

Evolution of Dissipative Regimes in Atomically Thin $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$ Superconductor

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Thermoelectric transport is widely used to study Abrikosov vortex dynamics in unconventional superconductors. However, only a few thermoelectric studies have been conducted near the dimensional crossover that occurs when the vortex-vortex interaction length scale becomes comparable to the sample size. Here, the effects of finite size on the dissipation mechanisms of the Nernst effect in the optimally doped $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$ high-temperature superconductor are reported, down to the atomic length limit. To access this regime, a new generation of thermoelectric chips based on silicon nitride microprinted circuit boards is developed. These chips ensure optimized signals while preventing sample deterioration. The results demonstrate that lateral confinement at the nanoscale can effectively reduce vortex dissipation. Investigating vortex dissipation at the micro- and nano-scale is essential for creating stable, miniaturized superconducting circuits.

1. Introduction

The creation of atomically thin van der Waals (vdW) superconducting $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$ (BSCCO) layers brought in created new possibilities for the investigation of high temperature topological superconductivity,^[1,2] superconducting fluctuations at the nanoscale and the exploration of topological defects.^[3] The vdW stacking of BSCCO thin crystals offers a unique platform for engineering a new generation of macroscopic quantum devices, ranging from superconducting nanowire single-photon detectors operating at high temperatures^[4,5] to twisted Josephson

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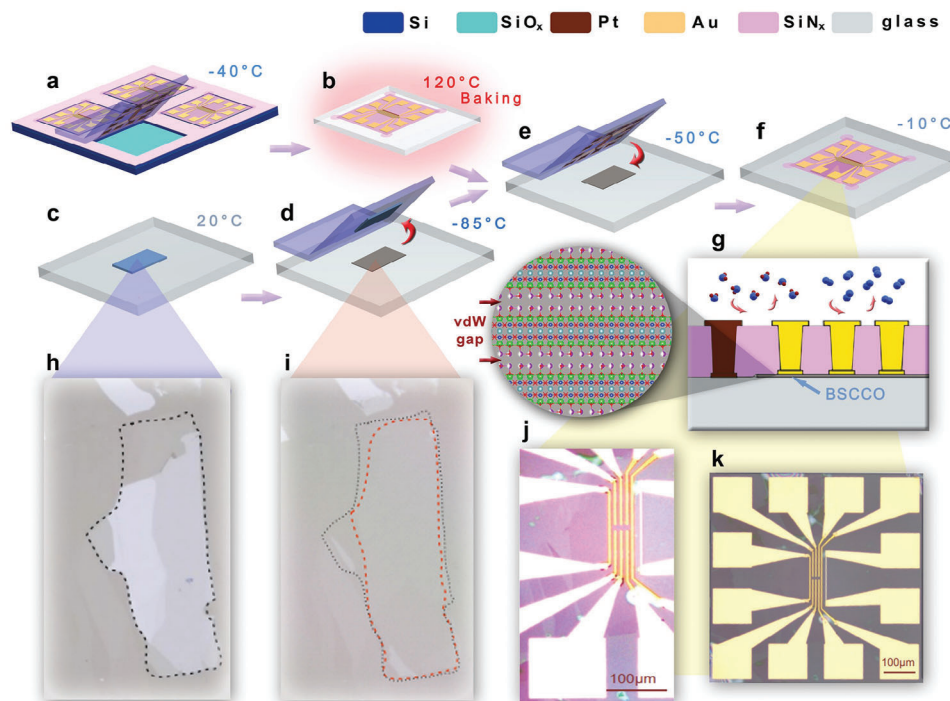


