the day 516 both in Lecce and Innsbruck, with a median value of 0.087 in Lecce and 0.086 in Innsbruck. The 517 cospectral maximum is expected at $n_m = 0.085$ under neutral conditions. These findings support the 518 assumption of spectral similarity for cospectra of urban particle number fluxes in two cities with 519 520 different micrometeorological conditions. At the same time, scalar similarity with respect to 521 temperature and particle number concentration is limited. However, when comparing cospectra of 522 particle number fluxes and buoyancy fluxes, the scalars are more similar in Lecce than in Innsbruck; in both cities, the cospectral peak of the buoyancy fluxes is shifted to higher frequencies, and the 523 524 contribution of high frequencies is larger to the buoyancy flux than to the particle flux. This may indicate that high frequency particle flux contributions were dampened due to insufficient time 525 526 resolution of the condensation particle counters, even when using 1 Hz data in this study.

527 Considering the results of the wavelet analysis, full resolution of the high frequency 528 contributions may be particularly important in Lecce, where the 2 - 20 s time scales contribute very 529 strongly to the particle flux in Lecce, while in Innsbruck the 20 - 200 s time scales are clearly 530 dominant. Both in Lecce and Innsbruck, the contribution of the 200 - 2000 s time scales to the total 531 median particle flux is very small. Thus, in order to quantify particle emission fluxes in these two 532 cities, the averaging interval used for the EC calculations may be changed to shorter periods of 5 or 533 10 min, and steady-state assumptions may not be required for full 30 min intervals. However, larger-534 sized eddies might sporadically contribute in a very strong way to particle number fluxes. Even if the 535 steady state assumption is not fulfilled, reconstruction of flux estimates from wavelet analysis can 536 still be applied to shorter time intervals. For the studied periods in Lecce and Innsbruck, the 1 min 537 wavelet estimates of particle number fluxes deviated by less than 30 % from the 30 min EC flux 538 estimates on average during daytime.

In summary, the presented results clearly suggest that spectral similarity of urban particle number fluxes holds to a large extent, even when comparing two very different urban environments such as Lecce close to the Adriatic Sea and Innsbruck in the Alpine Inn valley. The results also illustrate the great potential of spectral flux estimation methods such as wavelet analysis for application in future studies of turbulent particle fluxes.

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Graphical abstract

