

Engineering the Spin-Orbit-Torque Efficiency and Magnetic Properties of Tb/Co Ferrimagnetic Multilayers by Stacking Order

Mickey Martini,^{1,2,*} Can Onur Avci¹, Silvia Tacchi¹,³ Charles-Henri Lambert,¹ and Pietro Gambardella¹

¹Department of Materials, ETH Zürich, Hönggerbergstrasse 64, CH-8093 Zürich, Switzerland

²Department of Physics, Politecnico di Milano, P.zza Leonardo da Vinci 32, I-20133 Milano, Italy

³Istituto Officina dei Materiali del CNR (CNR-IOM), Sede Secondaria di Perugia, c/o Dipartimento di Fisica e Geologia, Università di Perugia, I-06123 Perugia, Italy

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We measure the spin-orbit torques (SOTs), current-induced switching, and domain wall (DW) motion in synthetic ferrimagnets consisting of Co/Tb layers with differing stacking order grown on a Pt underlayer. We find that the SOTs, magnetic anisotropy, compensation temperature, and SOT-induced switching are highly sensitive to the stacking order of Co and Tb and to the element in contact with Pt. Our study further shows that Tb is an efficient SOT generator when in contact with Co, such that its position in the stack can be adjusted to generate torques additive to those generated by Pt. With optimal stacking and layer thickness, the dampinglike SOT efficiency reaches 0.3, which is more than twice that expected from the Pt/Co bilayer. Moreover, the magnetization can be easily switched by the injection of pulses with current density of about $(0.5\text{--}2) \times 10^7 \text{ A/cm}^2$ despite the extremely high perpendicular magnetic anisotropy barrier (up to 7.8 T). Efficient switching is due to a combination of large SOTs and low saturation magnetization owing to the ferrimagnetic character of the multilayers. We observe current-driven DW motion in the absence of any external field, which is indicative of homochiral Néel-type DWs stabilized by the interfacial Dzyaloshinskii-Moriya interaction. These results show that the stacking order in transition metal/rare-earth synthetic ferrimagnets plays a major role in determining the magnetotransport properties relevant for spintronic applications.

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I. INTRODUCTION

Magnetization switching and domain wall (DW) motion driven by spin-orbit torques (SOTs) have attracted extensive research interest due to their potential applications in nonvolatile memory and logic technologies [1–14]. To improve the scalability and thermal stability of devices in these applications, materials with perpendicular magnetic anisotropy (PMA) are often preferred. Ultrathin films of $3d$ transition metals and alloys (e.g., Co or CoFeB) have been widely investigated for such purposes, where the interfacial spin-orbit coupling gives rise to PMA [15–18]. Recently, however, increasing interest has been devoted to ferrimagnetic alloys of rare earth metals and transition metals possessing bulk PMA [19–37]. In these compounds, the rare-earth-metal and transition-metal magnetic sublattices are coupled antiparallel to each other, resulting in a reduced total magnetic moment relative to the individual sublattices [38,39]. The low magnetization allows for efficient SOT-induced switching, whereas the large PMA

increases the thermal stability of devices. Moreover, the possibility of obtaining angular momentum compensation allows for antiferromagnetlike magnetization dynamics that, e.g., leads to ultrafast switching and DW motion [31–33]. To date, studies of SOTs and related phenomena have mainly focused on the alloy form of rare-earth-metal-transition-metal systems [19–33], whereas multilayer structures have been less explored [34–37]. In such structures, the stacking order and the thickness of each layer offer additional degrees of freedom to tune the SOTs and understand the role of each element in interface-driven phenomena [13]. Theoretical [40] and experimental [34,37,41–44] studies suggest that the rare-earth elements with partially filled f orbitals are candidates for generating large spin Hall effect, and hence can be used as a source of SOTs. The strong spin-orbit interaction in the rare earth metals combined with the inversion symmetry breaking at their interfaces with transition metals can also produce a sizeable Rashba-Edelstein effect and Dzyaloshinskii-Moriya interaction (DMI). The latter stabilizes homochiral Néel-type domain walls with efficient and ultrafast current-induced dynamics [9–11,45–47].

*mickey.martini@icloud.com

Motivated by the above considerations, we investigate the influence of the stacking order and layer thickness on current-induced SOTs, switching, and DW motion in Pt/Co/Tb-based multilayers. Harmonic Hall and magneto-optic Kerr effect measurements reveal strong SOTs in the perpendicularly magnetized Tb/Co multilayers, which lead to efficient current-induced switching and DW motion, comparable to those of TbCo alloys in contact with Pt. Moreover, the SOTs and other magnetic properties, such as the saturation magnetization, magnetic anisotropy, compensation temperature, and the anomalous Hall effect (AHE), are highly sensitive to the stacking order as well as to the element in contact with the Pt underlayer. We find that Tb can be an effective source of SOTs with additive contributions to the ones due to Pt when placed on top of Pt/Co. These results show that the stacking order in rare-earth-metal/transition-metal multilayers offers an additional degree of freedom to tune the efficiency of SOT-controlled switching and DW motion.

II. SAMPLE PREPARATION AND CHARACTERIZATION

We grow Pt(4)/Tb(t_{Tb})/[Co(0.5)/Tb(0.65)/Co(0.5)] and Pt(4)/[Co(0.5)/Tb(0.65)/Co(0.5)]/Tb(t_{Tb}) multilayers with PMA as well as Pt(5)/Tb(t_{Tb})/Co(5) and Pt(5)/Co(5)/Tb(t_{Tb}) trilayers with in-plane anisotropy on thermally oxidized silicon substrates by dc magnetron sputtering (numbers indicate the thickness in nm). For all layers, a Ti capping of 5 nm and a Ta seed layer of 3 nm are used. The base pressure and Ar partial pressure of the deposition chamber are 6×10^{-8} and 4×10^{-3} mbar, respectively. The first two series, schematically illustrated in Fig. 1(a), are used for the SOTs, current-induced switching, and DW motion studies, whereas in the last two series only the SOTs are quantified. In the samples with PMA we fix the layers between square brackets and change the Tb thickness (t_{Tb}) and position relative to them; similarly, in the trilayers with in-plane anisotropy we change the Tb thickness and position relative to Co. Hall bar devices are fabricated by patterning the substrates using optical lithography before deposition and subsequent lift-off.