Figure 1. Realization of atomically thin BSCCO thermoelectric circuit. a–f) Overview of the fabrication process in the Ar-filled glovebox: a) Picking up the free standing NMB by PDMS at $-40\text{ }^{\circ}\text{C}$. b) Baking of the NMB at $120\text{ }^{\circ}\text{C}$ to eliminate moisture. c) Room temperature mechanical exfoliation of BSCCO flake onto a glass substrate. d) Cryogenic PDMS technique to thin down the flake at $-85\text{ }^{\circ}\text{C}$. e) Positioning of the NMB onto the glass substrate at $-50\text{ }^{\circ}\text{C}$. f) Controlled release of the NMB at $-10\text{ }^{\circ}\text{C}$. g) Schematic view of the NMB cross-section on the BSCCO flake, illustrating both the Au underlying contact adjacent with the flake and the Pt heater that is directly in contact with the glass substrate. In the zoom the crystal structure of 4.5 nm, which corresponds to 1.5 u.c. of BSCCO is presented. h–k) Optical images of the step by step fabrication: h) Initial exfoliated flake onto the glass substrate, underlined by a black dashed line. i) The flake was thinned down to 1.5 u.c. by cryogenic PDMS technique, preserving the huge lateral dimensions. The red dotted line is determining the new edge of the flake. j) Optical image in modified colors to show the position of the atomically thin flake below the NMB. k) Overall picture of on-chip thermoelectric device.

junctions with a tunable coupling.^[6–8] Formation of intrinsic Josephson junctions between twisted interfaces of BSCCO thin crystals has enabled the observation of spontaneously broken time-reversal symmetry at angles near 45° ,^[6] holding potential for realizing high-coherent superconducting quantum bits,^[9] chiral Majorana modes,^[10] and novel twisted symmetries.^[11]

Despite these promising developments, experimental investigations of vdW heterostructures are still slow because the current technology for fabricating the vdW circuits remains limited. This occurs mostly due to the challenges of fabricating ultra-thin BSCCO crystals and integrating them into complex electrical circuits. These systems are highly susceptible to degradation from reactions with moisture and oxygen dopant loss.^[12,13] Additional challenges arise due to more subtle issues such as detrimental changes in the ordering of oxygen and this spatial ordering changes interstitials^[14,15] above $-73\text{ }^{\circ}\text{C}$ and spatial ordering changes of the incommensurate superlattice modulation.^[16] To mitigate these issues, noninvasive optical pump-probe approaches have been opted to study the superconductivity in atomically thin BSCCO crystals.^[17,18] Furthermore, in order to realize electrical measurements, stencil mask and low-power thermal evaporation have been employed for the fabrication of few electrical contacts in atomically thin BSCCO nanodevices, without involving chemicals or heating process.^[2] The introduction

of the cryogenic exfoliation methodology allowing for picking-up and assembly of sensitive van der Waals heterostructures,^[6–8] evidenced the potential of this technique for transformative applications.^[19] However, the integration of the advanced circuits required to move beyond the stencil mask approach. A fabrication technique relying on the cryogenic dry transfer of printable circuits embedded into silicon nitride membranes has therefore been developed.^[20,21]

Ideal applications for this technology are thermoelectric circuits, requiring spatial precision at the micro-/nano-scale and a variety of elements like heaters, thermometers and electrical leads, which are often not compatible with the chemistry of the ultra-thin BSCCO crystals. Besides their natural application in energy harvesting and power generation,^[22] thermoelectric devices have been proven to be remarkably useful for exploring several condensed matter systems including the inert 2D materials,^[23] topological non-trivial compounds,^[24] and unconventional superconductors. In particular, the transverse thermoelectric effect and Nernst effect have been widely employed in the field of unconventional superconductivity to investigate fluctuations, symmetry breaking,^[25–27] pseudogap phase^[28] and vortex dynamics.^[29–31] Among the high- T_c superconductors, bulk BSCCO is quite special because being extremely anisotropic^[32,33] and having large Ginzburg number and significant quantum

resistance, it exhibits unique vortex transitions,^[34,35] which are influenced by thermal and quantum fluctuations, as well as by quenched disorder.^[36]

Learning how to control the nature of the dissipative regime can improve the performance of atomically thin cuprate superconducting circuits and the Nernst effect is a powerful tool to reach this goal. To that end, we realize silicon nitride microprinted circuit boards to perform thermoelectric measurements on atomically thin BSCCO samples and probe the vortex dynamics and dissipation regimes in presence of the effects of the sample finite sizes.

