

Spin-dependent electron-phonon coupling in the valence band of single-layer WS₂

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The absence of inversion symmetry leads to a strong spin-orbit splitting of the upper valence band of semiconducting single-layer transition-metal dichalcogenides such as MoS₂ or WS₂. This permits a direct comparison of the electron-phonon coupling strength in states that only differ by their spin. Here, the electron-phonon coupling in the valence band maximum of single-layer WS₂ is studied by first-principles calculations and angle-resolved photoemission. The coupling strength is found to be drastically different for the two spin-split branches, with calculated values of $\lambda_K = 0.0021$ and 0.40 for the upper and lower spin-split valence band of the freestanding layer, respectively. This difference is somewhat reduced when including scattering processes involving the Au(111) substrate present in the experiment but it remains significant, in good agreement with the experimental results.

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The electronic structure of semiconducting single-layer (SL) transition-metal dichalcogenides with a trigonal prismatic structure (MoS₂, WS₂) resembles that of graphene in certain respects, but with a sizable band gap [1–3]. On closer inspection, however, an important difference from graphene is the lack of inversion symmetry which, combined with the presence of heavy atoms in the materials, leads to a lifting of the spin degeneracy in the band structure. This is especially important near the valence band (VB) maximum at K , where the spin splitting can be substantial (see Fig. 1). This spin splitting, combined with the two valleys at K and K' , gives rise to new spinlike quantum degrees of freedom [4] that could be exploited for storing or transmitting quantum information. Moreover, in hole-doped materials, the valence band's spin texture can have consequences ranging from increased hole mobility to topological superconductivity [5].

The strong spin splitting in the band structure also provides a unique opportunity to study the electron-phonon (el-ph) coupling in a system of states that only differ by their spin [6]. In this Rapid Communication, we report theoretical and experimental results for the el-ph coupling in SL WS₂ and find that the coupling strength is strongly dependent on the branch of the spin-split band structure. While this might appear surprising at first glance, it can be explained by a combination of spin-protected scattering and, more importantly, phase space restrictions. Our findings are directly relevant to hole transport in single-layer devices, to the generation of a long-lived valley polarization at elevated temperatures [7–9], and to the yet-to-be-demonstrated superconductivity in hole-doped materials [10].

The expected el-ph scattering contributions for the VB maximum of SL WS₂ are shown in Fig. 1 in a schematic representation of the band structure. The important features for the band structure are the two spin-split VB maxima at K and K' . Due to time-reversal symmetry, the spin structure is reversed at these two points. In the following, the spin-split bands at K will be referred to as the “upper” and “lower” bands, the “upper” band being the absolute VB maximum. Situated energetically between the maxima of the upper and lower bands, there is also a local VB maximum at Γ which is spin degenerate. Consider now how a hole can be filled by an electron with the help of crystal momentum (and energy) of a phonon. A hole near the top of the upper band at K can only be filled by an electron at higher binding energy, a scenario which requires the absorption of a thermally excited phonon. This electron has to come either from the same band at higher binding energy (process No. 1) or from the band at K' (process No. 2). The latter intervalley-scattering process would require a spin flip, or at least a considerable change in the spin-expectation value, making the process extremely unlikely [11]. Note that no el-ph scattering processes from the lower band or the band at Γ are possible because the energy difference between these bands and the upper band (≈ 0.43 eV and ≈ 0.22 eV, respectively) far exceed the maximum phonon energy of ≈ 52 meV [12,13]. The situation is drastically different in the lower band, for which several additional scattering processes are possible—e.g., from the VB at Γ (process No. 4); or, from a state in the upper branch away from K (process No. 3), for which the spin polarization is lower than it is exactly at K [6,13]; or, from the lower band near K' (not shown in the figure). Moreover, all of these processes can also proceed via phonon emission at low temperatures. Based on this simple picture, one would expect a substantially weaker el-ph coupling in the upper band than in the lower band, and this will also be confirmed by our findings. Note that this result