In Fig. 1(b) we show representative magnetization curves measured by a superconducting quantum interference device at room temperature with an out-of-plane field sweep for the two different positions of the Tb(1) layer with respect to the fixed [Co/Tb/Co] trilayer. Both sets of data show clear hysteresis and nearly 100% remanence at zero field, indicative of strong PMA. However, their saturation magnetization (M_s) differs significantly even though the amount of Tb and Co is the same in both multilayers. Measurements of all the six samples with PMA [Fig. 1(c)] show that M_s is larger when Co is in direct contact with Pt except for the thickest Tb samples. In both multilayer systems, M_s is significantly smaller relative to that expected

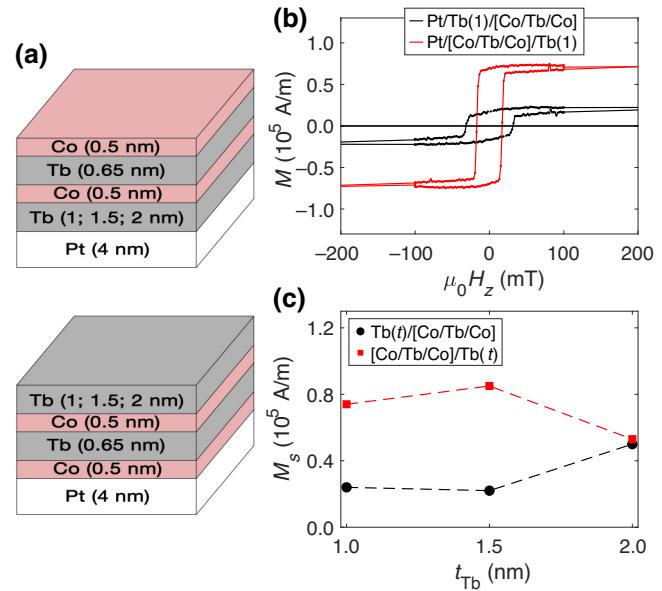


FIG. 1. (a) Schematic illustration of the Co/Tb/Co multilayers with different stacking order. (b) Magnetization curves of Pt/Tb(1)/[Co/Tb/Co] and Pt/[Co/Tb/Co]/Tb(1). (c) Saturation magnetization versus Tb thickness.

for Co ($> 10^6$ A/m), as expected due to the antiferromagnetic coupling of Co and Tb. The large difference in M_s and its dependence on Tb thickness indicate that the net magnetization is highly sensitive to the stacking order.

Figure 2(a) shows the device layout with the electrical connections and the coordinate system. Figure 2(b) reports the sheet resistance R_s measured using a four-point geometry in the structures with PMA. R_s is about 20% larger in samples with Pt/Tb interface compared with those with Pt/Co interface. The larger R_s and its increase with t_{Tb} in Pt/Tb(t_{Tb})/[Co/Tb/Co] might be due to increased interfacial electron scattering and/or intermixing between Tb and Pt in this system. In contrast, in Pt/[Co/Tb/Co]/Tb(t_{Tb}), R_s does not significantly change with the Tb thickness, suggesting that the electric conductivity is predominantly dictated by the Pt and Co layers. The resistivity ρ of all six multilayers with PMA, estimated by considering only the conduction through Pt, Co, and Tb and neglecting the contribution from the buffer and capping layers, is reported in Table II along with the other properties measured in this study.

In alloys of rare earth metals and transition metals and in multilayers, the magnetotransport properties are dominated by the $3d4s$ orbitals of the transition-metal elements near the Fermi level; thus the AHE is mainly driven by the transition-metal sublattice [20,34,48]. In Fig. 2(c) we report the Hall resistance R_H as a function of out-of-plane magnetic field. As evident from the data, the AHE is positive and large in the Pt/[Co/Tb/Co]/Tb series as opposed

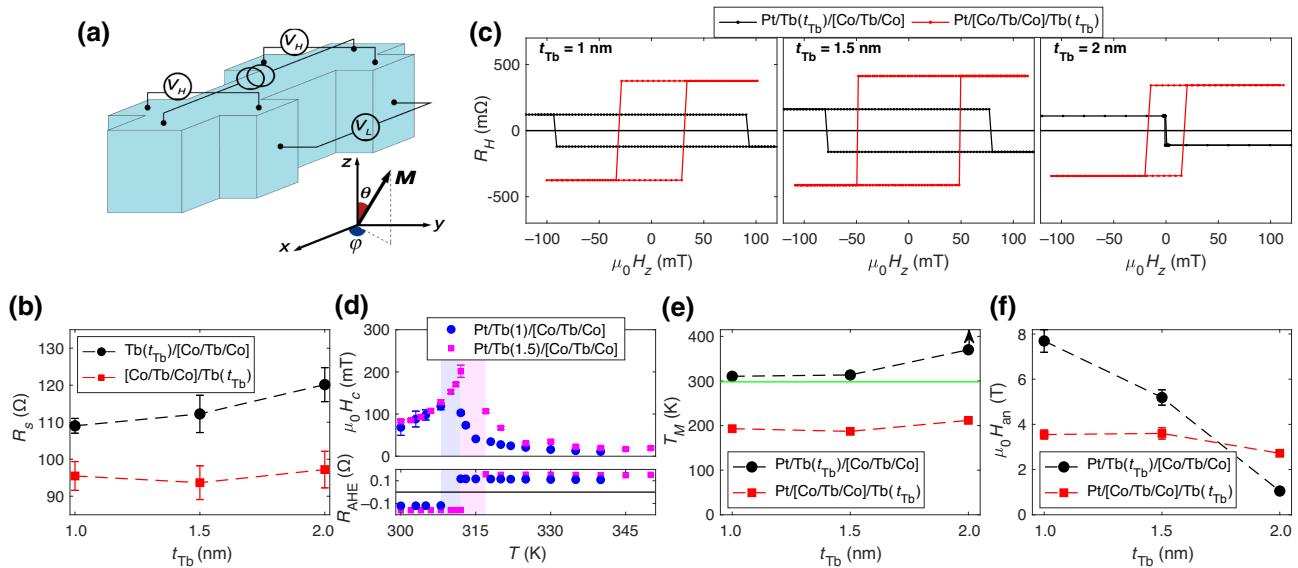


FIG. 2. (a) Schematics of a Hall bar device and coordinate system. The Hall bar channel is $100 \mu\text{m}$ long and $5 \mu\text{m}$ wide. (b) Sheet resistance versus thickness of Tb layer in $Pt/Tb(t_{Tb})/[Co/Tb/Co]$ and $Pt/[Co/Tb/Co]/Tb(t_{Tb})$. (c) Hall resistance as a function of out-of-plane magnetic field in samples with different Tb thickness. (d) Coercive field versus temperature in $Pt/Tb(1,1.5)/[Co/Tb/Co]$. The regions shaded in blue and magenta represent temperature ranges in which the magnetization is strongly compensated. (e) Magnetization compensation temperature as a function of Tb thickness. The black arrow indicates that $T_M > 370 \text{ K}$, which is the largest temperature reached in our setup; the green solid line indicates room temperature. (f) Anisotropy field at room temperature versus Tb thickness.

to the $Pt/Tb/[Co/Tb/Co]$ series, where the AHE is negative and relatively small. This means that (i) at room temperature the total magnetization is dominated by the Co (Tb) sublattice for the layers with Pt/Co (Pt/Tb) interface and that the magnetic compensation temperature T_M is below (above) room temperature; (ii) the Pt/Co interface has a significant contribution to the AHE, in agreement with literature data [49]. Our data clearly show that the stacking order plays a crucial role in determining the magnetic compensation point as well as the AHE, in addition to M_s and R_s discussed earlier. We further study the coercive field (H_c) as a function of temperature to characterize T_M of all six samples. As the temperature crosses T_M , the anomalous Hall resistance R_H changes sign; further, H_c diverges because a stronger external field is required to reverse the vanishing net magnetization [50], as shown for $Pt/Tb(1; 1.5 \text{ nm})/[Co/Tb/Co]$ in Fig. 2(d). T_M determined from the change of sign of R_H is shown in Fig. 2(e) for all the six samples. The stacking order gives rise to a substantial difference of more than 100 K in T_M between $Pt/Tb(t_{Tb})/[Co/Tb/Co]$ and $Pt/[Co/Tb/Co]/Tb(t_{Tb})$, which is likely related to the larger M_s of $Pt/[Co/Tb/Co]/Tb(t_{Tb})$.