2. Results and Discussion

To realize the on-chip Nernst experimental setup, we pick up the fabricated SiN microcircuit board at $-40\text{ }^{\circ}\text{C}$ using a polydimethylsiloxane (PDMS) stamp and bake it at $120\text{ }^{\circ}\text{C}$ to remove water molecules, as schematically shown in Figure 1a,b. The details of the circuit board fabrication are given in the Supporting Information. Following this procedure, the BSCCO crystal with optimal doping is mechanically exfoliated onto a glass substrate within an Argon-filled glovebox (Figure 1c) and is then further thinned down at cryogenic temperatures using another PDMS stamp, see Figure 1d. This step reduces the flake thickness to the atomic level while preserving its lateral dimensions. We successfully decrease the thickness of the flake depicted in Figure 1h down to 4.5 nm , which corresponds to 1.5 u.c. , as shown in Figure 1i, without causing any breaks. This is possible because the glass substrate provides stronger vdW forces with the flake as compared to red forces developing in the silicon substrate used in previous studies.^[7,8,20] Immediately after that, the nanomembrane (NMB) featuring the metallic contacts underneath are transferred and freely released from the stamp on top of the flake at low temperatures, as depicted in Figure 1e,f,g. The quick treatment guarantees a pristine interface between the metal contacts and thin BSCCO crystal, thereby preserving its superconducting properties and ensuring an optimal electrical signal.^[20] The optical micrograph of the device is shown in Figure 1j,k. The microcircuit consists of a resistive heater in contact with the substrate, which provides a dissipate power in the close vicinity of one side of the crystal and a set of electrodes measuring the transverse, V_T , and longitudinal, V_L , electric voltages.

Figure 2, shows our measured results of the thermoelectric effect. We present the time dependence of V_T at 80 K , when switching the heater on and off twice, as depicted in Figure 2a,b. The two Cr/Au stripes, $20\text{ }\mu\text{m}$ apart and $15\text{ }\mu\text{m}$ from the heater, act as hot and cold thermometers (inset of Figure 2a). The local temperature was inferred by four-probe resistance measurements, after a calibration of its temperature dependence from room to cryogenic temperatures (see the Figure S3, Supporting Information, for further details). Figure 2c presents the local temperature variation at base temperature of 80 K as a function of time. When the heater is turned on, the local temperature increases by a few degrees, establishing a temperature difference ΔT between the two thermometers, as shown in Figure 2d. The observed ΔT is consistent with COMSOL simulations reported in the Supporting Information. The V_T signal in Figure 2e exhibits a sign change when the external out-of-plane magnetic field of 5 T is reversed, which is consistent with the expected behavior for a transverse signal that