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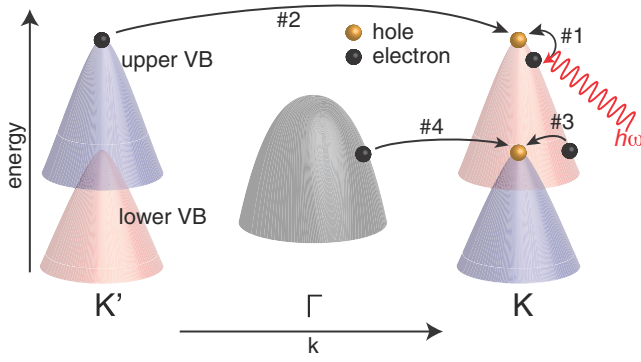


FIG. 1. Schematic valence band for SL WS₂ with the absolute valence band (VB) maxima at K and K' and a local maximum at Γ . The VB at K and K' are spin split with the color indicating the spin direction. The VB at Γ is spin-degenerate. el-ph scattering processes to fill holes at the top of the spin-split band at K are illustrated. In process No. 1, an electron is scattered into the hole by absorbing a phonon (red line). For the other scattering processes, the phonons are omitted for clarity.

is only partly a direct consequence of the state's spin texture, even though the upper and lower bands only differ by the spin part of their wave function. An important consideration is also the restriction of scattering phase space—i.e., the number of available final states—which can be a dominant factor for the el-ph coupling strength [14].

The electronic structure and vibrational properties of SL WS₂ and of the Au(111) substrate used in the experiments were calculated from first principles within density functional theory, as implemented in the QUANTUM ESPRESSO code [15]. Relativistic effects, e.g., spin-orbit coupling, were treated self-consistently and are accounted for in all calculations. Based on the electronic and vibrational properties, the el-ph coupling was obtained within a modified version of the EPW code [16,17], either for the freestanding SL WS₂ or for the states in the SL in the presence of the Au(111) substrate.

The *a priori* state-dependent, temperature-dependent phonon-induced electronic linewidth Γ_{nk} is closely related to the imaginary part of the lowest order el-ph self-energy Σ''_{nk} for the Bloch state of energy ε_{nk} at band n and momentum \mathbf{k} and given by

$$\begin{aligned} \Gamma_{nk}(T) &= 2\Sigma''_{nk}(T) = 2\pi \sum_{mv} \int_{\text{BZ}} \frac{d\mathbf{q}}{\Omega_{\text{BZ}}} |g_{mn,v}(\mathbf{k}, \mathbf{q})|^2 \\ &\times \{ [n_{\mathbf{q}v}(T) + f_{m\mathbf{k}+\mathbf{q}}(T)] \delta(\varepsilon_{nk} - \varepsilon_{m\mathbf{k}+\mathbf{q}} + \omega_{\mathbf{q}v}) \\ &+ [n_{\mathbf{q}v}(T) + 1 - f_{m\mathbf{k}+\mathbf{q}}(T)] \delta(\varepsilon_{nk} - \varepsilon_{m\mathbf{k}+\mathbf{q}} - \omega_{\mathbf{q}v}) \}, \end{aligned} \quad (1)$$

where $g_{mn,v}(\mathbf{k}, \mathbf{q})$ are the el-ph scattering matrix elements; n and f are Bose and Fermi functions, respectively; ε and ω are noninteracting electron and phonon energies, respectively. The electron-phonon coupling strength λ_{nk} is essentially counting the possible scattering processes for a chosen initial state (\mathbf{k}, n) into possible final states, weighted by a squared matrix

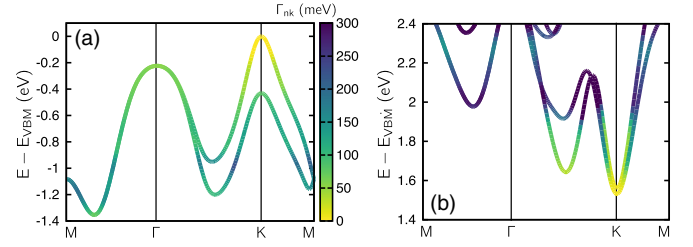


FIG. 2. (a) Calculated valence-band structure for freestanding SL WS₂. (b) Calculated conduction-band structure for freestanding SL WS₂. The color coding of the bands represents the el-ph coupling induced linewidth (or inverse lifetime $\tau_k = \frac{\hbar}{\Gamma_k}$) of the state at 300 K and applies to holes and electrons in (a) and (b), respectively.