Finally, we characterize the effective magnetic anisotropy field H_{an} by measuring R_H in the samples with PMA as a function of an external magnetic field applied nearly in plane at polar and azimuthal angles $\theta_H = 88^\circ$ and $\varphi_H = 90^\circ$ [see Fig. 2(a) for the definition of the angular coordinates]. We use a macrospin approximation to

calculate $H_{an} = H ((\sin \theta_H / \sin \theta) - (\cos \theta_H / \cos \theta))$, where $\theta = \arccos |R_H / R_{AHE}|$ [51], as reported in Fig. 2. We find $\mu_0 H_{an} = 7.8 \pm 0.5 \text{ T}$ in $Pt/Tb(1)/[Co/Tb/Co]$, which rapidly decreases with increasing Tb thickness due to the shift of T_M to higher temperatures. In the $Pt/[Co/Tb/Co]/Tb(1)$ series, on the other hand, H_{an} is relatively constant, which is consistent with the behavior of T_M in these samples. We note that extremely large anisotropy fields in excess of 3 T are measured in all of our samples, with the exception of $Pt/Tb(2)/[Co/Tb/Co]$.

III. RESULTS AND DISCUSSION

A. SOTs in multilayers with PMA

The SOT-induced effective fields are quantified by performing harmonic Hall effect measurements in the PMA samples [52,53]. An alternating current with frequency $\omega/2\pi = 10 \text{ Hz}$ and amplitude $j = 0.3 - 1 \times 10^7 \text{ A/cm}^2$ is applied along the x axis, and the first- and second-harmonic Hall resistances ($R_H^{1\omega}$ and $R_H^{2\omega}$) are measured during an in-plane field sweep along the x and y axes (H_x, H_y). The current density is estimated by dividing the current by the total cross section of the Pt, Co, and Tb layers. We neglect the conductivity of the highly resistive Ta buffer and Ti capping layers. In multilayers with inversion symmetry along the z axis and current injection along x , the dampinglike and fieldlike SOT effective fields are

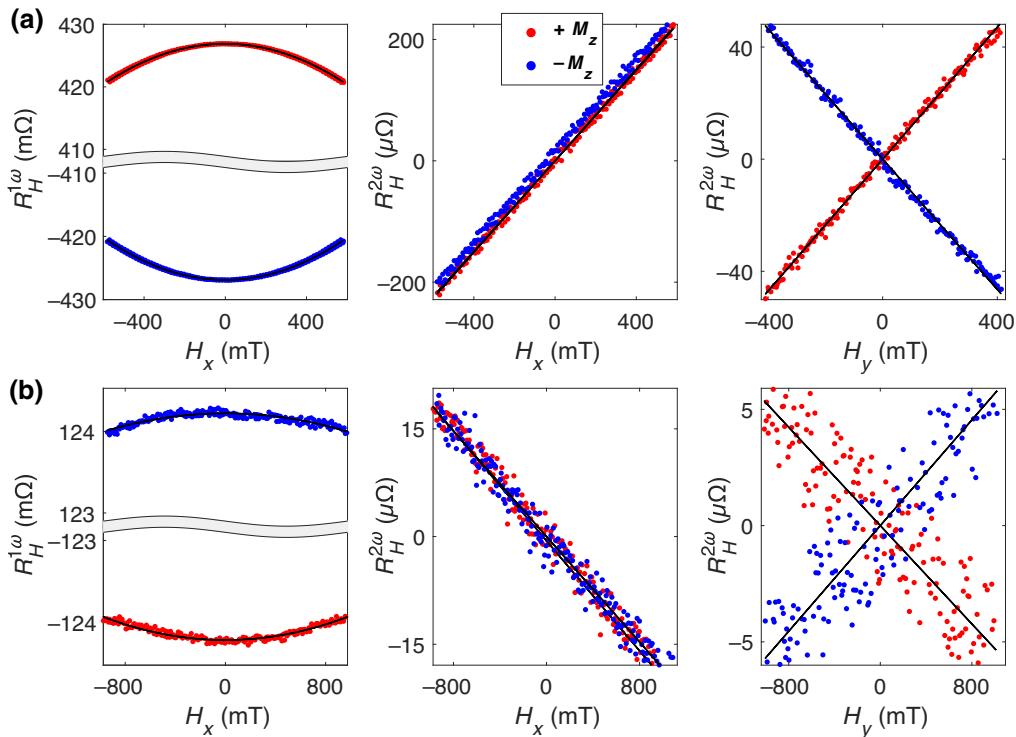


FIG. 3. First and second harmonic of the Hall resistance ($R_H^{1\omega}$ and $R_H^{2\omega}$, respectively) versus in-plane longitudinal and transverse magnetic fields (H_x and H_y) measured using $j = 0.8 \times 10^7$ A/m² in (a) Pt/[Co/Tb/Co]/Tb(1.5) and (b) Pt/Tb(1)/[Co/Tb/Co].

given by $\mathbf{H}_{\text{DL}} = H_{\text{DL}}(\mathbf{y} \times \hat{\mathbf{M}})$ and $\mathbf{H}_{\text{FL}} = H_{\text{FL}}\mathbf{y}$, respectively, where \mathbf{M} is the unit vector of the magnetization and the current-induced spin accumulation is polarized along \mathbf{y} [13]. In order to define the sign of the field amplitudes $H_{\text{DL,FL}}$, we adopt the convention that H_{DL} (H_{FL}) is positive (negative) when the field points in the same direction as in Pt/Co (opposite direction to the Oersted field), where Pt is deposited before Co [52]. Due to the large PMA in our samples, we opt for the small-angle approximation method where the magnetization is slightly tilted away from equilibrium by the applied field. In this regime, the effective fields can be estimated using the following relations [54,55]:

$$\Delta H_{x(y)} = \left(\frac{\partial R_H^{2\omega}}{\partial H_{x(y)}} \right) \left/ \left(\frac{\partial^2 R_H^{1\omega}}{\partial H_{x(y)}^2} \right) \right., \quad (1)$$

$$H_{\text{DL(FL)}} = -2 \frac{\Delta H_{x(y)} \pm v \Delta H_{y(x)}}{1 - 4v^2}, \quad (2)$$

where v is the ratio of the planar Hall resistance R_{PHE} to the anomalous Hall resistance R_{AHE} and \pm corresponds to the measurements taken when the magnetization is pointing along the $\pm z$ direction. To characterize R_{AHE} and R_{PHE} , we use the first-harmonic signal given by $R_H^\omega = R_{\text{AHE}} \cos \theta + R_{\text{PHE}} \sin^2 \theta \sin 2\varphi$. Since the magnetization cannot be fully saturated in plane by the available field,

we quantify R_{PHE} by measuring R_H^ω with an external field applied at $(\theta_H, \varphi_H) \equiv (88^\circ, 45^\circ)$. We then separate the antisymmetric and symmetric signal contributions (with respect to the field reversal), which originate from the first and second terms in the above equation, respectively. The antisymmetric signal is then plotted as a function of $\sin^2 \theta$, where θ is estimated using the macrospin approximation as $\theta = \arccos |R_H^{1\omega}/R_{\text{AHE}}|$. Finally the slope of the linear fit represents R_{PHE} . The details of this approach can be found in Ref. [52].