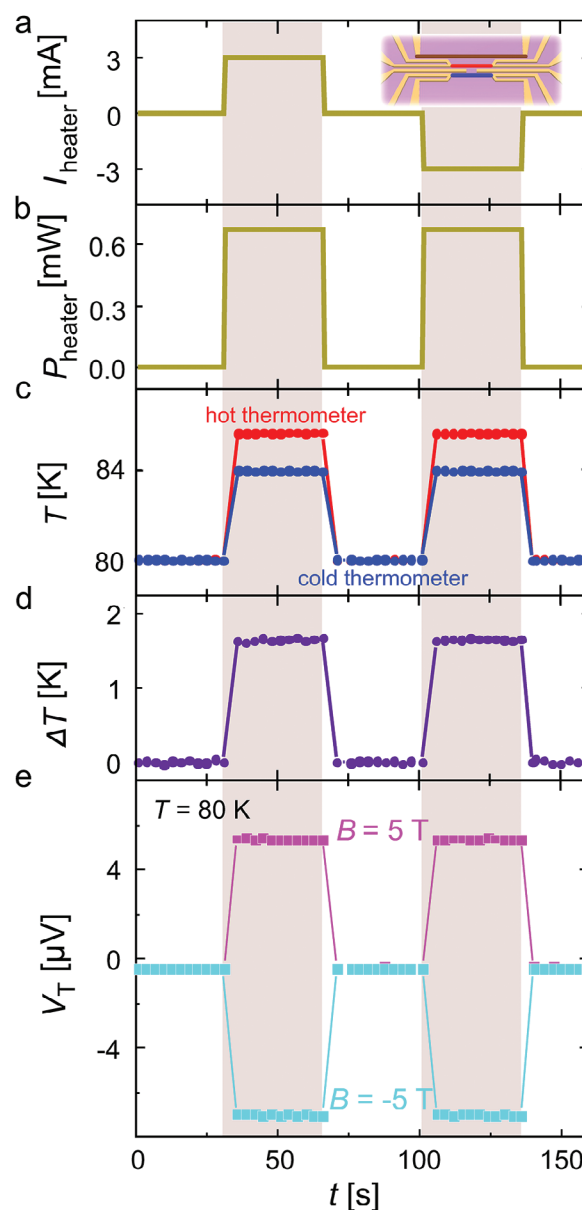


Figure 2. Transport properties of the microprinted thermoelectric circuit. a) Current flowing in the heater as a function of time. Inset, displaying the schematics of the metallic pattern underneath the NMB shows the heater, the transverse electric contacts on the flake, and the hot (red) and cold (blue) thermometers (inset of Figure 2a). b) The time dependence of the power dissipated into the heater. c) The local temperature obtained by hot and the cold thermometers as a function of time. d) Time dependence of the temperature difference between the two thermometers. e) Transverse thermoelectric voltage at $T = 80\text{ K}$, showing a sign change with an applied out-of-plane magnetic field $B = \pm 5\text{ T}$.

is typically an odd function of the magnetic field. This property allows us to antisymmetrize the positive and negative magnetic field data to estimate the Nernst voltage variation ΔV_T . Similarly, the time dependence of the Seebeck signal is reported in the Supporting Information (Figure S2). To calculate the absolute value of the Nernst coefficient S_{xy} for our thermal transport, the thermal gradient generated by the heating current must be quantified

