

Supporting Information for: Electric Field Enhancements and Hot Spots in Amorphous Carbon Materials

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S1 DynReaxMas a-C structures

S1.1 Massaged parameters and MM_n/MM_m notation

Within the DynReaxMas protocol, the PES exploration is accelerated by *messages*, that is, by judicious modifications of the ReaxFF potential parameters (including bond strengths, dispersion, bending constants, ...). Clearly, not all the messages affect the generation of the models in the same way (we refer to Ref. 1 for a more detailed discussion). On the one hand, a subset of parameters, the *hard* parameters, which include bond strengths, lead to a major reorganization of the structure (large displacement on the PES), which can be quantified by means of the root mean square displacement of the atoms. On the other hand, other parameters, the *soft* ones, allow for a more local exploration of the PES, helping to find the most stable configurations. In order to obtain structurally different models, it is thus important to always include at least one hard parameter in the message sequence, but only at the beginning of the sequence, while allowing for a reconstruction of the networks under the message of soft parameters in the following steps, especially the final ones. For this reason, we found it convenient in designing the DynReaxMas protocol to generate random sequences of 4 messages each, to be combined in pairs, one sequence containing at least 1 hard parameter message, and one sequence that does not contain hard parameter messages. For instance, in the original DynReaxMas paper,¹ MM1 (for convenience here named M1) is a sequence of four messages including a hard parameter. M1 can be combined with MM8 (or M8), containing soft-only messages, to yield a MM1/MM8 DynReaxMas standardized message protocol (or M18 for simplicity). Analogously, M3, containing message of hard parameters, can be combined with M4, containing only soft messages, to give a proper MM3/MM4 DynReaxMas sequence or standardized message protocol. In this work we simplify the notation from MM1/MM8 to M18.

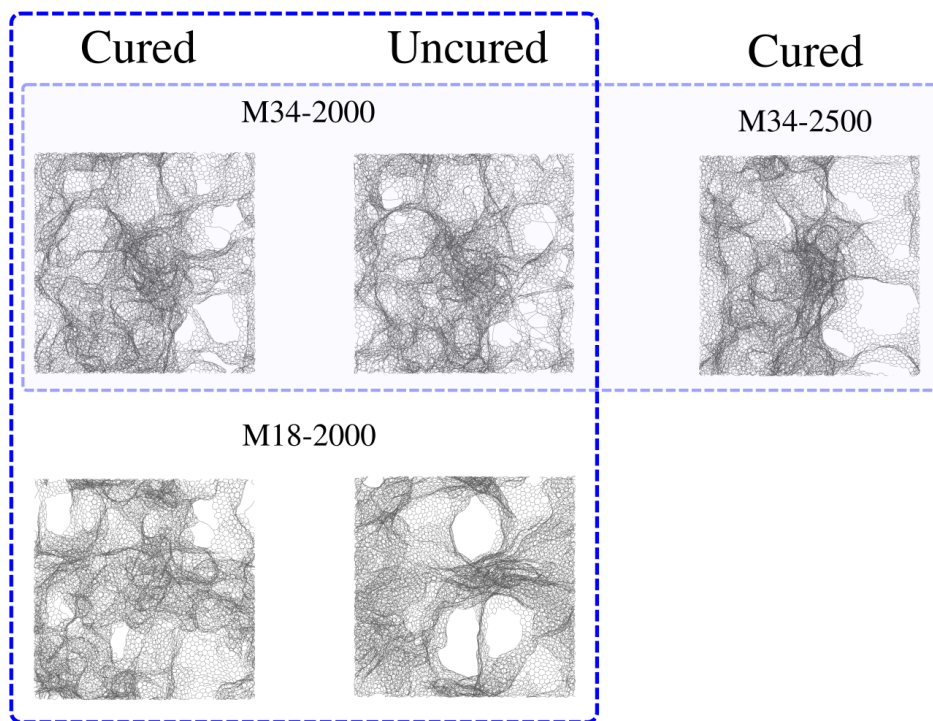


Figure S1: Schematic atomistic depiction of the different a-Carbon phases in their simulated unit cells.

S1.2 Main descriptors of a-C structures

Table S1 contains the main structural descriptors of the a-Carbon phases described in the main text. C_1 , C_2 , C_3 , C_4 , are the number of carbon atoms that have only one, two, three, four, respectively, neighbors within bonding distance, normalized by the total number of atoms in the cell. Pure graphene would have $C_1=C_2=C_4=0$ and $C_3=1$. As expected, the curing protocol increases the C_3 content, which is related to the higher degree of graphitization achieved upon curing. $A(\text{sp})$ quantifies the deviation from the theoretical 180° angle energy minimum for 2-coordinated C atoms. Since the edges of the graphitic sheets have 2-coordinated atoms with 120° angles, smaller values of $A(\text{sp})$ in the cured phases are related to a higher sheet extension/edge ratio. R_5 , R_6 , R_7 describe the number of 5-, 6-, and 7-member rings, respectively, as a percent (normalized by the total number of atoms). For reference, graphite would have $R_6=50$, since every atom is part of three 6-member rings, so the total number of rings normalized by the number of atoms n is $3n/6n \times 100\% = 50$. It is apparent that the curing step increases the amount of 6-member rings while decreasing the 5-member ones.

In order to estimate the defect content of the structures (dangling bonds and/or unsaturation), we developed in Ref. 2 a screening probe protocol in which a mildly reactive molecule (a fake water-like species with

purposely decreased overcoordination penalty) is introduced in the system to react with the defects. While we refer to the original work for details, Table S2 summarizes the percent number of atoms (normalized by the total amount of carbon atoms) that react with the probe. We note that the curing step clearly decreases the number of such sites, indicating a lower amount of high energy defects in the structures.

Table S1: Structural descriptors for the M18 and M34 phases discussed in the paper, in both their as-prepared and cured forms.

Structure	C1	C2	C3	C4	A(sp)	R5	R6	R7
050-18-2000cured	0.000	0.039	0.954	0.006	27.709	9.822	26.225	9.499
050-18-2000	0.000	0.092	0.892	0.016	22.929	11.135	18.894	9.363
050-34-2000cured	0.000	0.042	0.951	0.007	28.056	9.399	26.345	9.255
050-34-2000	0.000	0.093	0.884	0.022	21.084	10.461	19.975	9.559
050-34-2500cured	0.000	0.025	0.969	0.007	27.965	9.179	27.826	9.279
050-34-2500	0.000	0.040	0.943	0.017	24.688	9.782	24.118	9.714

Table S2: Percent number of sites vs. total number of carbon atoms that are available for saturation with a reactive water probe for the phases discussed in this paper, for both as-prepared and cured forms.

Structure	Reacted	Structure	Reacted
050-18-2000	16.46	050-18-2000 cured	13.58
050-34-2000	15.94	050-34-2000 cured	12.96
050-34-2500	12.50	050-34-2500 cured	11.17

S2 ω FQ parameters and dependence of the optical response on τ

Table S3: ω FQ parameters exploited in the calculations.³

Parameter	Value
η	0.37 a.u.
τ	170.0 a.u.
E_F	0.4 eV
\mathcal{A}_i	0.4879 \AA^2
d	100.0
s	1.2
l_{ij}^0	1.4129 \AA