Figure 3 shows representative $R_H^{1\omega}$ and $R_H^{2\omega}$ measurements taken from the Pt/[Co/Tb/Co]/Tb(1.5) and Pt/Tb(1)/[Co/Tb/Co] samples. $R_H^{1\omega}$ has a parabolic field dependence due to the coherent rotation of the magnetization. Note that we only plot the data corresponding to the H_x sweep since the H_y sweep shows an identical behavior. The sign of $R_H^{2\omega}$ is opposite in these two samples for a given magnetization orientation due to the opposite AHE [see Fig. 2(c)]. $R_H^{2\omega}$ varies linearly with both H_x and H_y as expected from the action of SOTs. We note that the slopes of $R_H^{2\omega}$ are opposite in Co-like and Tb-like samples. Considering also the opposite sign of $R_H^{1\omega}$ in these two samples, we conclude that the SOT effective fields have the same sign in both systems. Thus, the SOTs act on the net magnetization, in agreement with previous works [21,23]. The SOT effective fields normalized by the current density, $\chi_{\text{DL(FL)}} = \mu_0 H_{\text{DL(FL)}}/j$,

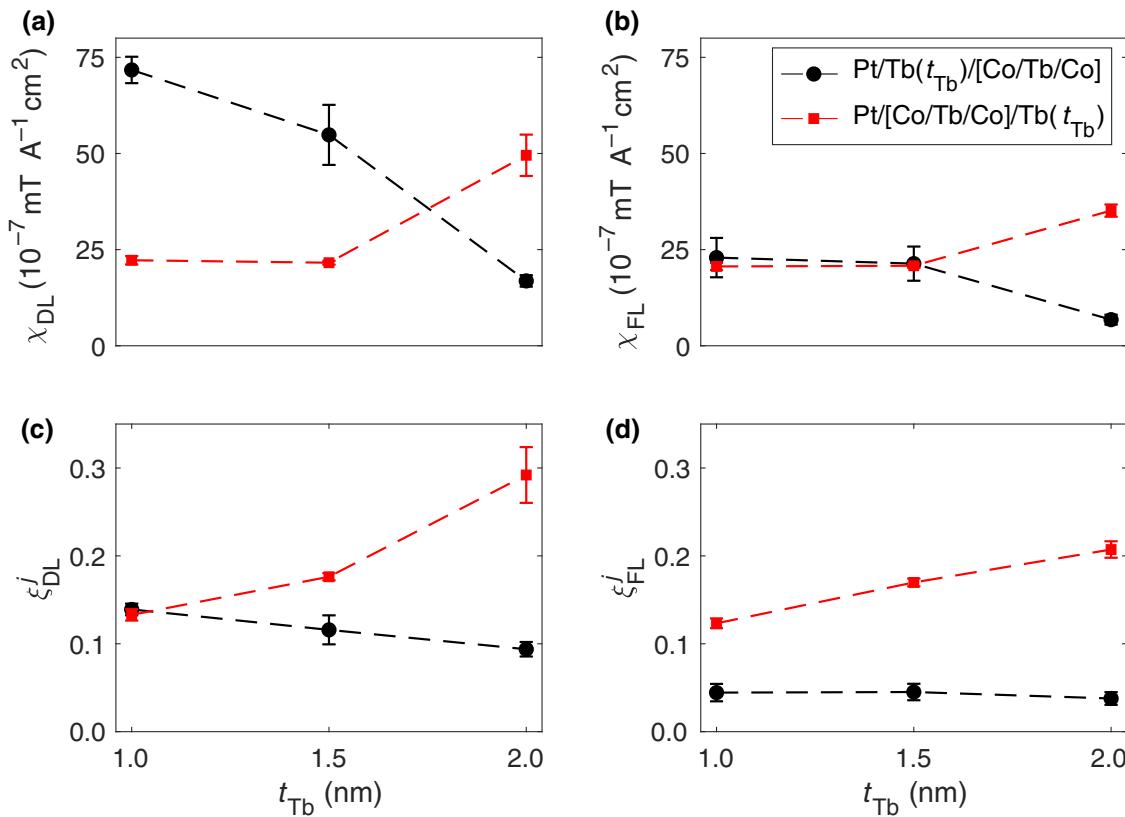


FIG. 4. (a) Dampinglike and (b) fieldlike SOT effective field per unit current density $\chi_{\text{DL},\text{FL}}$ versus Tb thickness in $\text{Pt}/[\text{Co/Tb/Co}]/\text{Tb}(t_{\text{Tb}})$ and $\text{Pt/Tb}(t_{\text{Tb}})/[\text{Co/Tb/Co}]$. (c) Dampinglike and (d) fieldlike SOT efficiency $\xi_{\text{DL},\text{FL}}^j$ versus Tb thickness. The error bars take into account the errors of the linear and parabolic fits of $R_H^{1\omega}$ and $R_H^{2\omega}$, respectively, averaged according to Eq. (2) for each current density, propagated in the linear fits of $H_{\text{DL},\text{FL}}(j)$ for the $+\mathbf{M}_z$ and $-\mathbf{M}_z$ configurations.

are summarized in Figs. 4(a) and 4(b) as a function of Tb thickness. The values of $\chi_{\text{DL},\text{FL}}$ are obtained by performing a linear fit of $H_{\text{DL},\text{FL}}$ versus j for both magnetization orientations (not shown). The fieldlike component includes also the Oersted field contribution due to the current flowing through Pt, which we estimate as $\mu_0 H_{\text{Oe}}/j = 0.3 \text{ mT } 10^{-7} \text{ A}^{-1} \text{ cm}^2$ by Ampere's law [51]. The Oersted field points in the opposite direction to the fieldlike component of the SOT field, and can be neglected due to its small amplitude compared with H_{FL} . We observe that χ_{DL} is very strong in $\text{Pt/Tb}(1)/[\text{Co/Tb/Co}]$, reaching $+72 \text{ mT } 10^{-7} \text{ A}^{-1} \text{ cm}^2$ but rapidly decreasing as the Tb thickness is increased. Also χ_{FL} reaches remarkable values, about $+25 \text{ mT } 10^{-7} \text{ A}^{-1} \text{ cm}^2$ in both $\text{Pt/Tb}(1)/[\text{Co/Tb/Co}]$ and $\text{Pt}/[\text{Co/Tb/Co}]/\text{Tb}(1)$. To compare the SOTs in different layers on an equal footing we calculate the SOT efficiencies $\xi_{\text{DL},\text{FL}}^j = (2e/\hbar) M_s t_M \chi_{\text{DL},\text{FL}}^j$ [56], where e is the electron charge, \hbar is the reduced Planck's constant, and t_M is the magnetic layer thickness. The SOT efficiencies are plotted in Figs. 4(c) and 4(d) as a function of Tb thickness. We observe that ξ_{DL}^j and ξ_{FL}^j vary between $+0.1$ and $+0.1$ and between $+0.03$ and $+0.2$, respectively.