element:

$$\begin{aligned} \lambda_{nk} &= \sum_{mv} \int_{\text{BZ}} \frac{d\mathbf{q}}{\Omega_{\text{BZ}} \omega_{\mathbf{q}v}} |g_{mn,v}(\mathbf{k}, \mathbf{q})|^2 \\ &\times \delta(\varepsilon_{nk} - \varepsilon_{m\mathbf{k}+\mathbf{q}} \pm \omega_{\mathbf{q}v}). \end{aligned} \quad (2)$$

Note that λ_{nk} has the character of an energy- and k -dependent general coupling constant and is thus a more general quantity than the mass-enhancement parameter at the Fermi surface of a metal [18]. A signature of the electron-phonon interaction is the linear temperature dependence of Γ_{nk} at high temperatures. The latter is a direct consequence of the T dependence of the phonon occupation numbers—i.e., $n_{\mathbf{q}v}(T \rightarrow \infty) \propto \frac{k_B T}{\omega_{\mathbf{q}v}}$. Comparing Eqs. (1) and (2), one readily obtains $\Gamma_{nk}(T) = 2\pi \lambda_{nk} k_B T$ [19].

In the experimental part of the current study, SL WS₂ was epitaxially grown on Au(111) following the well-established procedure of Refs. [20–22]. Angle-resolved photoemission spectroscopy data were collected on the SGM-3 beamline of ASTRID2 [23]. The energy and angular resolution were better than 30 meV and 0.2°, respectively.

The calculations for freestanding SL WS₂ are presented in Fig. 2. Figure 2(a) shows the calculated VB dispersion with a color coding that represents the linewidth at $T = 300$ K, calculated using Eq. (1). This figure already confirms the simple picture discussed in connection with Fig. 1: We find a very narrow linewidth for the top of the upper band near K (a long hole lifetime) and a substantially increased linewidth for the top of the lower band. Phase space considerations also appear to be significant for other states at higher binding energies, with particularly short lifetimes close to critical points in the density of states. Figure 2(b) shows the corresponding calculation for the conduction band (CB). Here the spin splitting is much smaller (28 meV) and, moreover, the absolute CB minimum is found in the vicinity of the local minimum at the Q point. Due to these two factors, the el-ph induced broadening for the two branches is much more similar, and in total larger, than in the VB.

Figure 3(d) shows the calculated linewidth for the upper and lower bands at K as a function of temperature, demonstrating once again the much stronger el-ph coupling for the lower band. The linear high-temperature regime appears to be reached above ≈ 300 K, and a linear fit to the linewidth in the experimentally accessible temperature range between 300 and 600 K yields $\lambda_K = 0.0021$ ($\lambda_K = 0.40$) for the upper (lower)

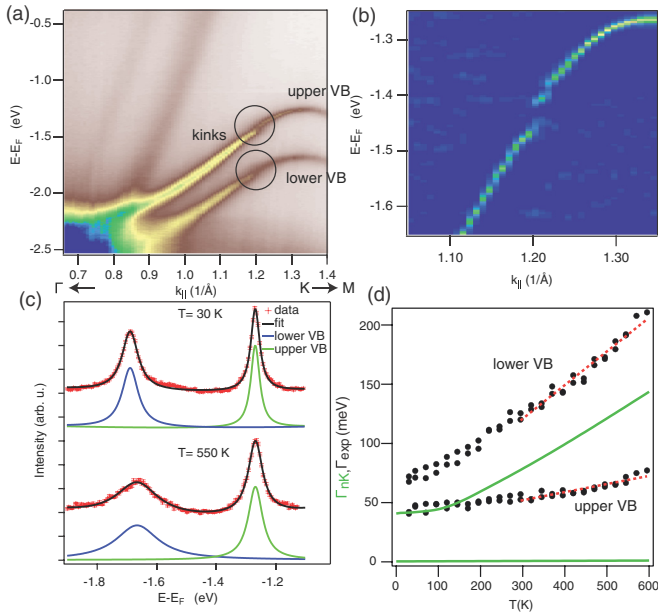


FIG. 3. (a) Photoemission intensity along $\Gamma-K$ at 30 K. The positions of kinks in the WS_2 bands are marked. (b) Curvature of the photoemission data presented in (a) [29], showing the kink in the upper valence band. (c) EDCs through K at low and high temperature. The markers are the data points. The resulting fit with a polynomial background and two Lorentzian peaks is also shown. (d) Temperature-dependent Lorentzian linewidth of the two bands in an energy distribution curve through K (markers). The solid lines show the calculation for the freestanding layer from Fig. 2(a). The dashed lines are a fit of the experimental data at high temperature ($T > 300$ K.)