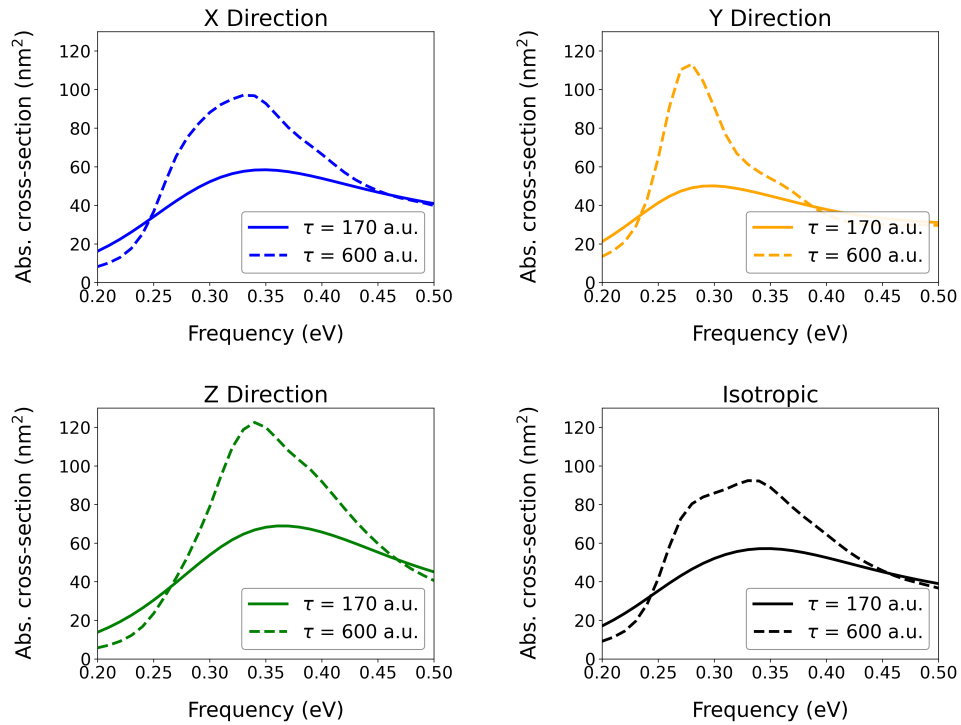


Figure S2: ω FQ absorption spectra of the cured M34-2000 structure (generated from a 50% replication of the unit cell) using $\tau = 170$ a.u. and $\tau = 600$ a.u..

Table S4: Maximum electric field enhancement $|E|/|E_0|$ for the M34-2000 Cured structure (generated from a 50% replication of the unit cell) using $\tau = 170$ a.u. and $\tau = 600$ a.u. as a function of the field polarization.

Polarization	Maximum $ E / E_0 $	
	$\tau = 170$ a.u	$\tau = 600$ a.u
\vec{E}_x	25.92	62.92
\vec{E}_y	37.73	123.66
\vec{E}_z	32.21	119.85
Average	32.09	102.14

S3 Optical Absorption: Cured M34-2000 vs. Cured M34-2500

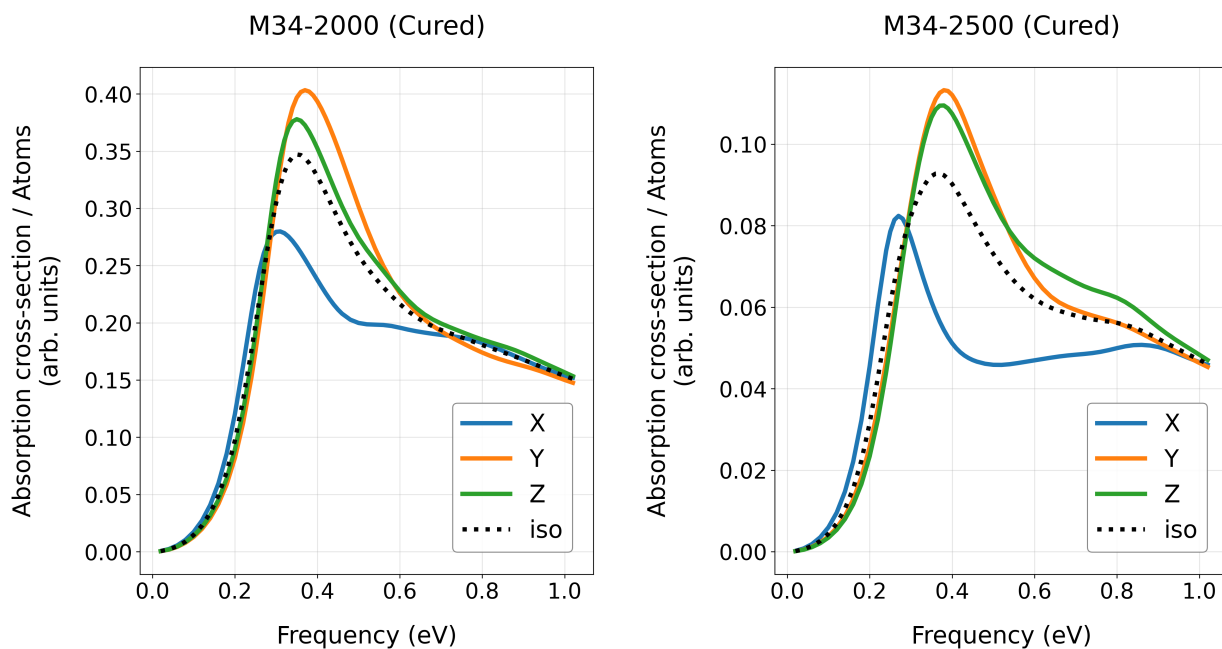


Figure S3: ω FQ absorption spectra of the cured M34-2000 and M34-2500 structures (generated from a 50% replication of the unit cell), normalized by the total number of atoms.

S4 Three-dimensional density

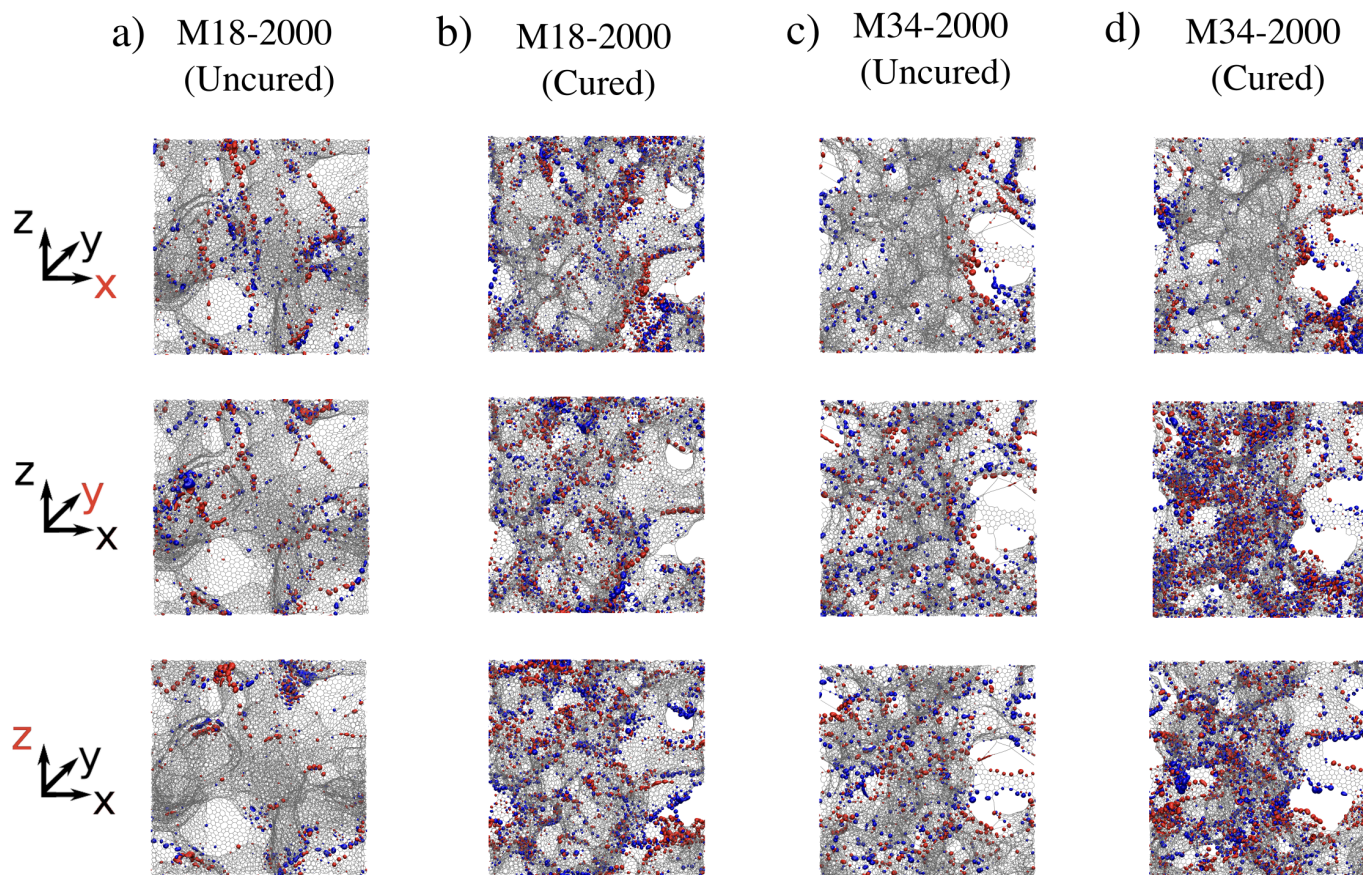


Figure S4: ω FQ induced densities for X, Y, and Z field polarizations for M18-2000 (a-b) and M34-2000 (c-d) in their uncured (a,c) and cured (b,d) forms. The maps are provided within the central unit cell.