Whereas ξ_{DL}^j and ξ_{FL}^j in $\text{Pt}/[\text{Co/Tb/Co}]/\text{Tb}(1)$ and $\text{Pt/Tb}(1)/[\text{Co/Tb/Co}]$ are comparable to those measured in Pt/Co bilayers [13,52], we observe that both efficiencies increase strongly as a function of Tb thickness in $\text{Pt}/[\text{Co/Tb/Co}]/\text{Tb}(t)$, reaching values that are about two times larger compared with Pt/Co . Moreover, ξ_{FL}^j is significantly larger in $\text{Pt}/[\text{Co/Tb/Co}]/\text{Tb}(t_{\text{Tb}})$ compared with that in $\text{Pt/Tb}(t_{\text{Tb}})/[\text{Co/Tb/Co}]$, and has a different thickness dependence in the two series. Similar trends are also observed if we consider the SOT efficiency per unit electric field $\xi_{\text{DL},\text{FL}}^E = \xi_{\text{DL},\text{FL}}^j / \rho$ (see Table II).

We note that ξ_{DL}^j and ξ_{FL}^j are obtained by normalization to the average current density j flowing in the multilayers, such that even larger efficiencies would be obtained by normalization to the current density flowing in Pt, as often done in the literature. The dependence of $\xi_{\text{DL},\text{FL}}^j$ on the stacking order and Tb thickness can have several origins. First, the structural details of the multilayers and of the interface with Pt generally change with the stacking order, which may ultimately lead to changes of the SOTs. This point is supported by the resistivity measurements, which suggest that Tb deposited on Pt induces intermixing between the two species rather than favoring sharp

interfaces. Second, the Tb layer can be a source of dampinglike and fieldlike SOTs in itself, with a contribution opposite to that of Pt. Such a scenario, which agrees with a previous study of Pt/[Co/Ni]/Co/Tb multilayers [37], is consistent with the enhancement of $\xi_{\text{DL(FL)}}^j$ when Pt and Tb are placed on opposite sides of the [Co/Tb/Co] trilayer. Third, placing the Tb layer on top of the stack might provide an efficient sink for the spin current generated by Pt and the Pt/Co interface [57]. The monotonic increase of the dampinglike and fieldlike SOTs in this series is consistent with both the second and third explanation taking into account the finite spin diffusion length of Tb. Overall, even if the exact mechanism giving rise to the enhancement of ξ_{DL}^j and ξ_{FL}^j cannot be singled out with certainty, our data indicate that Tb and the stacking order of Co/Tb multilayers play a crucial role in determining the strength of the SOTs.

B. SOTs in Pt/Tb/Co and Pt/Co/Tb trilayers with in-plane magnetic anisotropy

We quantify the dampinglike SOT efficiency in samples with in-plane anisotropy following the method outlined in Ref. [58]. Injection of a relatively small alternating current [$\omega/2\pi = 10$ Hz, $j = (0.3\text{--}1) \times 10^7$ A/cm²] gives rise to periodic oscillations of the magnetization about its equilibrium position. The second-harmonic Hall resistance related to the current-induced fields and the thermoelectric signal due to Joule heating can be written as

$$R_H^{2\omega} = \left(R_{\text{AHE}} \frac{H_{\text{DL}}}{H_{\text{ext}}} + I_0 \alpha \nabla T \right) \cos \varphi + 2R_{\text{PHE}} (2 \cos^3 \varphi - \cos \varphi) \frac{H_{\text{FL}} + H_{\text{Oe}}}{H_{\text{ext}} + H_{\text{dem}}}, \quad (3)$$

where I_0 is the amplitude of the injected current, α the anomalous Nernst coefficient, ∇T the perpendicular thermal gradient, and H_{dem} the demagnetizing field. Figure 5(a) shows a representative angle scan measurement of $R_H^{2\omega}$ in Pt/Co/Tb(3) for different external in-plane fields along with the fitting curves (dashed lines) given by Eq. (3). In Fig. 5(b) we plot the $\cos \varphi$ component of $R_H^{2\omega}$, which includes the combined contributions of dampinglike torque and the Nernst (and/or Seebeck) effect. The amplitude of the $\cos \varphi$ component of $R_H^{2\omega}$ decreases on increasing the external field. The latter tends to rigidly align the magnetization along its direction, suppressing the periodic oscillations. This results in a reduction of the SOT and therefore of $R_H^{2\omega}$ and its $\cos \varphi$ component. This field dependence can be exploited to further separate the dampinglike torque and the thermoelectric effects in the $\cos \varphi$ component of $R_H^{2\omega}$. The anomalous Nernst effect depends only on the magnetization direction and not on the external field amplitude (provided that the magnetization is saturated), whereas the SOT decreases at higher field, as already discussed. Thus, the dampinglike effective field H_{DL} can be quantified by performing a linear fit of the $\cos \varphi$ component of $R_H^{2\omega}$ versus the inverse of the external field plus the demagnetizing field H_{dem} [58], as shown in the inset of Fig. 5(b). This experiment is repeated for all the samples for several current densities to estimate χ_{DL} as the slope of H_{DL} versus j , as done for the multilayers with PMA in Sec. III A. The values of χ_{DL} are reported in Table I. Compared with the multilayers with PMA, the dampinglike effective field in the samples with in-plane anisotropy is 2 orders of magnitude lower. This is due to the large magnetization on which the SOT acts, n is dominated by the bulk magnetic moments of the Co layer (the ferromagnetic layer is now thick). The dampinglike SOT

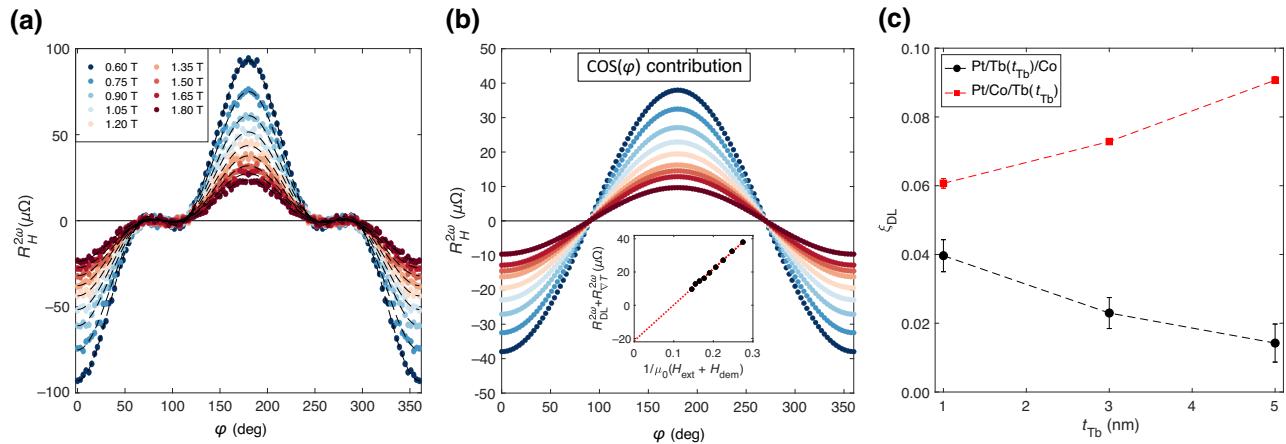


FIG. 5. (a) In-plane angular dependence of the second-harmonic Hall resistance of Pt/Co/Tb(3) for $j = 0.8 \times 10^7$ A/cm². (b) Dampinglike and thermal contribution to the second-harmonic Hall resistance. Inset: linear fit of the cosine component of the second-harmonic Hall resistance versus the inverse of the external field and the demagnetizing field acting against the current-induced field. (c) Dampinglike SOT efficiency versus Tb thickness. The error bars take into account the uncertainty of the linear fit of H_{DL} versus j .