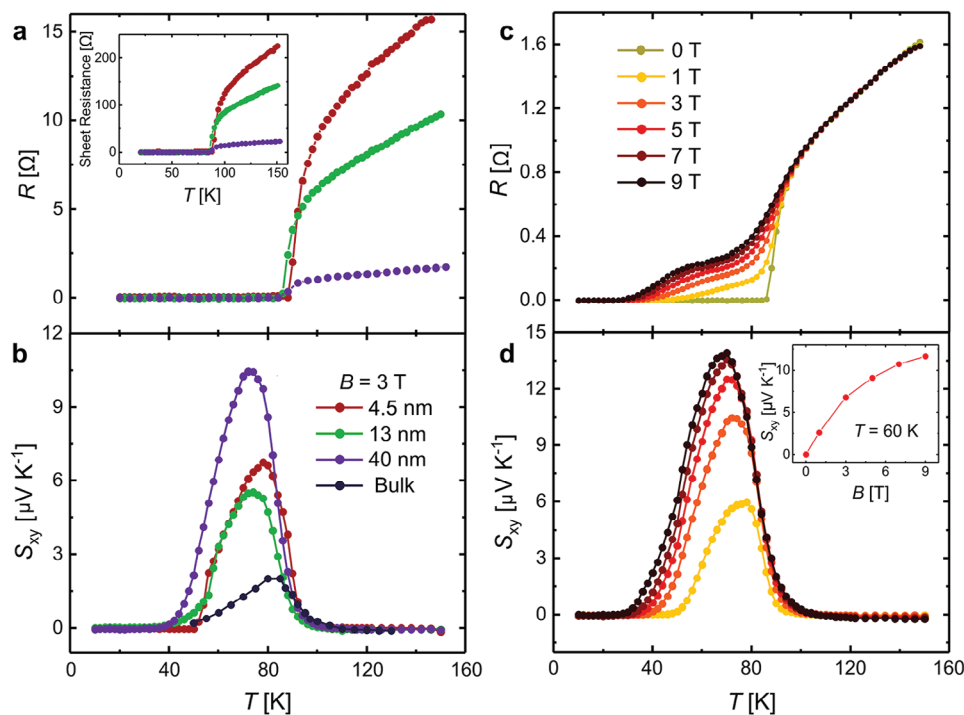


Figure 3. Size dependent evolution of the Nernst effect. a) Four-probe resistance of the BSCCO flakes as a function of the temperature. Inset: temperature dependence of the sheet resistance for all the previous devices calculated as ρ/t , where t is the thickness of the crystals. All samples are measured under identical geometric conditions. b) Temperature dependence of the Nernst effect at $B = 3$ T for BSCCO flakes in (a) with different thicknesses compared with optimally doped bulk adapted from ref. [30]. c, d) Temperature dependence of (c) the resistance and of (d) the Nernst effect of 40 nm-thick flake under various applied magnetic fields up to 9 T. Inset: magnetic field dependence of the Nernst effect at $T = 60$ K.

once for all the temperatures under study, see Supporting Information for further details.

To execute our thermal transport study, we fabricate, in total, three devices for three different BSCCO crystal thicknesses: 4.5, 13, 40 nm. Figure 3a presents the temperature dependence of the four-probe resistance of these devices across the superconducting transition and, in the inset, the sheet resistance is presented. Notably, thinner crystals exhibit higher sheet resistance and sharper superconducting transitions, as reported in ref. [2]. In Figure 3b, the temperature dependence of the Nernst effect is reported as a function of the thickness at $B = 3$ T compared to the bulk one (adapted from ref. [30]). In the normal state S_{xy} is small. By decreasing the temperature, a pronounced positive peak below the critical temperature appears, which corresponds to the motion of depinned vortices. Finally, S_{xy} vanishes at the lowest temperatures. The typical signature of mobile superconducting vortices in the mixed state of cuprates^[30,37] is clearly seen in all studied samples.

The intensity of the Nernst effect is significantly amplified in flakes as compared to that in the standard bulk samples,^[30] see also other experimental data in bulk BSCCO.^[38,39] Remarkably, the peak value for the 40 nm-thick flake is nearly an order of magnitude greater than the peak in the bulk and twice as much as that of the 4.5 nm- and 13 nm-thick devices.

Interestingly, Hall effect measurements on atomically thin BSCCO flakes exhibit a sign reversal roughly in the same temperature range and the region of the H - T plane where the Hall voltage is negative and increases its magnitude when flake

thickness decreases.^[2] As normal excitations inside and outside vortex cores contribute to the Hall effect both below T_c and above T_c in the vortex-like fluctuation regime, the sign reversal indicates flux-flow dominated transport, occurring when the negative contribution from vortex cores dominates over the positive normal state contribution. The thickness dependence is attributed to the smaller mobility of the outermost atomic layers, whose relative contribution increases with decreasing thickness.^[2] However, the similarity between Hall and Nernst transverse effects cannot be extended further, as Hall effect reflects the sign of charge carriers, whereas vortex Nernst effect does not achieve a more comprehensive understanding of the work of the 40 nm-thick device which exhibits the most pronounced Nernst effect, we show in Figure 3c,d the temperature dependence of both resistance and Nernst effect as a function of magnetic field up to 9 T. Applying the external field broadens the superconducting transition,^[38] and the magnitude of the Nernst effect in the mixed state increases with field, see inset in Figure 3d.

The Nernst coefficient $S_{xy} = E_y/(\nabla_x T)$ in the mixed state, where E_y is the y-component of the electric field that results from the magnetic field's z-component B_z , which is determined by the vortex dissipative motion. Thus, an enhancement of the Nernst signal indicates a growing ratio of driving to pinning forces, reflecting their competition.