S5 Electric field enhancement

S5.1 Effective Volume and Effective Area

Table S5: Effective volume and effective area for M18-2000 and M34-2000 a-C superstructures in their uncured and cured forms as a function of the field polarization calculated on the representative planes shown in Fig. 3 in the main text.

Structure	Effective volume ($\times 10^{-2} \text{ nm}^3$)				Effective area ($\times 10^{-2} \text{ nm}^2$)			
	M18-2000		M34-2000		M18-2000		M34-2000	
	Uncured	Cured	Uncured	Cured	Uncured	Cured	Uncured	Cured
\vec{E}_x (YZ plane)	5.682	1.031	3.894	0.841	28.408	5.153	19.469	4.203
\vec{E}_y (XZ plane)	7.692	3.187	8.559	0.786	38.462	15.935	42.796	3.932
\vec{E}_z (XY plane)	6.765	1.954	15.335	4.819	33.824	9.771	76.674	24.096
Average	6.713	2.057	9.263	2.149	33.565	10.286	46.313	10.744

S5.2 2D Field Enhancement Maps

S5.2.1 M18-2000 Uncured

M18-2000 (Uncured) XY

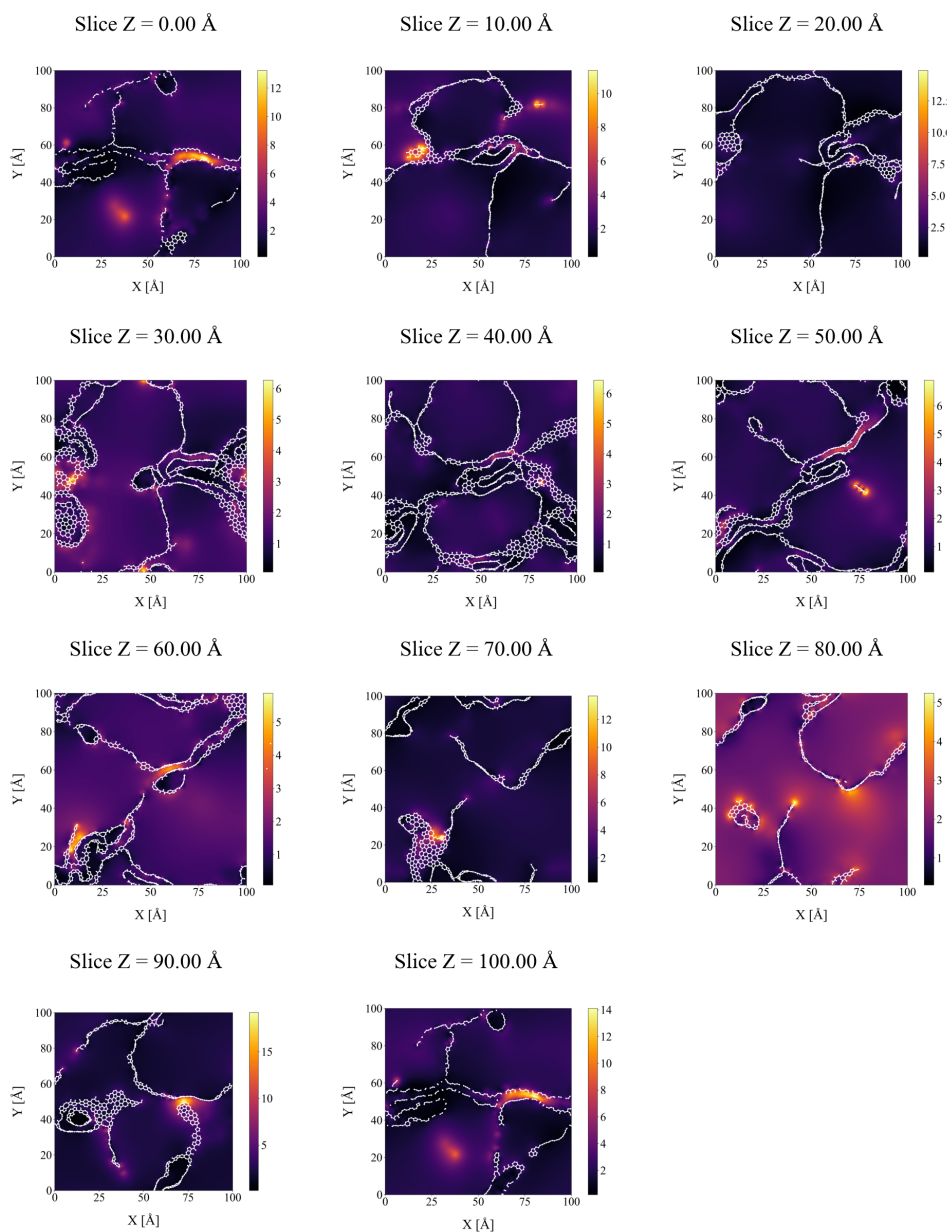


Figure S5: 2D field enhancement maps on XY planes for the uncured M18-2000 structure.