VB, respectively. It turns out, however, that the dependence is not completely linear, due to high-energy phonons not being equally occupied in this temperature range, and the corresponding values from a fit for even higher temperatures (550–750 K) are slightly higher, with $\lambda = 0.0025$ ($\lambda = 0.42$). The much reduced el-ph coupling of the upper VB branch is also reflected in a theoretically estimated large hole mobility of $988 \frac{\text{cm}^2}{\text{Vs}}$ at a hole carrier concentration of $1 \times 10^{13} \text{ cm}^{-2}$ and $T = 300$ K [13].

Figure 3(a) shows the experimentally determined band structure for high-quality SL WS_2 on Au(111) close to the K point, with the two well-separated spin-split branches of the VB. Since this part of the band structure is found in a projected bulk band gap of Au(111) [24], there is little direct hybridization between the SL WS_2 and substrate bands, and the states are very narrow. The high quality of the sample reveals some hitherto undetected details. In particular, a kinklike deviation from the nearly parabolic dispersion is visible at energies of 174 ± 14 and 124 ± 18 meV below the top of the upper and lower VB branches, respectively [for a magnification, see Fig. 3(b)]. Such kinks are often indicative of strong el-ph coupling, and while they normally occur close to the Fermi energy [25], they can also be found at higher binding energy such as near the top of the σ band of graphene [26,27]. Here, el-ph coupling can be ruled out as the cause of the kink, as its separation from the valence-band top by far exceeds the

highest phonon energy. Moreover, unlike in the situation of graphene, the calculated el-ph coupling is extremely small and one would not expect any observable kinks [13]. Instead, we assign the kink to a minigap opening at the new Brillouin zone boundary caused by the moiré superstructure formed between SL WS_2 and Au(111). Note that the minigaps do not affect the band structure exactly at K [13].

The effect of el-ph coupling on the two spin-split branches can be determined by analyzing energy distribution curves (EDCs) through the K point for data taken at different temperatures. Figure 3(c) shows a comparison of data taken at 30 and 550 K [13]. Even without any detailed analysis, it is clear that the temperature-induced broadening of the lower branch is substantially stronger than for the upper branch, in qualitative agreement with the theoretical results. For a more quantitative analysis, EDCs taken over a wide temperature range are fitted using a polynomial background and two Lorentzian peaks [13], and the resulting linewidth $\Gamma(T)$ is plotted in Fig. 3(d) together with the theoretical result for the freestanding layer [28]. The experimental linewidth is not expected to be identical to the theoretically calculated value of Eq. (1) because it contains contributions of electron-electron and electron-defect scattering. These can be significant but they are generally independent of the temperature. When comparing calculation and experiment, one should hence allow for a temperature-independent offset.

From the data in Fig. 3(d), the coupling constant λ can be estimated in the same way as previously used for the theoretical data: A linear fit of the data for high temperatures ($T > 300$ K, dashed lines in the figure) yields coupling constants of $\lambda_K \approx 0.52$ and 0.13 for the lower and upper VB, respectively. Note, however, the experimental linewidth is not reaching a truly linear regime and therefore the resulting λ depends on the temperature range chosen for the fit. Thus, rather than attempting an accurate determination of λ from the experimental data, we concentrate on a direct comparison of measured and calculated linewidths.

For the lower band, a good agreement between the experimental and calculated linewidths is found, especially when allowing for a temperature-independent offset between the curves. Indeed, the calculated slope at high temperature can be seen to be very similar to the experimental result. For the upper band, the agreement is less satisfying. Even when adding a constant offset to the calculated linewidth, the experimental data still shows a noticeable slope (reflected by $\lambda \approx 0.13$), in contrast to the nearly flat calculated curve.