Note the challenging trends of changing S_{xy} across the three flakes in our experiment: all the flakes present an enlarged Nernst coefficient with respect to the bulk sample, suggesting a crucial

effect of the spatial confinement. However, among the flakes, the 40 nm-one, presents the largest S_{xy} , proving that the Nernst coefficient is not simply scaled by the sample thickness. This evidences the fact that the vortex motion must be also influenced by the lateral confinement, giving rise to a complex scenario in which different pinning mechanisms are competing over different lengthscales. It is interesting to remark that our samples are all much thinner than the typical London penetration depth λ of BSCCO, which is about 270 nm.^[40,41] In this regime, the vortex–vortex interaction is mainly mediated by the magnetic stray field and the scale of the screening of the vortex in-plane supercurrents is set by the Pearl length $\Lambda = 2\lambda^2/d$, rather than by λ .^[42] In our samples Λ ranges from few to tens of microns, being comparable with the characteristic lateral size of the flakes L . Note that L represents the smallest length of the flake. (see **Table 1**). Thus, we attempt to represent our experimental Nernst data as a function of the ratio $L/2\Lambda$, which contains different lengthscales (L , d and λ), as shown in **Figure 4**. However, though a trend is found, the role of Λ is expected to be relevant only at very small fields, when a limited number of vortices are within the interaction range. Therefore other mechanisms, relevant at higher fields must be considered. In this regard, it is established that the dissipative motion of vortices across the finite-width superconducting strip involves an interplay between defects near the strip’s edges, which stimulate vortex entry and exit,^[43,44] and the standard pinning effects of defects nearer to the strip’s center, which are expected to determine vortex motion within the “depth” of the strip. In this interplay, not only the sample width, but also edge morphology and defect distribution near the edges, play key roles.

Recent reports show a systematic decrease of the Nernst effect with doping in atomically thin samples.^[3] The relevance of such effects has been demonstrated for sub-micrometric strips.^[45] In our work, we present experimental evidence that the Nernst coefficient S_{xy} increases with the lateral width L of the atomically thin samples. This observation probably indicates the growing effect of pinning in the central region of the strip (pinning effects decrease near the edges of the strip). The control of the sample-edges geometry becomes therefore an important control knob for reducing the dissipation in possible superconducting circuits^[9] and improving photon detectors^[4] based on cuprate van der Waals artificial systems. This stresses the need for careful investigations of the details of pinning phenomena, particularly the possible interplay between different pinning regimes and their influence on the Nernst effect in strips of finite lateral width. This study, including the detailed investigation of the effects of collective pinning in the finite-width system and the possible emergence of the long range interactions, decaying as the inverse distance $1/r$ between vortices^[42] along with a detailed analysis of the behavior of the Nernst coefficient within the framework of pinning theory,^[36,45,46] will be the subject of forthcoming research.

3. Experimental Section

Device Fabrication: The exfoliated flakes were obtained within an Ar-filled glovebox from a bulk single crystal of BSCCO and transferred from the scotch tape on a glass substrate, i.e., quartz monocrystals with var-

Table 1. Characteristic lengths of the BSCCO flakes under study.

d [nm]	L [μm]	Λ [μm]	$L/2\Lambda$	$S_{xy}@3\text{T}$ [$\mu\text{V K}^{-1}$]
4.5	100	32.4	1.54	6.74
13	56	11.2	2.50	5.53
40	155	3.65	22.3	10.44