M18-2000 (Uncured) XZ

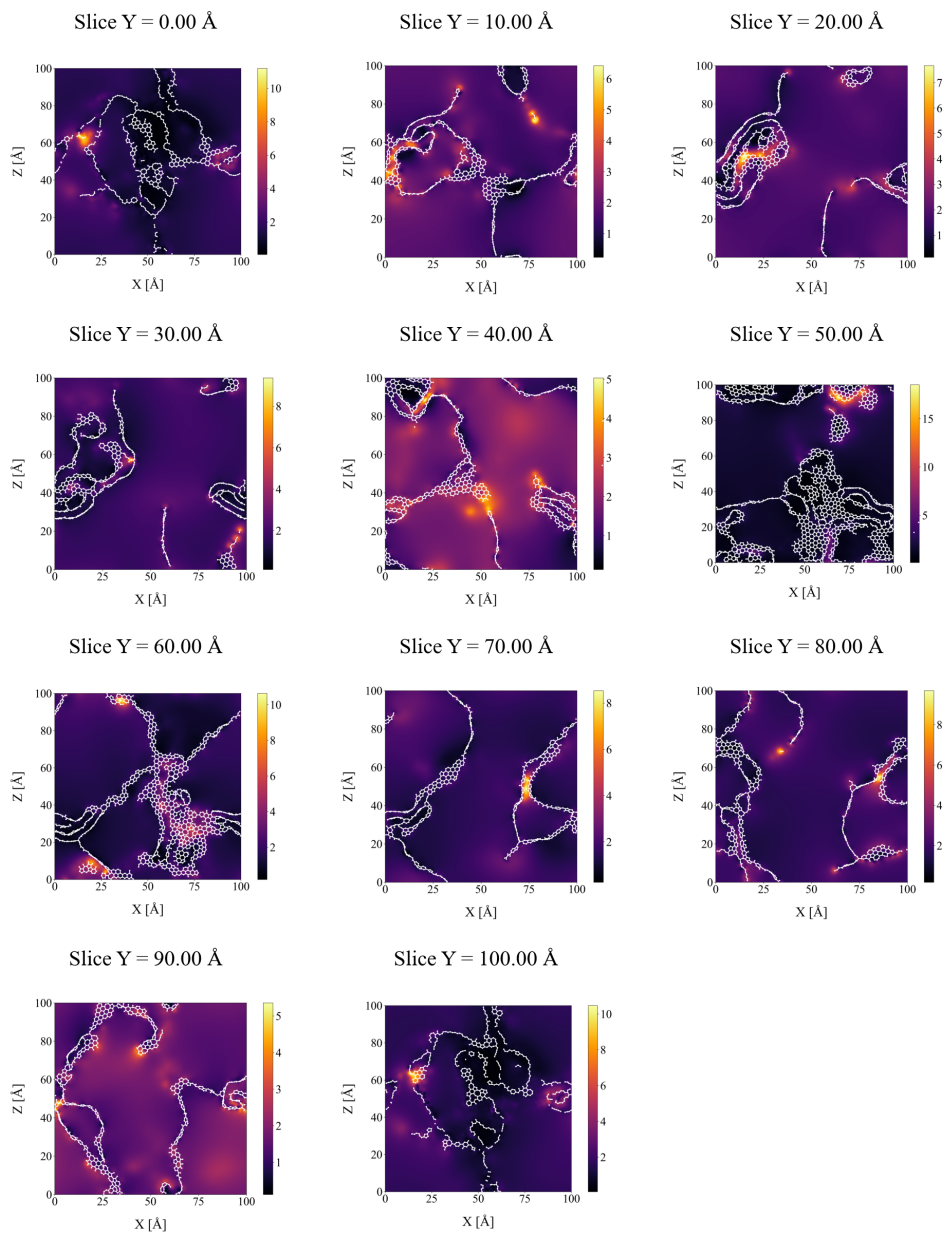


Figure S6: 2D field enhancement maps on XZ planes for the uncured M18-2000 structure.

M18-2000 (Uncured) YZ

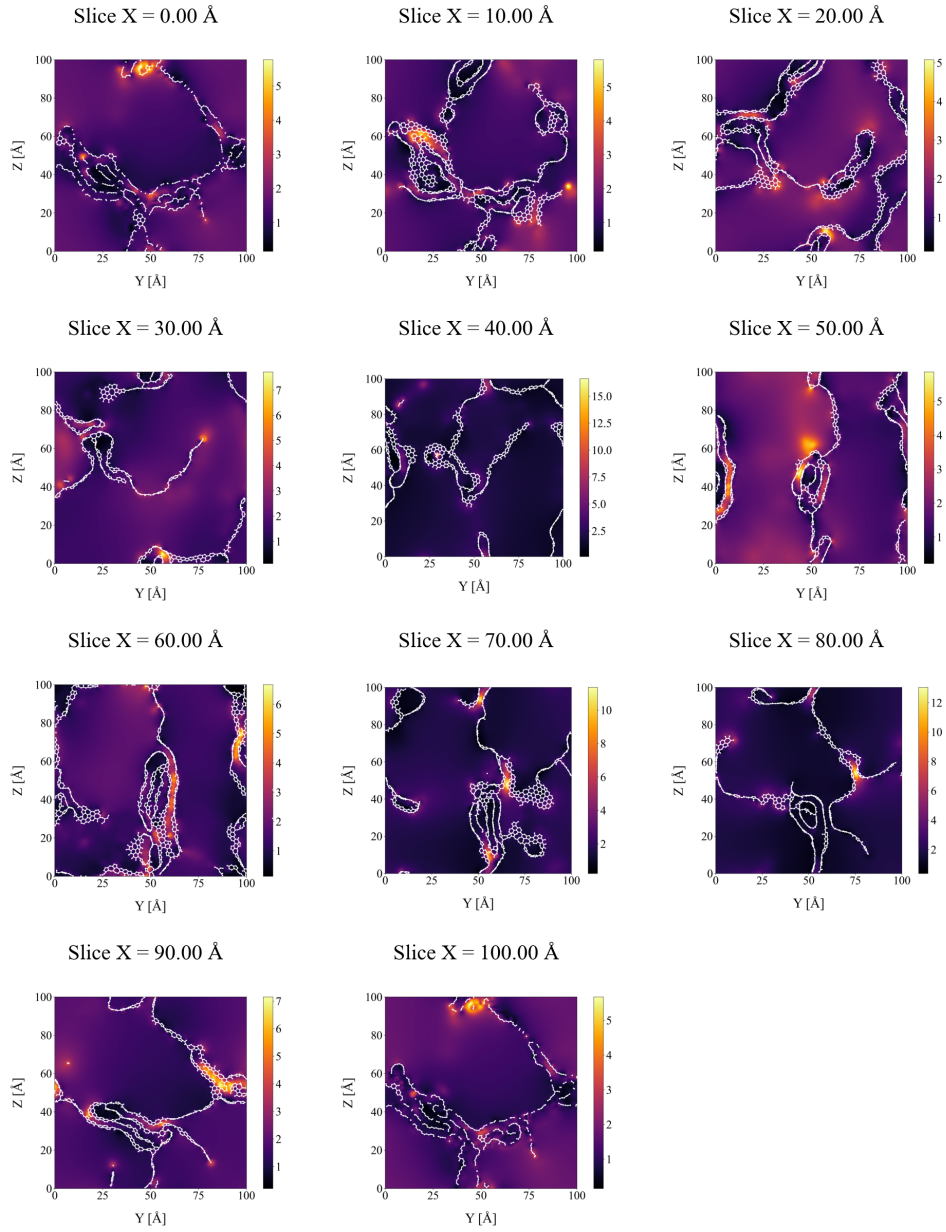


Figure S7: 2D field enhancement maps on YZ planes for the uncured M18-2000 structure.

S5.2.2 M18-2000 Cured

M18-2000 (Cured) XY

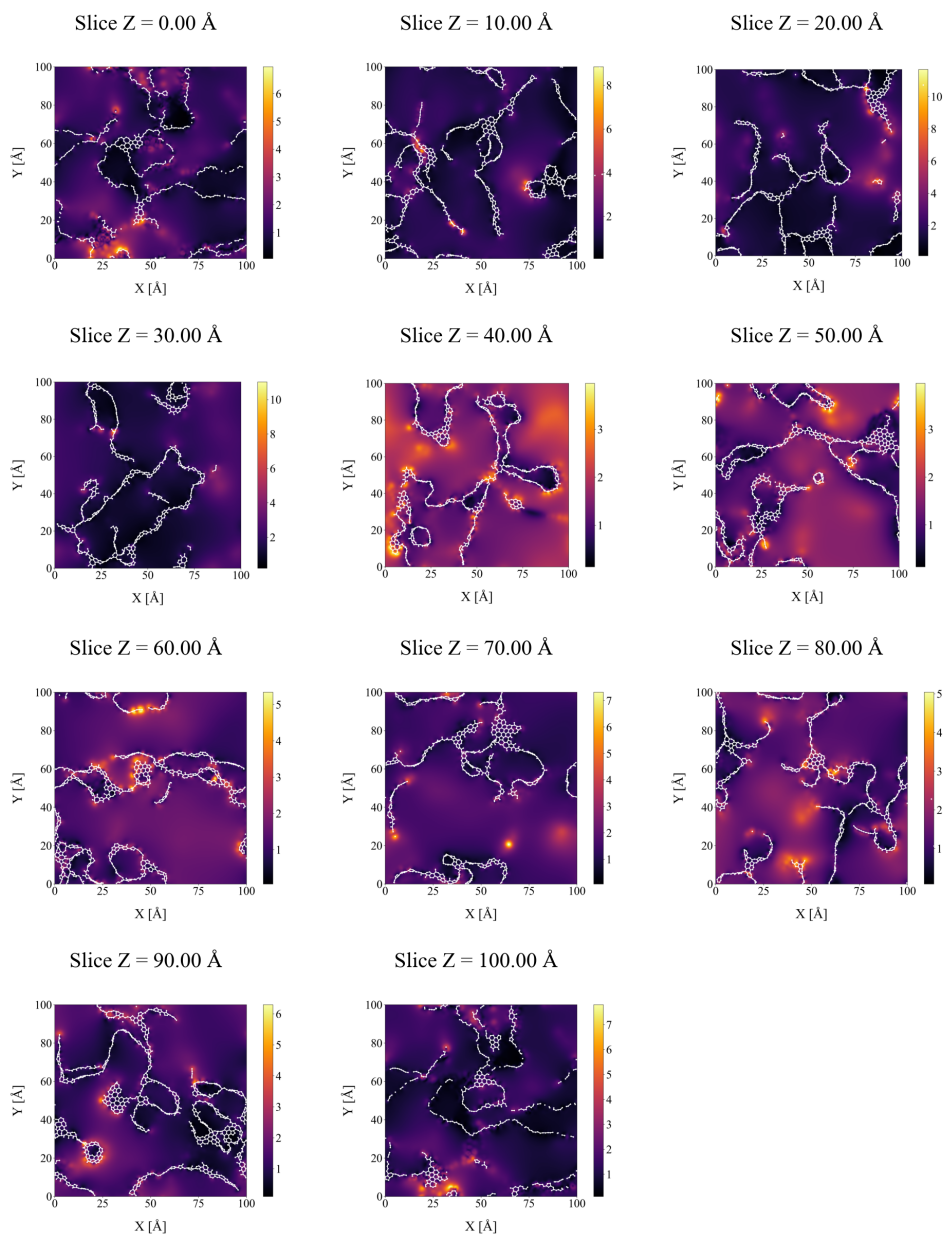


Figure S8: 2D field enhancement maps on XY planes for the cured M18-2000 structure.