TABLE I. Saturation magnetization, demagnetizing field, dampinglike effective field per unit current density, and SOT efficiency in trilayers with in-plane anisotropy. Errors are a fraction of the least significant digit.

	M_s (10^6 A m^{-1})	$\mu_0 H_{\text{dem}}$ (T)	χ_{DL} (mT $10^{-7} \text{ A}^{-1} \text{ cm}^2$)	ξ_{DL}^j
Pt/Tb(1)/Co	1.13	1.80	0.19	0.040
Pt/Tb(3)/Co	0.81	1.59	0.12	0.023
Pt/Tb(5)/Co	0.48	1.48	0.10	0.014
Pt/Co/Tb(1)	1.22	0.75	0.27	0.061
Pt/Co/Tb(3)	0.81	0.72	0.37	0.073
Pt/Co/Tb(5)	0.68	0.56	0.44	0.091

efficiency, calculated also here as $\xi_{\text{DL}}^j = (2e/\hbar)M_s t_M \chi_{\text{DL}}$, is plotted in Fig. 5(c) as a function of t_{Tb} . Although ξ_{DL}^j is significantly lower in these samples compared with the samples with PMA, it scales in the same way with t_{Tb} , increasing (decreasing) in the trilayer with Pt/Co (Pt/Tb) interface. The comparison between Pt/Tb/Co and Pt/Co/Tb structures provides further evidence that the SOTs are very sensitive to t_{Tb} and the stacking order of Co/Tb.

C. Current-induced magnetization switching

The large SOTs evidenced by the harmonic Hall effect measurements in Sec. III A can be exploited to realize current-induced magnetization switching with enhanced efficiency relative, e.g., to Pt/Co bilayers. In order to study SOT-induced switching in our multilayers with PMA, we inject 10-ms-long current pulses of variable amplitude through the Hall bar devices in the presence of an in-plane bias field H_x applied parallel to the current line. This field is required to break the SOT symmetry and uniquely define the switching polarity [1,13]. Figure 6(a) shows representative AHE hysteresis loops as a function of current measured for Pt/Tb(2)/[Co/Tb/Co] and Pt/[Co/Tb/Co]/Tb(2). In both samples, the net magnetization switches from $+M_z$ to $-M_z$ when the current is parallel to the in-plane field and from $-M_z$ to $+M_z$ when it is antiparallel to it. The loops of Fig. 6(a) have opposite polarity because the AHE has opposite sign in these two samples at room temperature [see Fig. 2(c)].

We repeat the measurements summarized in Fig. 6(a) for all of the multilayers with PMA and several in-plane magnetic fields to characterize the threshold current density j_{th} required to switch the magnetization. The data are shown in Fig. 6(b) as a function of $\mu_0 H_x$. In the macrospin approximation, the threshold switching current is given by [29,59]

$$j_{\text{th}} = \frac{2e}{\hbar} \frac{\mu_0 M_s t_M}{\xi_{\text{DL}}^j} \left(\frac{H_k}{2} - \frac{H_x}{\sqrt{2}} \right), \quad (4)$$

where t_M is the thickness of the magnetic layer. Although Eq. (4) does not apply to switching by domain nucleation and propagation, which is the preferred mode of magnetization reversal in mesoscopic samples [47], one still

expects j_{th} to scale with H_k and H_x given that these two fields determine the domain nucleation barrier. Figure 6(b) shows that, despite the very large H_k of our multilayers (see Sec. II), we are able to switch all of the samples with current densities below $2.5 \times 10^7 \text{ A/cm}^2$ and in-plane field $H_x \ll H_k$. This is due to the combined effect of strong dampinglike SOTs and low M_s owing to the ferrimagnetic character of our multilayers. The strongest dependence of

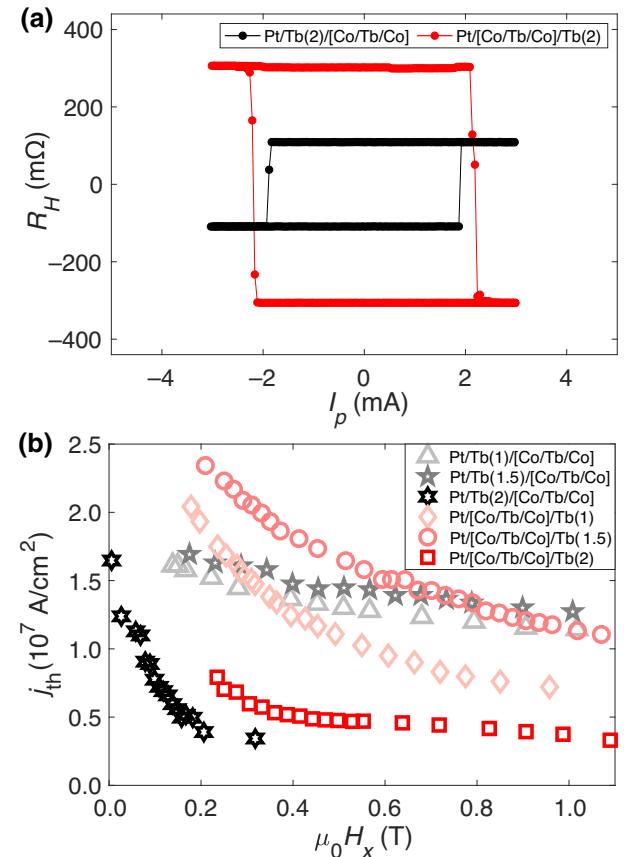


FIG. 6. (a) Change of the anomalous Hall resistance due to SOT-induced switching in Pt/Tb(2)/[Co/Tb/Co] with constant in-plane field $\mu_0 H_x = 182$ mT and in Pt/[Co/Tb/Co]/Tb(2) with $\mu_0 H_x = 333$ mT. The Hall resistance is plotted versus the amplitude I_p of 10-ms-long current pulses. (b) Threshold current density for switching as a function of the in-plane field $\mu_0 H_x$.

j_{th} on H_x is found in the sample with weakest magnetic anisotropy, namely Pt/Tb(2)/[Co/Tb/Co], as expected. The samples with strongest anisotropy, where $\mu_0 H_k \geq 6$ T, present a much weaker dependence of j_{th} on H_x , suggesting that the in-plane field is not the main cause of reduction of the domain nucleation barrier in such a case. On the other hand, j_{th} scales with ξ_{DL} and M_s in samples with comparable anisotropy, such as in the Pt/[Co/Tb/Co]/Tb(t_{Tb}) series.