ious different crystal directions formed via hydrothermal synthesis. The substrate was pre-treated with oxygen plasma to optimize the flake adhesion and placed on a hotplate at 150 °C for several hours to remove the moisture. The thicknesses of the flakes were estimated, based on the RGB calibration by the optical microscope. Nevertheless, the actual thickness was accurately determined using atomic force microscopy (AFM) after the completion of the transport measurements. To successfully perform the cryogenic thinning described in the main text, the glass substrate was placed on the stage and fixed at –85 °C. This temperature, which is low enough to freeze the interlayer O_2 dopants, was chosen based on the dew point of the glovebox, –97 °C. Note that the cryogenic PDMS treatment at –85 °C was employed to remove thick flakes adjacent to the target flake, for arranging the optimal NMB landing. The precise alignment of the NMB at –50 °C with the flake was facilitated by a motorized micro manipulator. After removing the PDMS at –10 °C, the device reached room temperature before removing from the glovebox. Finally, the glass substrate was affixed to the chip carrier using silver paste and wire bonded with the automatic BONDTEC 5630i.

Transport Measurements: The transport measurements were performed in a 9 T Quantum Design Physical Property Measurement System (PPMS). For the resistivity measurements, a standard four-probe method was applied using external SR830 lock-in amplifiers. For the on-chip Nernst effect measurements, both the transverse thermoelectric voltage, ΔV_T , and the temperature difference across the flake, ΔT were evaluated. First, ΔV_T was obtained for all the temperatures under study, following the procedure described in the main text, see **Figure 1**, and performing an antisymmetrization of two curves at positive and negative magnetic fields. Then, the calibration of the temperature gradient from room to low temperature was done once with the particular patterned NMB reported in

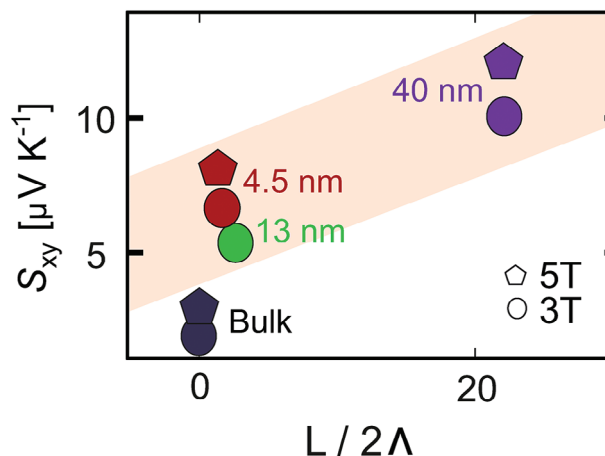


Figure 4. Vortex distribution depending on the sample dimensions. Experimental evolution of the Nernst coefficient S_{xy} as a function of L and normalized over 2Λ for different magnetic fields $B = 5$ T and $B = 3$ T. S_{xy} is maximal in correspondence of the collective pinning regime, while it diminishes due to the effect of the finite lateral sizes. The solid black symbols related to the bulk samples^[30] are set as a reference for the limit of very large thickness, specifically their horizontal position is calculated as $\frac{L}{2\lambda}$, replacing Λ by λ .

Figure 2. A calibration of the four probe resistance of the hot and cold thermometers was done to evaluate the local temperature by four-probe resistance measurements, see Figure 2f,g. All thermoelectric measurements were performed using an external current source KEYTHLEY 4200 and nanovoltmeters KEYTHLEY 2182A. All the samples were measured with identical NMBs.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Author Contributions

N.P. conceived and designed the experiment; S.S. performed the fabrication. C.N.S. and S.S. initiated the nanomembrane fabrication. S.S. and M.C. performed the measurements and analyzed the data with the contribution of F.C. and I.P. The cuprate crystals were provided by G.G. The fabrication procedure were discussed by S.S., M.C., T.C., M.M., Y.L., K.N., N. P., and the results were discussed by F.C., I.P., K.N., N.P., V.M.V. The manuscript was written by S.S., M.C., M.M., V.M.V., I.P., K.N., F.C., N.P. All authors discussed the manuscript.

Data Availability Statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Keywords

air-sensitive materials nanofabrication, cuprate superconductivity, thermoelectric transport, van der Waals materials, vortex physics, dissipation in superconductors

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