M18-2000 (Cured) XZ

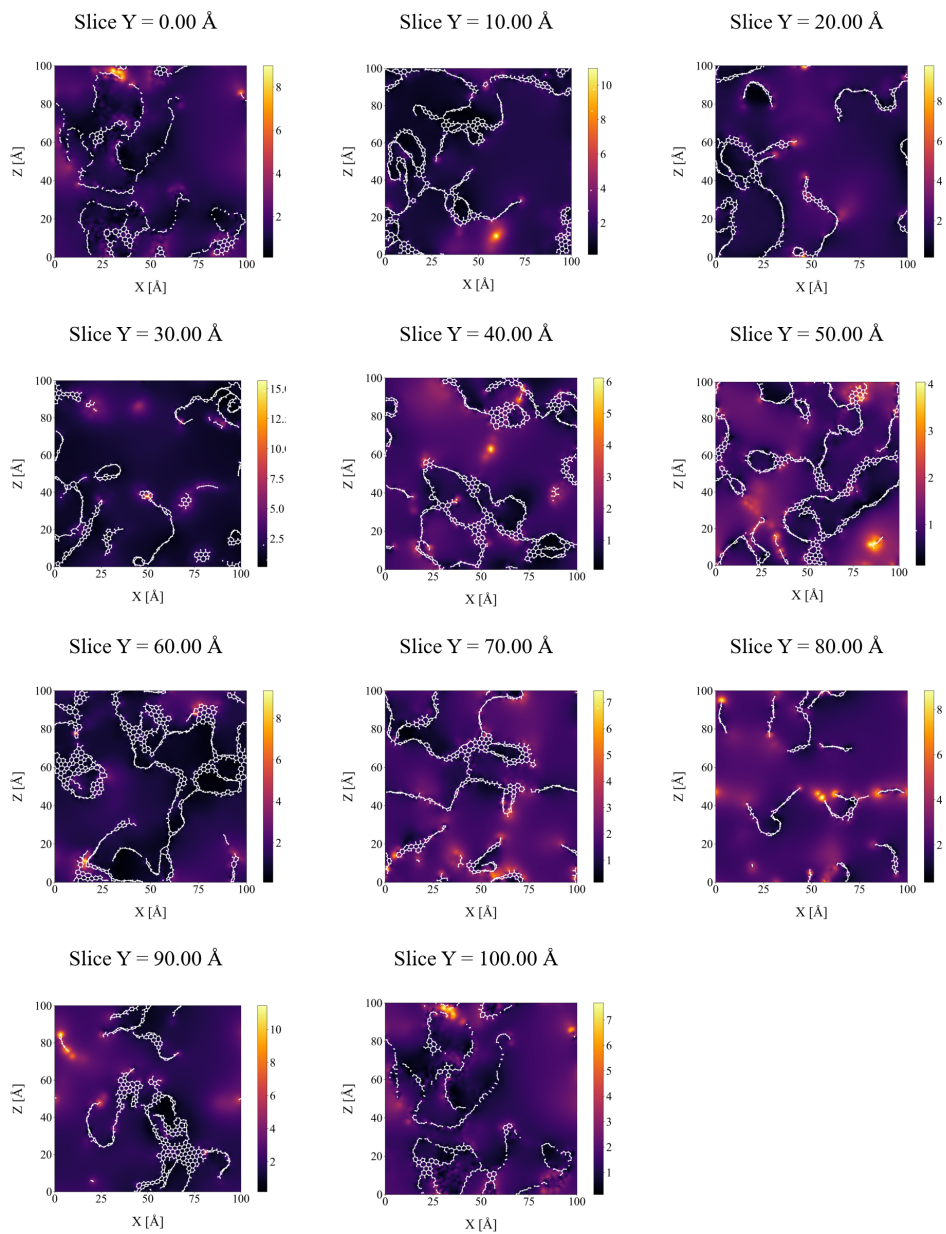


Figure S9: 2D field enhancement maps on XZ planes for the cured M18-2000 structure.

M18-2000 (Cured) YZ

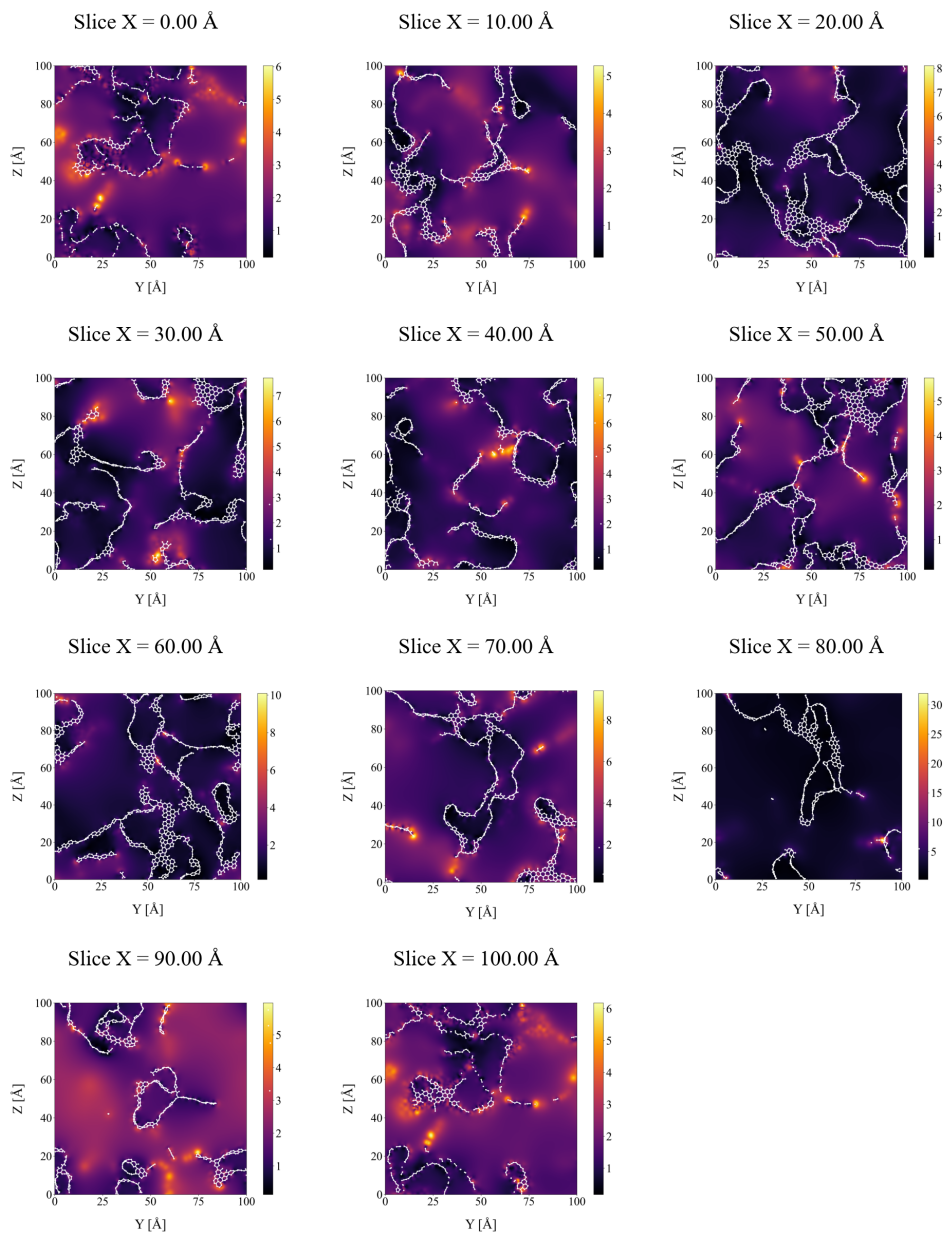


Figure S10: 2D field enhancement maps on YZ planes for the cured M18-2000 structure.