To investigate the role of Joule heating in the switching experiments, we measure the Hall effect by injecting different current densities up to $j \simeq 2 \times 10^7$ A/cm². We find that the coercivity decreases by about 30% upon increasing j from 0.5 to 2×10^7 A/cm² (not shown). Likewise, we also estimate the anisotropy field $\mu_0 H_k$ in all the multilayers and record a drop smaller than 25% from the case of $j < 1 \times 10^7$ A/cm² to the case of $j = 2 \times 10^7$ A/cm². Therefore we conclude that Joule heating does not play a major role in determining j_{th} for $j < 1 \times 10^7$ A/cm², whereas it partially assists the switching at higher current by decreasing the magnetic anisotropy energy barrier and favoring DW depinning. Indeed, j_{th} is determined by the interplay of several factors beyond H_k , H_x , ξ_{DL} , and M_s , which include Joule heating as well as ξ_{FL} , the DMI and DW pinning properties of the multilayers. Overall, these data show that SOTs can switch ferrimagnetic multilayers with very strong PMA at a current density of the order of 10⁷ A/cm², similarly to what is observed in CoTb alloys [28].

D. Current-induced DW motion

SOTs can efficiently move DWs in suitable devices and heterostructures [13]. Compensated ferrimagnets are particularly interesting for the SOT-induced DW motion because the DWs can be propelled at very high speeds with moderate currents owing to their particular dynamical properties near the magnetic and angular momentum compensation [11,27,31,32,60–62]. We investigate the current-induced DW motion in the Pt/[Co/Tb/Co]/Tb(t_{Tb}) samples. We use a wide-field Kerr microscope configured in polar geometry to detect the out-of-plane magnetization component in Pt/[Co/Tb/Co]/Tb(t_{Tb}) racetracks and study the DW response to external fields and currents. The experimental procedure can be briefly described as follows. First, the magnetization is saturated along +z or -z by applying an out-of-plane magnetic field larger than the coercivity. Next, a domain with the opposite magnetization is nucleated by the Oersted field produced by a short current pulse I_{nuc} injected into an electrically insulated wire crossing the racetrack [Fig. 7(a)]. Finally, the DW is displaced by injecting current pulses along the DW track. We perform two types of experiments: (i) determination of the critical current for depinning a single DW in the presence or absence of an out-of-plane field (H_z); (ii) determination of the DW velocity in the absence of any applied field.s

TABLE II. Summary of the magnetic properties and SOT efficiency of Pt/Tb(t_{Tb})/[Co/Tb/Co] and Pt/[Co/Tb/Co]/Tb(t_{Tb}) multilayers with PMA. All values are measured in ambient conditions. Errors are a fraction of the least significant digit, except for T_M , whose error is of the order of 1 K.

	ρ ($\mu\Omega$ cm)	M_s (10 ⁵ A m ⁻¹)	T_M (K)	R_{AHE} (mΩ)	R_{PHE} (mΩ)	$\mu_0 H_k$ (T)	χ_{DL} (mT 10 ⁻⁷ A ⁻¹ cm ²)	χ_{FL} (mT 10 ⁻⁷ A ⁻¹ cm ²)	ξ_{DL}^j $\Omega^{-1} \text{ m}^{-1}$	ξ_{FL}^E $\Omega^{-1} \text{ m}^{-1}$	ξ_{FL}^E (10 ⁵ $\Omega^{-1} \text{ m}^{-1}$)
Pt/Tb(1)/[Co/Tb/Co]	72.5	0.24	310	129	18	7.8	+72	+23	+0.14	+0.04	+1.92
Pt/Tb(1.5)/[Co/Tb/Co]	80.3	0.22	313	154	22	5.2	+55	+21	+0.12	+0.04	+1.44
Pt/Tb(2)/[Co/Tb/Co]	91.9	0.50	> 370	120	16	1.1	+17	+7	+0.10	+0.04	+1.02
Pt/[Co/Tb/Co]/Tb(1)	63.5	0.74	193	375	89	3.2	+22	+20	+0.13	+0.12	+2.09
Pt/[Co/Tb/Co]/Tb(1.5)	67.0	0.85	187	425	101	3.5	+22	+20	+0.18	+0.17	+2.63
Pt/[Co/Tb/Co]/Tb(2)	74.4	0.53	212	341	62	2.7	+50	+35	+0.29	+0.21	+3.93
											+2.79

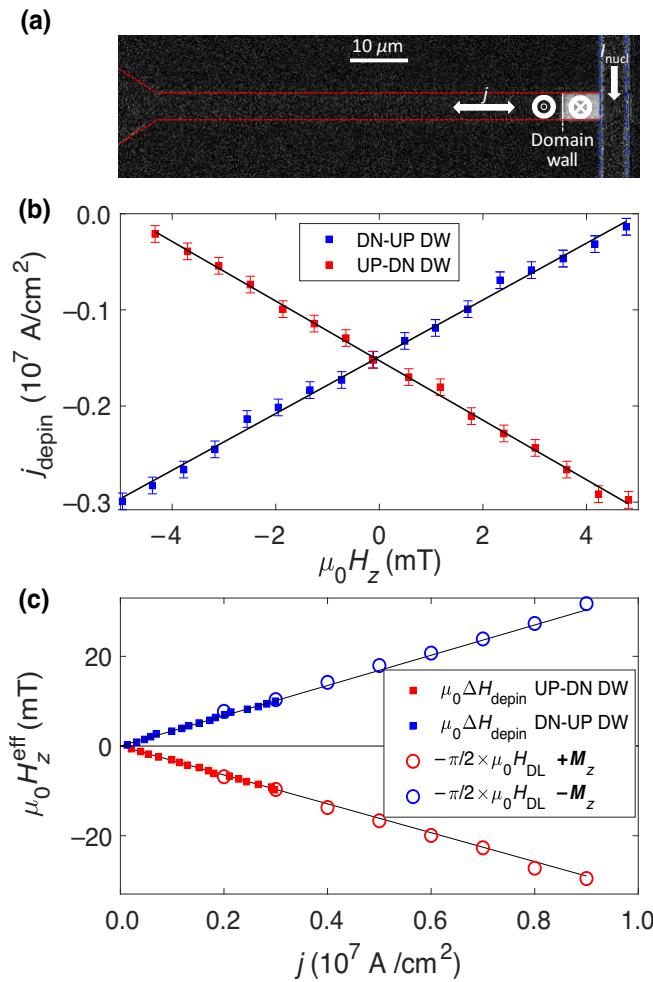


FIG. 7. (a) Differential Kerr microscopy image showing the nucleation of a magnetic domain (white region) in a Pt/[Co/Tb/Co]/Tb(1) racetrack delimited by the red dotted line. (b) Critical current density required to depin up-down and down-up DWs as a function of applied out-of-plane magnetic field in Pt/[Co/Tb/Co]/Tb(1). (c) Effective out-of-plane magnetic field corresponding to the depinning field ΔH_{depin} (squares) and dampinglike SOT effective field $-\pi/2 \times H_{\text{DL}}$ (circles) versus current density for both DWs and magnetic states in Pt/[Co/Tb/Co]/Tb(1).