An aspect that has so far not been considered is a possible involvement of the Au(111) substrate states. The presence of the substrate enables new decay channels via el-ph, electron-electron, and electron-defect scattering. Scattering into the substrate is known to be a significant process for the decay of excited carriers in the conduction band [30]. Including the substrate states in the calculation of Σ'' and λ is straightforward because it merely requires that the sums in Eqs. (1) and (2) be extended over the Au(111) electron and phonon states [13]. Note, however, that this approach neglects effects of band hybridization between SL WS_2 and the Au substrate, as well as the impact of the Au(111) surface state, at the expense of computational feasibility. None of the latter effects is expected to have a major impact on the final results at K , as band

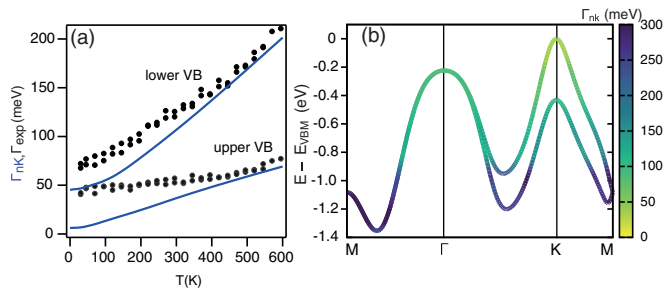


FIG. 4. (a) Temperature-dependent linewidth of the spin-split valence band branches at K , showing the experimental data together with a calculation including scattering contributions from the Au(111) substrate. (b) Band structure with encoded linewidths, as in Fig. 2(a), but including the effects of the Au(111) substrate.

hybridization effects were found to mainly occur in the vicinity of Γ at high binding energies. However, the hybridization in the possible final states for scattering processes might still affect the quantitative results. The Au(111) surface state is found to be energetically well above the VB maximum and should thus not play a role here [22].

When including the substrate's contribution to the el-ph coupling, a linear fit of the calculated linewidth between 300 and 600 K results in $\lambda_K = 0.20$ ($\lambda_K = 0.58$) for upper (lower) VB, respectively. Thus an improved agreement for temperature dependence of the upper band is found, but this happens at the expense of the agreement for the lower band, where the theoretical coupling strength now exceeds the experimental value [see Fig. 4(a)]. Figure 4(b) shows the VB band structure with a color coding of the linewidth, in the same way as in Fig. 2(a) but involving the Au substrate. Comparing Figs. 2(a) and 4(b) reveals that the Au substrate leads to an overall broadening of the states, especially at high binding energies. However, the energy-dependent changes of the two branches are still very similar, as seen in a detailed plot of their linewidth as a function of binding energy in Ref. [13].

While the strong branch dependence of the el-ph coupling is present in both calculations and in the experimental data, and while there is good agreement for the high-temperature slopes of the temperature-dependent linewidths, our model

does not provide an accurate quantitative description of the experimental data. This is evident in the entire temperature range shown in Fig. 4(a). Clearly, experimental results and calculations cannot be reconciled by a simple rigid shift to account for temperature-independent scattering mechanisms. The most likely explanation lies in the simplicity of the model, which requires a relatively small unit cell to be tractable and does not describe the hybridization of SL WS_2 and Au(111) adequately.

In summary, our results reveal drastically different el-ph coupling strengths in the spin-split VB states at K in SL WS_2 . Indeed, holes in the upper band can be expected to have a very long lifetime, in contrast to holes in the lower band that are fairly strongly affected by el-ph coupling. The strong spin-orbit interaction in WS_2 could easily permit inducing a hole population in the upper band at K without a significant number of carriers in the lower band or in the branch at Γ . Such a scenario should not only yield high hole mobilities and can help to explain the recently observed long lifetimes of a spin and valley-polarized hole population [8,9], it could also be a candidate for topological superconductivity [5]. Conventional el-ph mediated superconductivity, on the other hand, would be extremely unlikely in this situation. The effects reported here are not restricted to freestanding SL WS_2 but extend to a large group of equivalent two-dimensional semiconductors with a spin-orbit splitting that is larger than the phonon energy scale. Moreover, as we have demonstrated here, the strong difference of el-ph coupling in the two spin-split branches even survives in the presence of a strongly interacting substrate.

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