S5.2.3 M34-2000 Uncured

M34-2000 (Uncured) XY

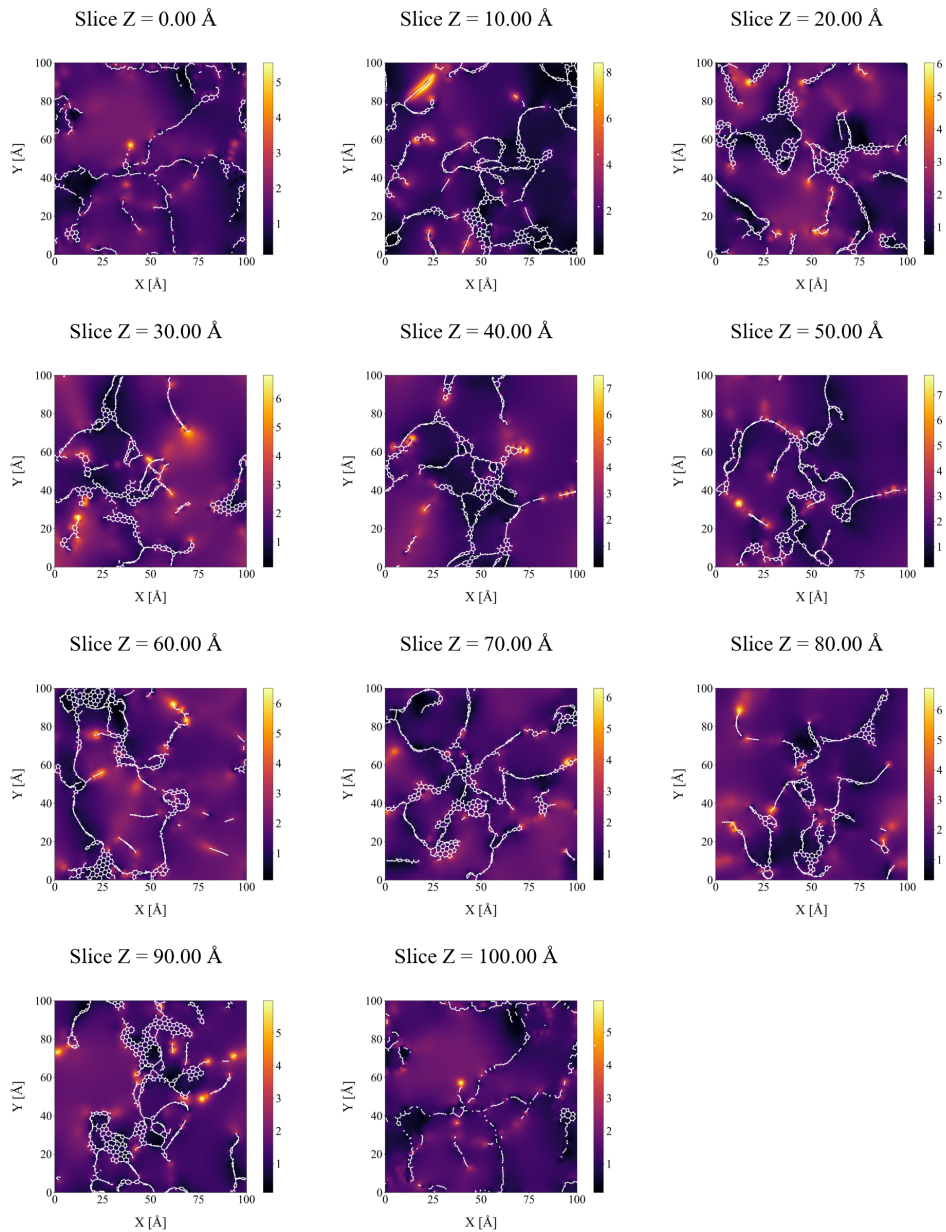


Figure S11: 2D field enhancement maps on XY planes for the uncured M34-2000 structure.

M34-2000 (Uncured) XZ

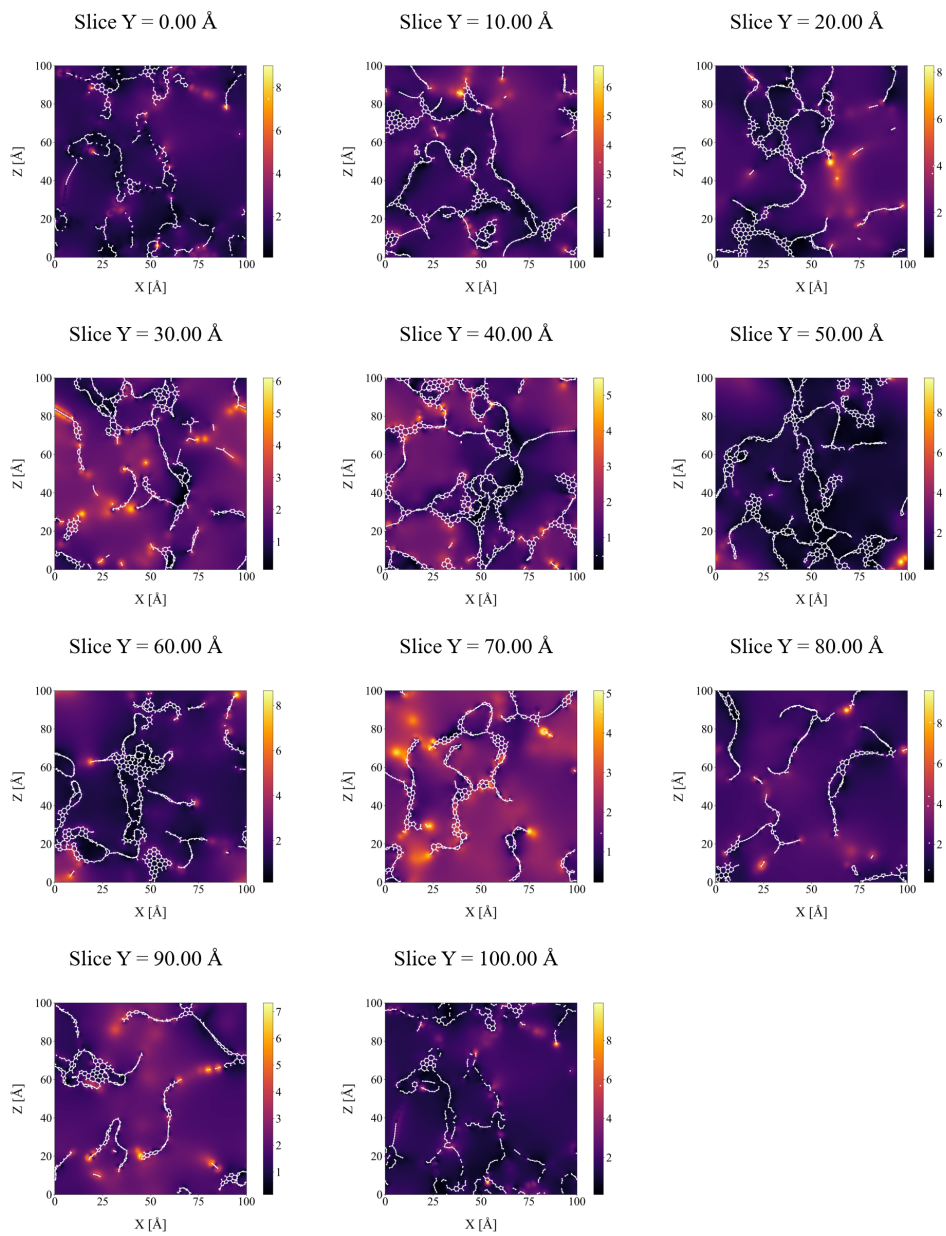


Figure S12: 2D field enhancement maps on XZ planes for the uncured M34-2000 structure.