Figure 7(b) shows the critical current density j_{depin} required to depin a DW as a function of H_z for both the up-down and down-up DWs in Pt/[Co/Tb/Co]/Tb(1). The linear variation of $j_{\text{depin}}(H_z)$ shows that the current induces a dampinglike SOT that acts as an effective magnetic field along $\pm z$, assisting or hindering H_z to depin the DWs [9,11,63,64]. In the one-dimensional DW model, neglecting the spin-transfer and fieldlike torques, the effective field induced by the current is given by $H_z^{\text{eff}} = \Delta H_{\text{depin}}$, where ΔH_{depin} is the change in the DW depinning field under dc current injection. Alternatively, we estimate $H_z^{\text{eff}} = -(\pi/2)H_{\text{DL}} \cos \Psi$, where H_{DL} is the dampinglike SOT effective field obtained by the harmonic Hall effect

measurements in Sec. III A and Ψ is the angle between the DW magnetization and the x axis [65]. Figure 7(c) compares H_z^{eff} obtained using ΔH_{depin} and $- (\pi/2)H_{\text{DL}}$ for different current densities. The two measurements are in excellent agreement, which implies that the DWs are of purely homochiral Néel type (i.e., $\Psi = 0^\circ$). Moreover, the DW motion along the current flow indicates that they have left-handed chirality. This is consistent with the interfacial DMI occurring at the Pt/Co interface with possible additional contributions from the inner interfaces between Co and Tb and the top Tb/Ti interface [66]. Qualitatively the same results are obtained for Pt/[Co/Tb/Co]/Tb(1.5) and Pt/[Co/Tb/Co]/Tb(2), showing that the current-induced DW depinning measurements can be effectively used to identify the DW type and estimate the DL-SOT effective field in this system. Next, we characterize the current-induced DW velocities in Pt/[Co/Tb/Co]/Tb(1, 1.5, 2). To do so, we capture a sequence of Kerr images while injecting a train of current pulses through the track to move a pre-nucleated DW, as shown in Fig. 8(a). To estimate the DW velocity (v_{DW}), we divide the total displacement by the total pulse length. Figure 8(b) shows the results from Pt/[Co/Tb/Co]/Tb(2), where v_{DW} is plotted as function of current density j_p for different pulse lengths τ_p . The data exhibit several important features. First, the current required to initiate the DW motion, i.e., the onset of the linear regime, is strongly dependent on the pulse width and is lower for longer pulses. This can be understood by the effect of thermal activation on the DW depinning, which is stronger for longer pulses. Second, in the linear regime the slope v_{DW}/j_p is approximately the same for all pulse widths, suggesting that Joule heating plays a minor role in v_{DW} unlike in the depinning process. In all of the cases, the depinning current in the Pt/[Co/Tb/Co]/Tb multilayers is comparable to that found in Pt/Co_{1-x}Tb_x ferrimagnetic alloys [27]. Third, the extrapolation of the linear fits yields velocities in the range of 10–15 m/s for $j_p = 10^8 \text{ A/cm}^2$. These values are moderate in comparison with those of other ferrimagnetic [27,31,67] and synthetic antiferromagnetic [68] systems despite the strong SOTs. However, we refrain from drawing definitive conclusions on the DW velocity behavior of our films based on the available data because we cannot conclude whether the upturn of v_{DW} is due to the onset of a wide creep regime or the flow regime. In the former case, it is not possible to extrapolate the velocities at higher current density.

Finally, we attempt to quantify the effective DMI field H_{DMI} in all the samples studied above. To do so, we measure j_{depin} as a function of applied in-plane field up to $H_x = 40$ mT, the maximum in-plane field available in the Kerr microscope. If H_x is applied opposite to H_{DMI} , we expect that the DW magnetization rotates first along the y axis, i.e., the DW becomes Bloch-like for $|H_x| \simeq |H_{\text{DMI}}|$, and then Néel-like with right-handed chirality for $|H_x| > |H_{\text{DMI}}|$ [11]. In the applicable in-plane field range,

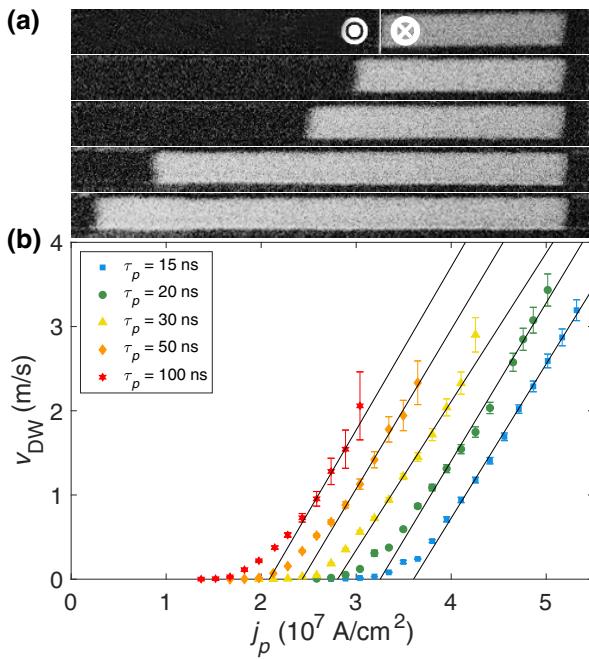


FIG. 8. (a) Series of Kerr differential images showing current-driven DW motion in Pt/[Co/Tb/Co]/Tb(2) as hundreds of 20-ns-long current pulses with $j_p = 3.6 \times 10^7 \text{ A/cm}^2$ amplitude are injected along the track. (b) DW velocity as a function of current density for different pulse widths $\tau_p = 15\text{--}100 \text{ ns}$ in Pt/[Co/Tb/Co]/Tb(2). The errors in the DW velocity are due to the arrival time uncertainty, which is larger when a small number of pulses is used.

however, we do not observe any change in the sign of j_{depin} , indicating that the chirality is not affected by H_x and that $|H_{\text{DMI}}| > 40 \text{ mT}$. These measurements show that H_{DMI} is relatively strong in Pt/[Co/Tb/Co]/Tb.

IV. CONCLUSIONS

Our systematic study of synthetic ferrimagnets based on Co/Tb layers shows that the magnetic properties, SOT efficiency, and switching depend strongly on the stacking sequence of Co and Tb in the heterostructures as well as on the thickness of Tb. In Pt/[Co/Tb/Co]/Tb, the damping-like SOT efficiency reaches 0.3, which we attribute to the additive SOT contributions from the bottom Pt and the top Tb layer. Our conclusion is also supported by harmonic Hall measurements performed in the Tb/Co multilayers with in-plane anisotropy. The high value of the SOT efficiency in Pt/[Co/Tb/Co]/Tb is about two and three times larger than that in Pt/Co and Pt/Tb/[Co/Tb/Co], respectively. The PMA in these multilayers is very strong with effective magnetic anisotropy fields estimated between 1 and 8 T. Despite the large PMA, the critical current for magnetization switching is relatively low, of the order of $(0.5\text{--}2.5) \times 10^7 \text{ A/m}^2$, depending on the assisting in-plane field. Current-induced DW motion measurements reveal

that the DWs are of Néel type with left-handed chirality, stabilized by interfacial DMI similar to Pt/Co bilayers. Our experiments show that synthetic ferrimagnetic heterostructures have comparable or improved PMA, SOT, and DMI relative to ferromagnetic systems and ferrimagnetic alloys. The stacking order offers an additional degree of freedom to tune and maximize these parameters in spintronic devices.

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