M34-2000 (Uncured) YZ

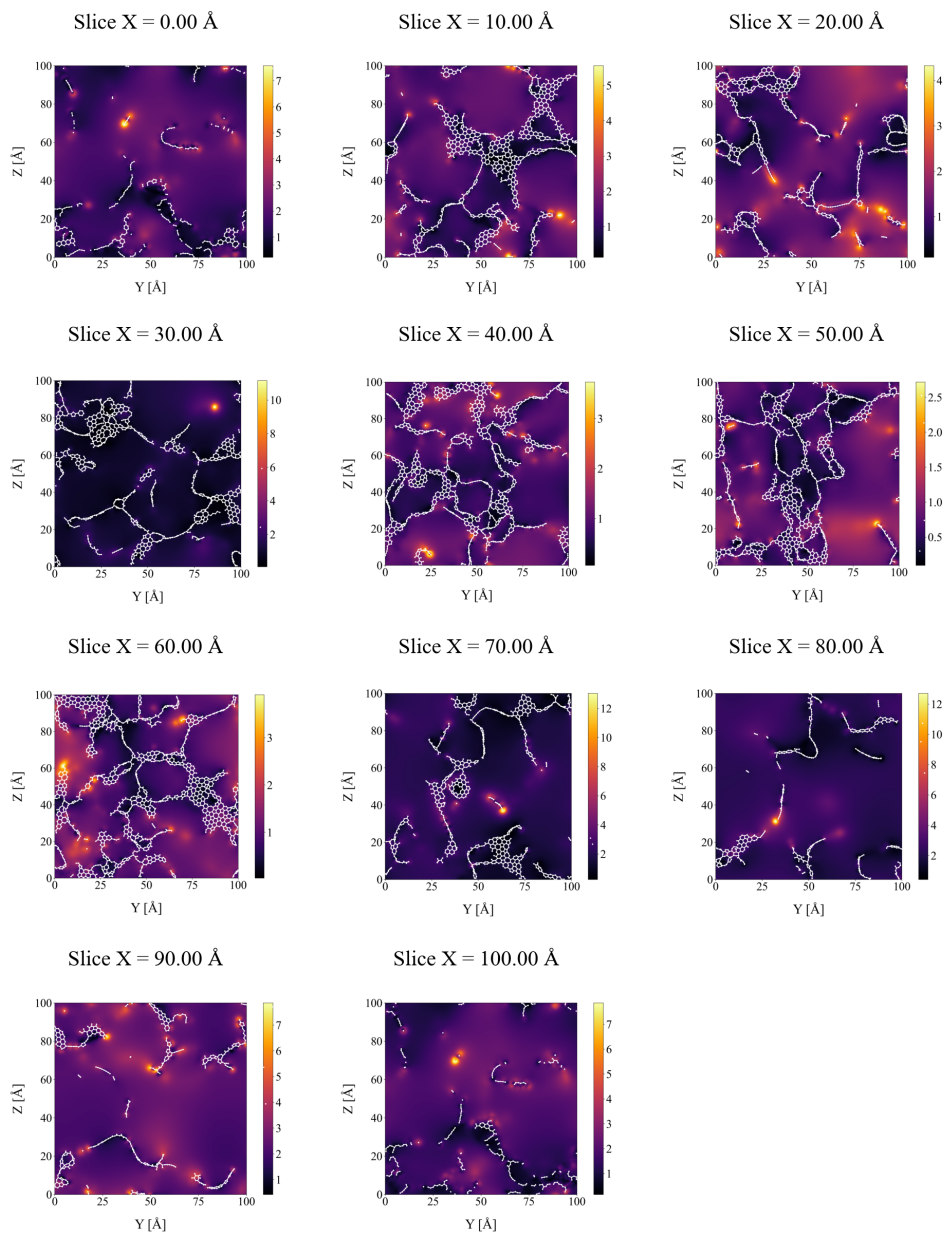


Figure S13: 2D field enhancement maps on YZ planes for the uncured M34-2000 structure.

S5.2.4 M34-2000 Cured

M34-2000 (Cured) XY

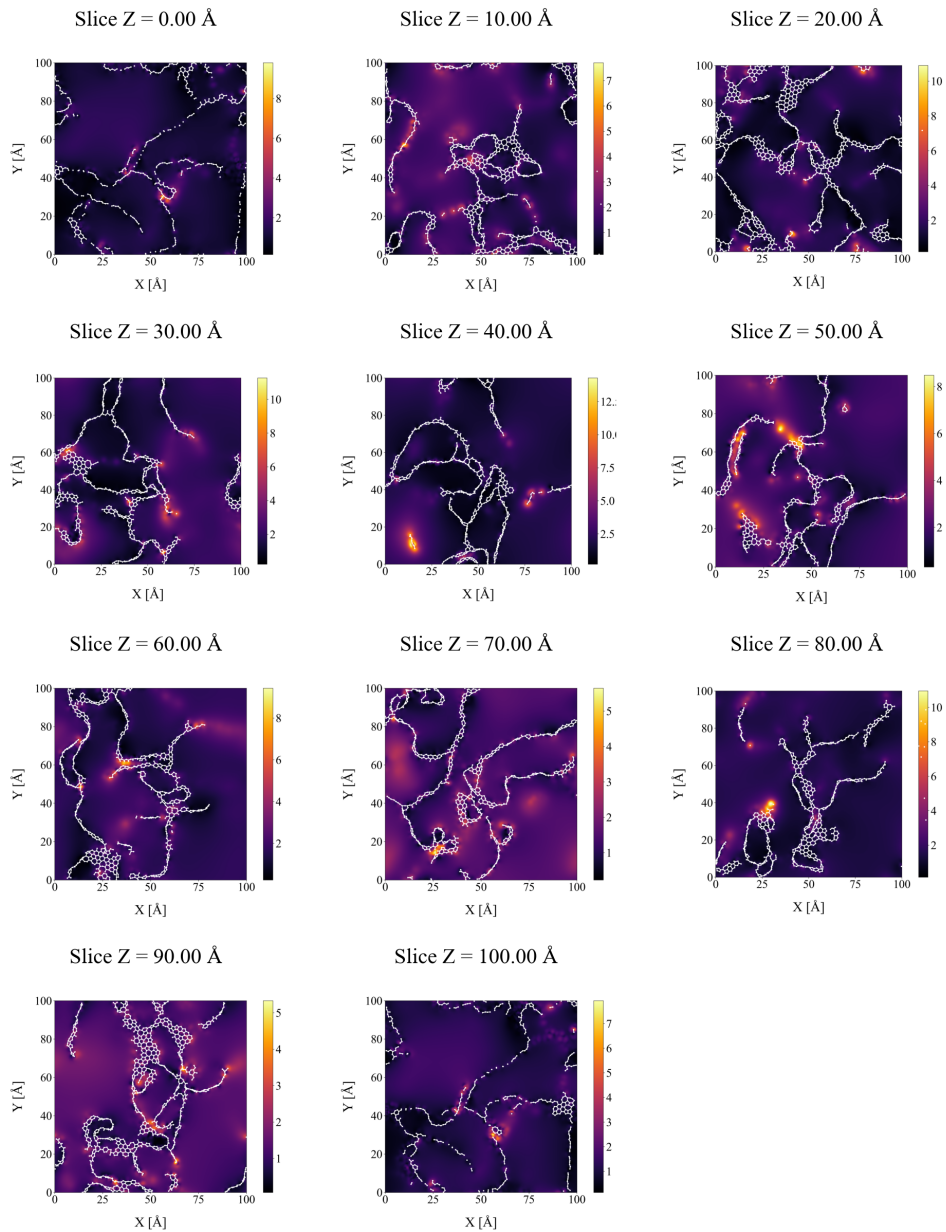


Figure S14: 2D field enhancement maps on XY planes for the cured M34-2000 structure.

M34-2000 (Cured) XZ

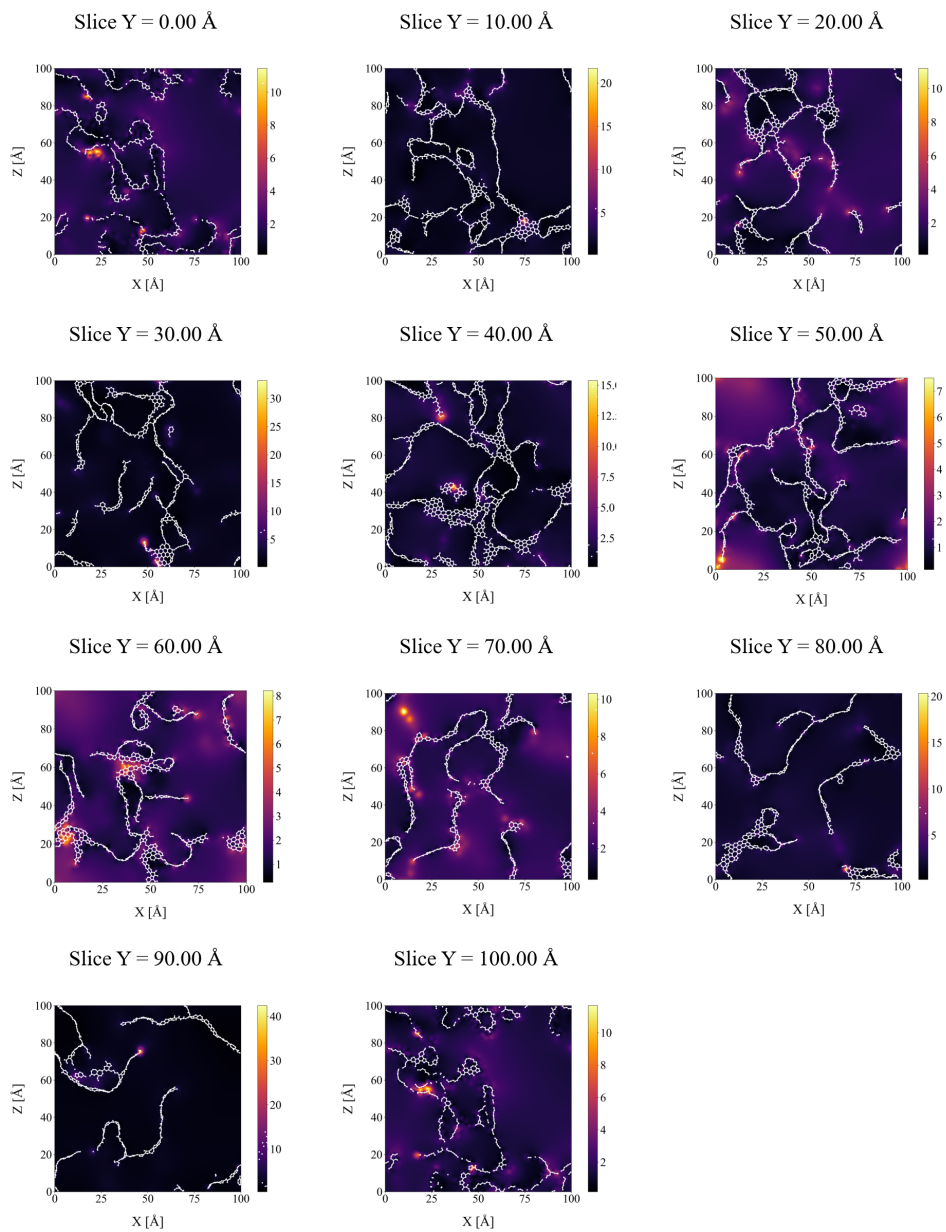


Figure S15: 2D field enhancement maps on XZ planes for the cured M34-2000 structure.

M34-2000 (Cured) YZ

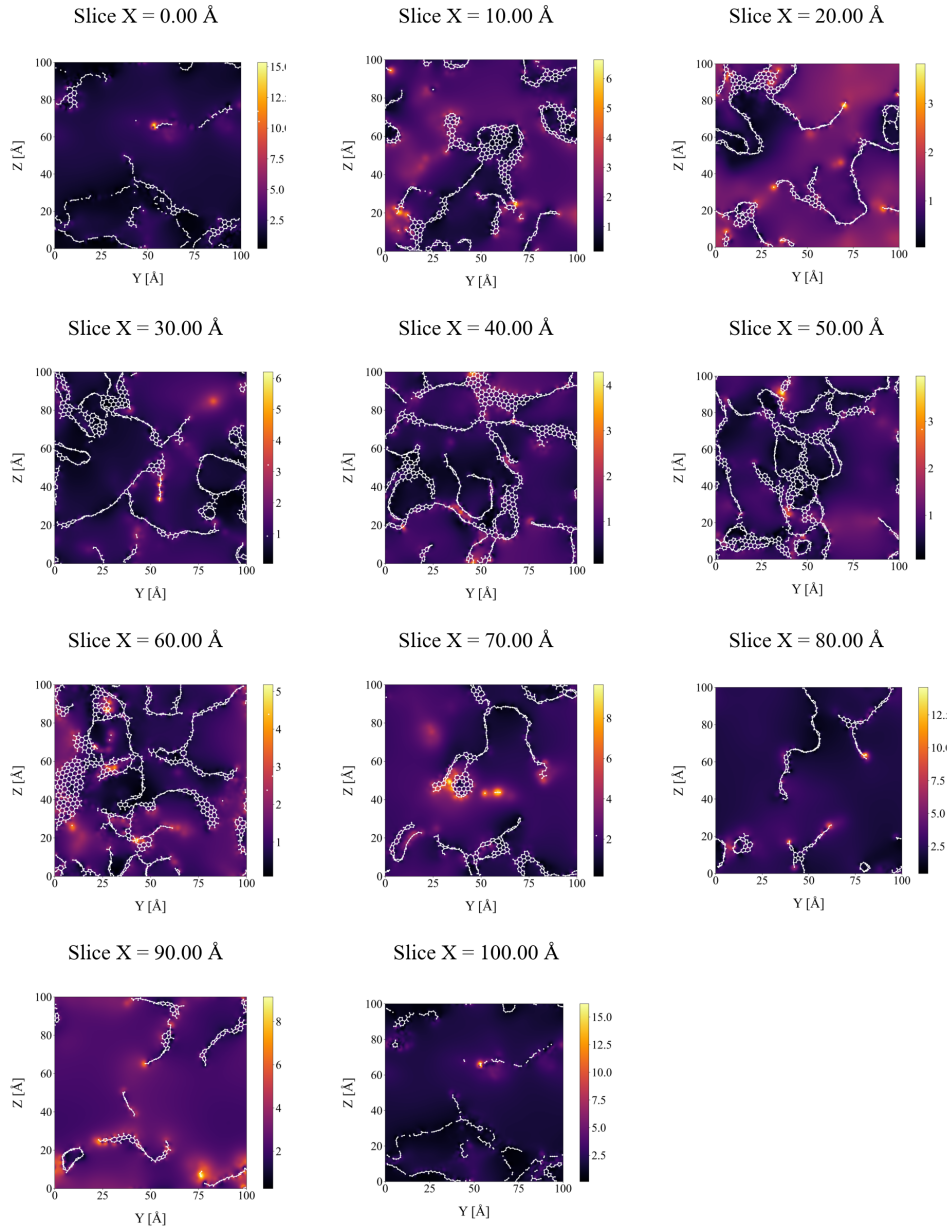


Figure S16: 2D field enhancement maps on YZ planes for the cured M34-2000 structure.

References

- (1) Monti, S.; Barcaro, G.; Goddard, W. A. I.; Fortunelli, A. Diverse Phases of Carbonaceous Materials from Stochastic Simulations. *ACS Nano* **2021**, *15*, 6369–6385.
- (2) Conter, G.; Monti, S.; Barcaro, G.; Goddard, W. A. I.; Fortunelli, A. Functionalized Amorphous Carbon Materials via Reactive Molecular Dynamics Simulations. *ACS Applied Materials & Interfaces* **2024**, *16*, 48043–48057.
- (3) Giovannini, T.; Bonatti, L.; Polini, M.; Cappelli, C. Graphene plasmonics: Fully atomistic approach for realistic structures. *J. Phys. Chem. Lett.* **2020**, *11*, 7595–7602.